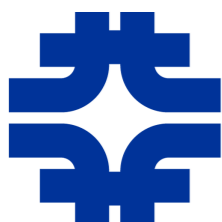
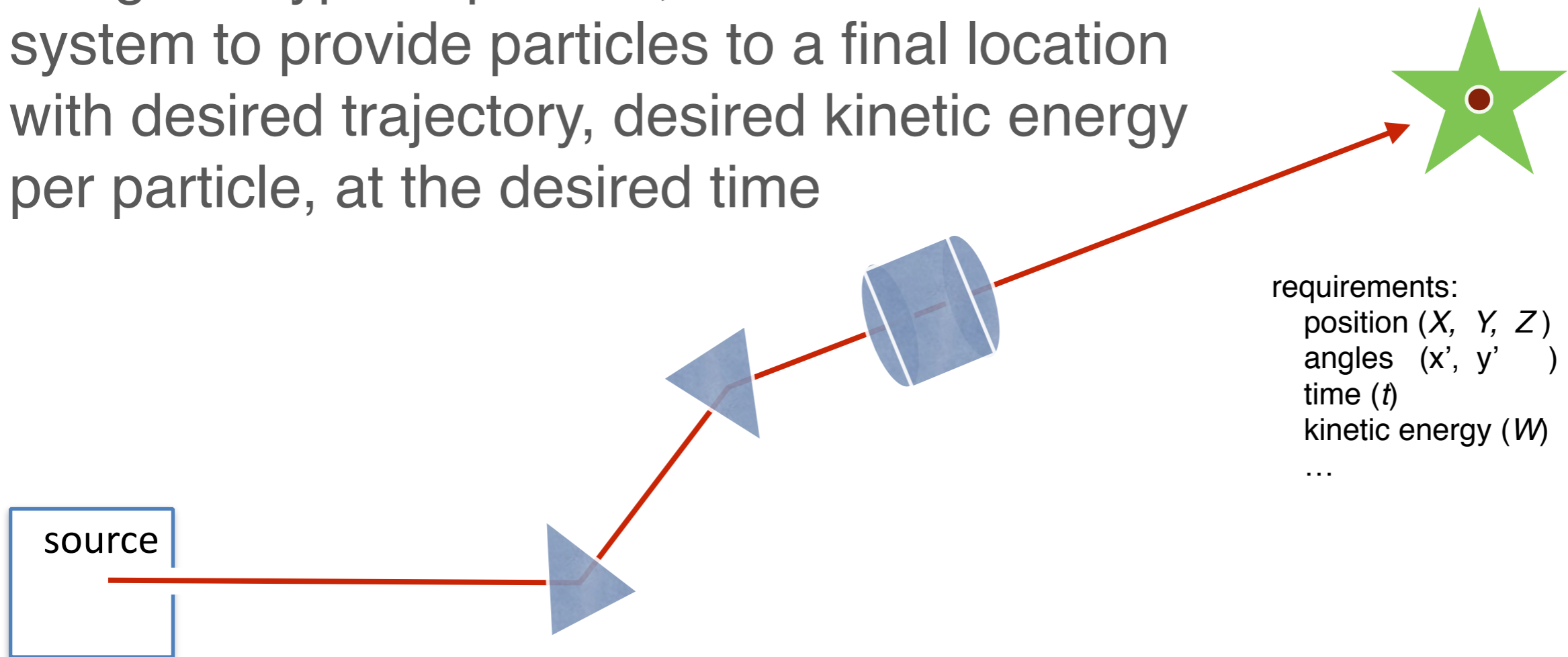


# The Problem

1927: Lord Rutherford requested a “copious supply” of projectiles “more energetic than natural alpha and beta particles”

- For given type of particle, create an ideal system to provide particles to a final location with desired trajectory, desired kinetic energy per particle, at the desired time



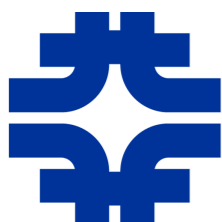
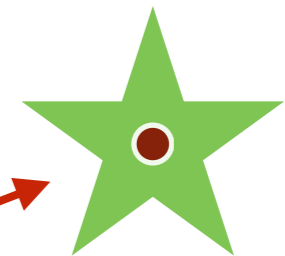
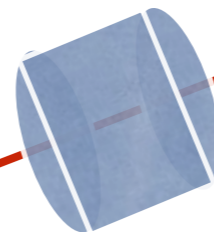
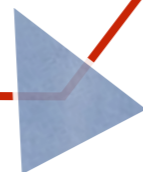
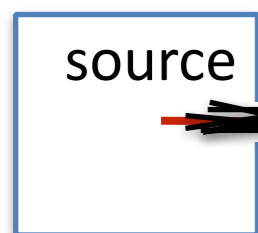
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*and within tolerable spreads of these quantities*

requirements:  
position  $(X, Y, Z)$   
angles  $(x', y')$   
time  $(t)$   
kinetic energy  $(W)$   
...

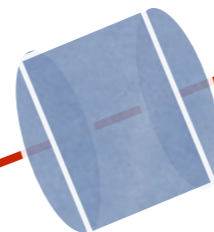
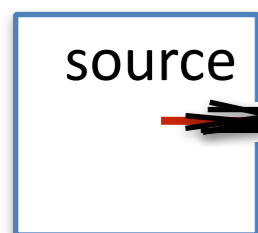


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requirements:  
 position  $(X, Y, Z)$   
 angles  $(x', y')$   
 time  $(t)$   
 kinetic energy  $(W)$   
 ...

within  $dX, dY, dt, dW, \dots$





# A Few Words on Particle Sources...

- Electrons — relatively easy
  - ▶ filaments; photocathodes, laser driven plasmas, ...
- Protons — not “too” hard
  - ▶ ionized hydrogen gas, plasma sources, ...
- Ions — similar techniques
  - ▶ ovens, plasma sources, ECRs — plus, separation
- Even more exotic particles: target, separate, collect
  - ▶ heavy ion isotopes
  - ▶ pions, muons, antiprotons, neutrinos, ...
- Also polarized sources, ...





# A Little Accelerator History



Northern Illinois  
University

## ■ DC Acceleration

1927: Lord Rutherford requested a “copious supply” of projectiles more energetic than natural alpha and beta particles. At the opening of the resulting High Tension Laboratory, Rutherford went on to reiterate the goal:

“What we require is an apparatus to give us a potential of the order of 10 million volts which can be safely accommodated in a reasonably sized room and operated by a few kilowatts of power. We require too an exhausted tube capable of withstanding this voltage... I see no reason why such a requirement cannot be made practical.”



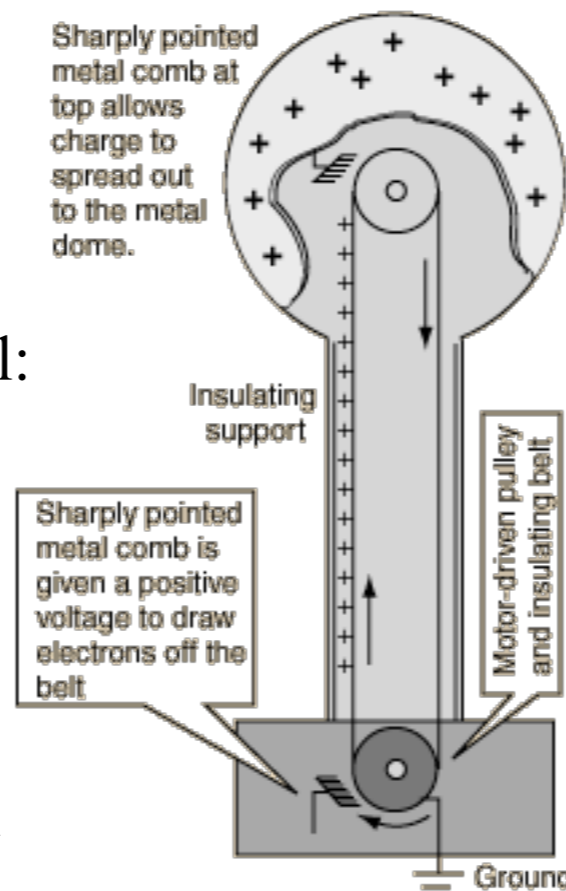
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Van de Graaff  
(1929)



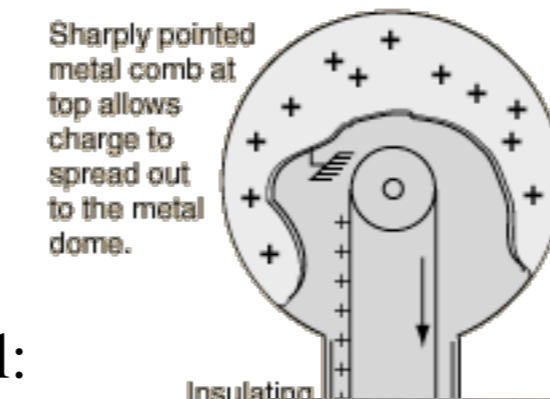
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## ■ DC Acceleration

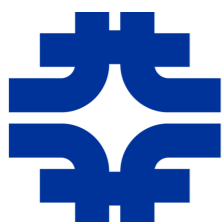
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Sharply pointed metal comb is given a positive voltage to draw electrons off the belt





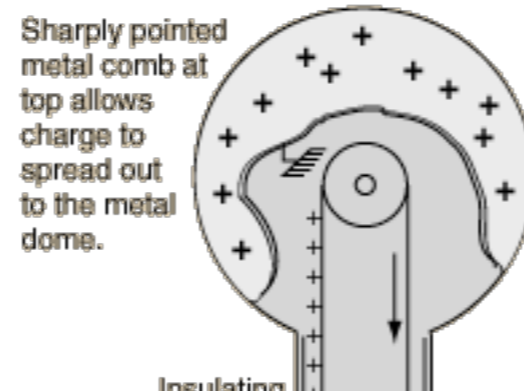
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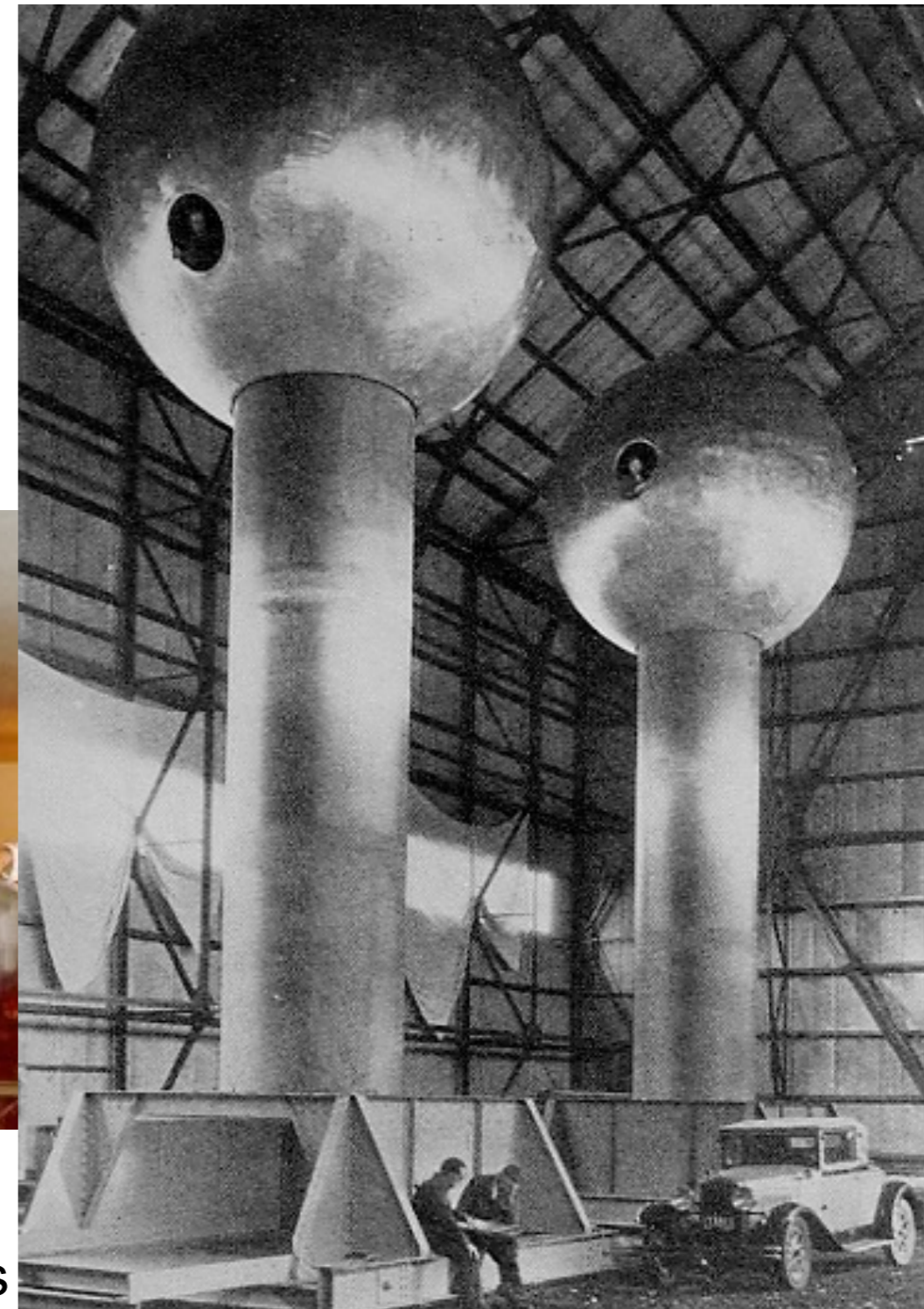
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Insulating supp

Sharply pointed metal comb is given a positive voltage to draw electrons off the belt



MIT, c.1940s





# A Little Accelerator History

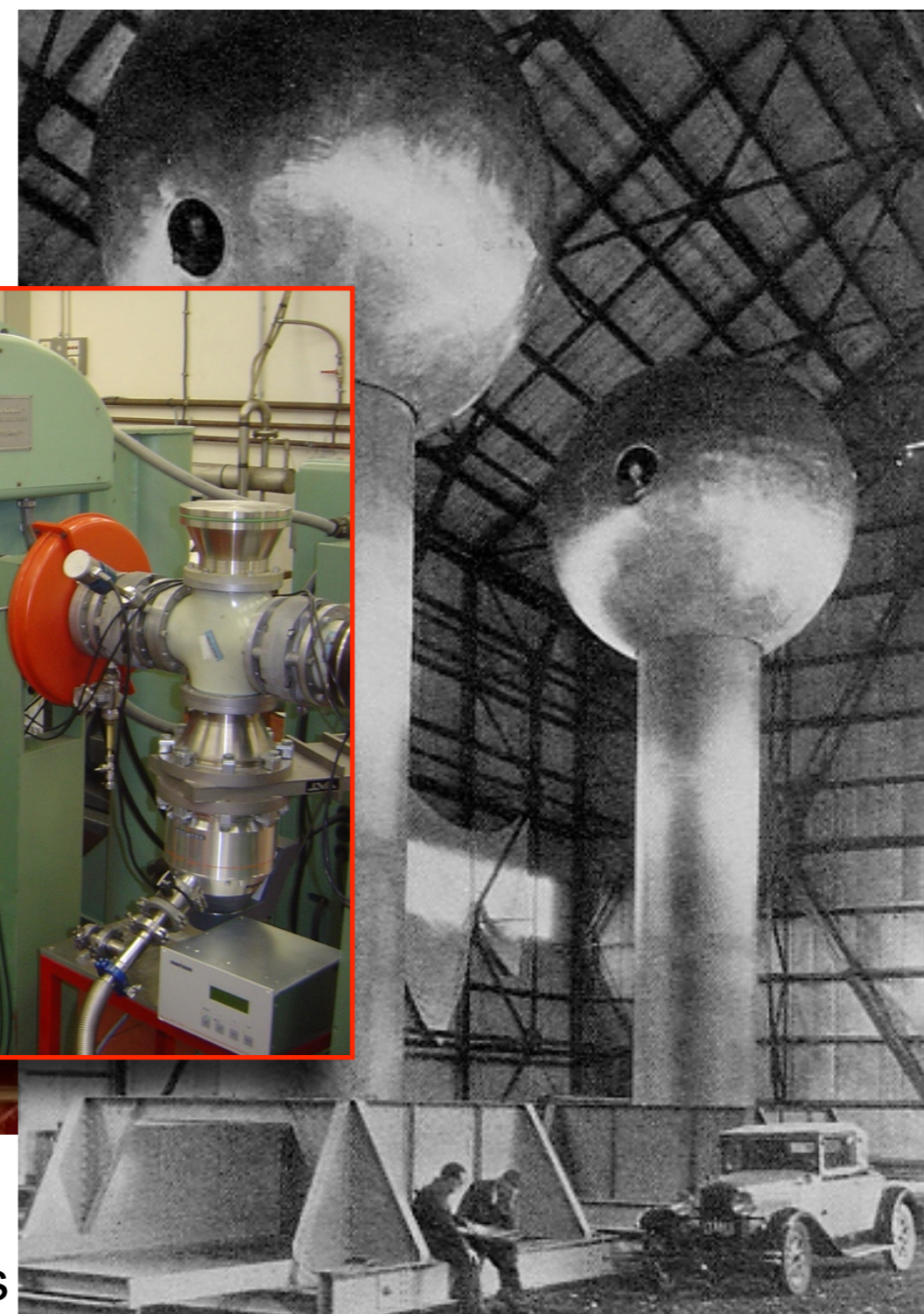
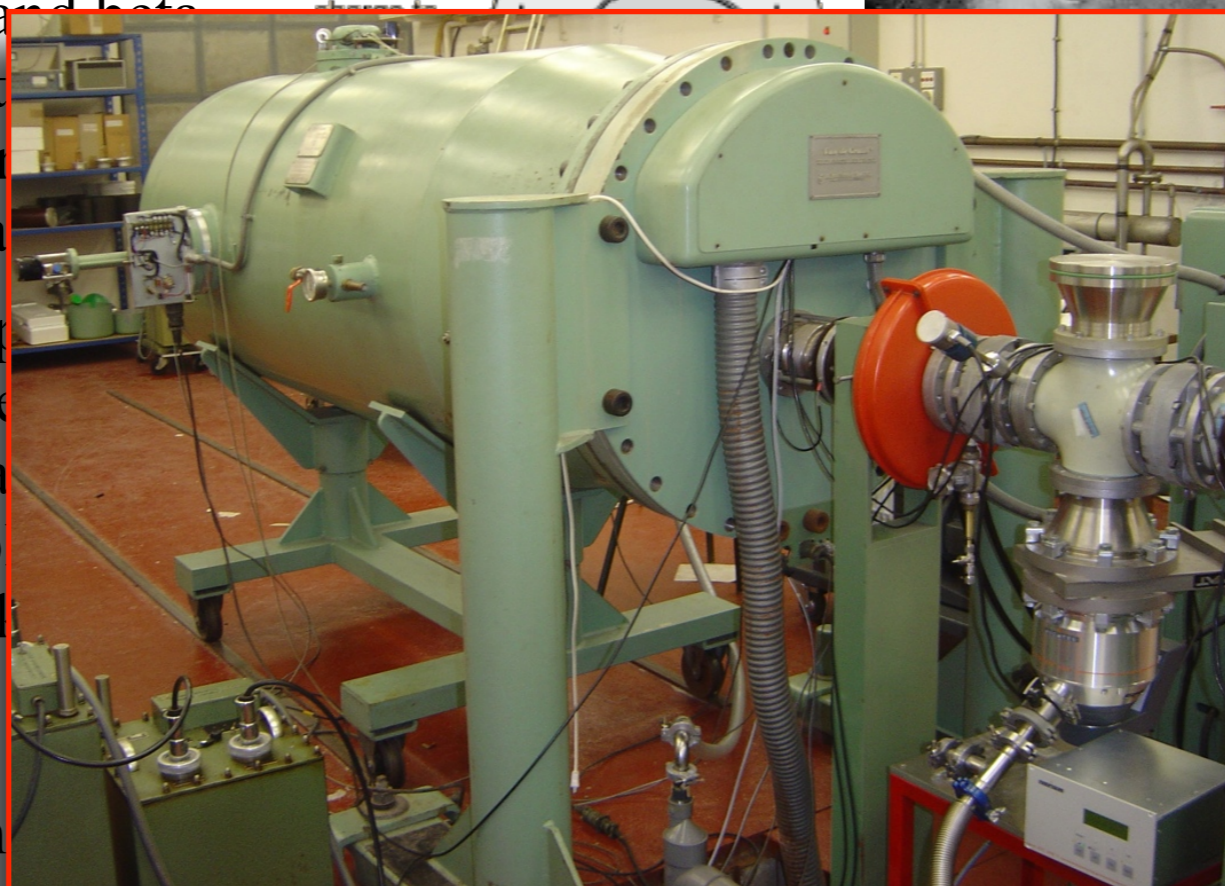
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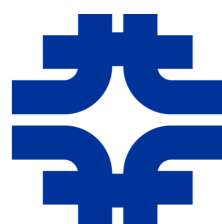
“What we require is an apparatus which will give us a potential of the order of a few million volts which can be safely accommodated in a reasonable sized room and operated by a few kilowatts of power. We require too an evacuated tube capable of withstanding such a high voltage... I see no reason why this requirement cannot be made practical.”

Van de Graaff  
(1929)

Sharply pointed metal comb at top allows charge to be transferred to the top sphere.



MIT, c.1940s



# Cockcroft and Walton



## ■ Voltage Multiplier

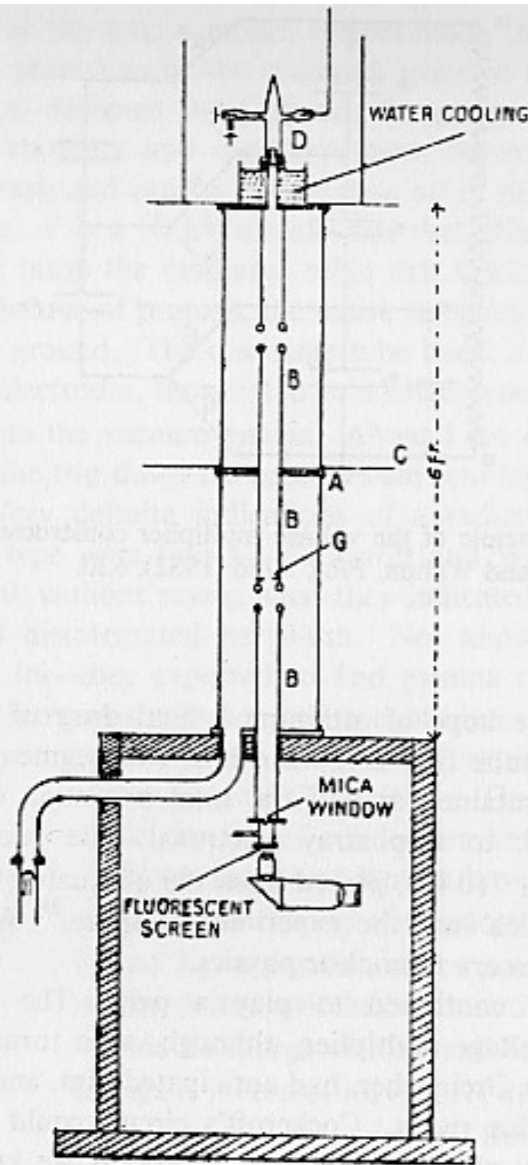


FIG. 2.11 Accelerating tube and target arrangement of the Cockcroft-Walton machine. The source is at D; C is a metallic ring joint between the two sections of the constantly pumped tube. The mica window closes the evacuated space. Cockcroft and Walton, *PRS*, A136 (1932), 626.





# Cockcroft and Walton

## Voltage Multiplier

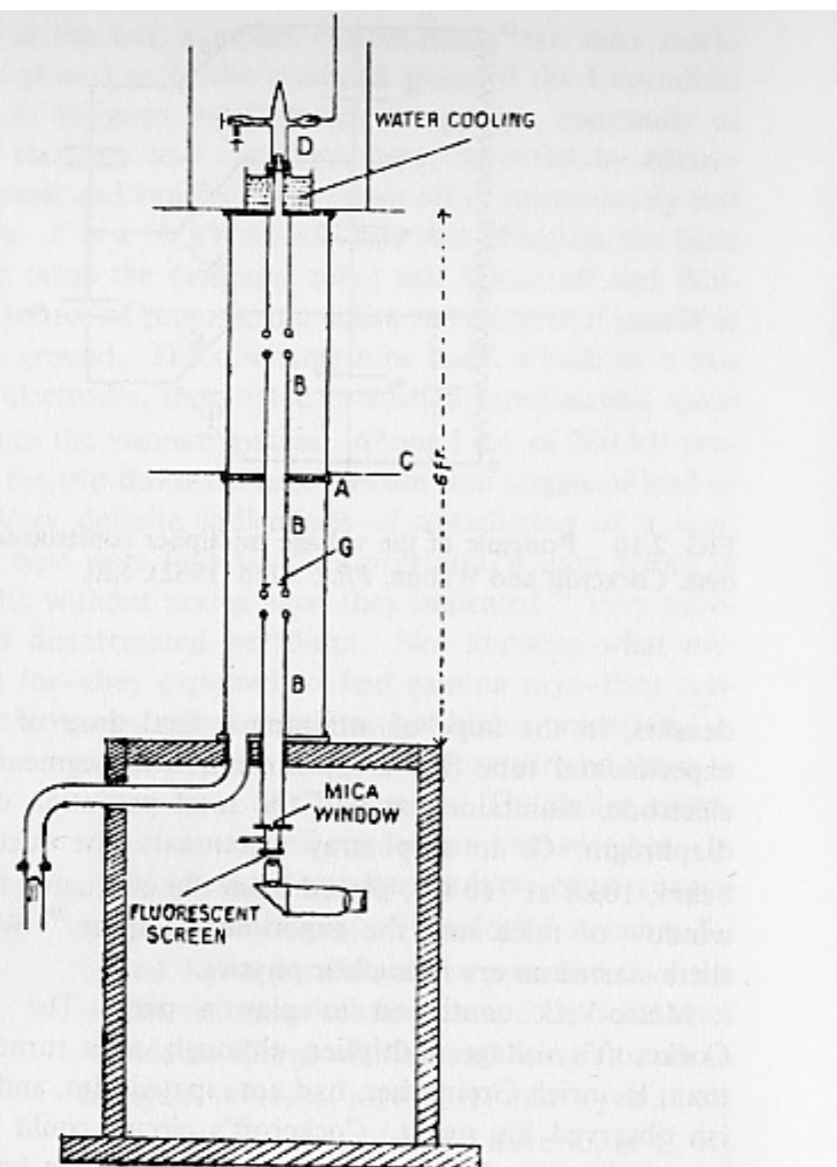
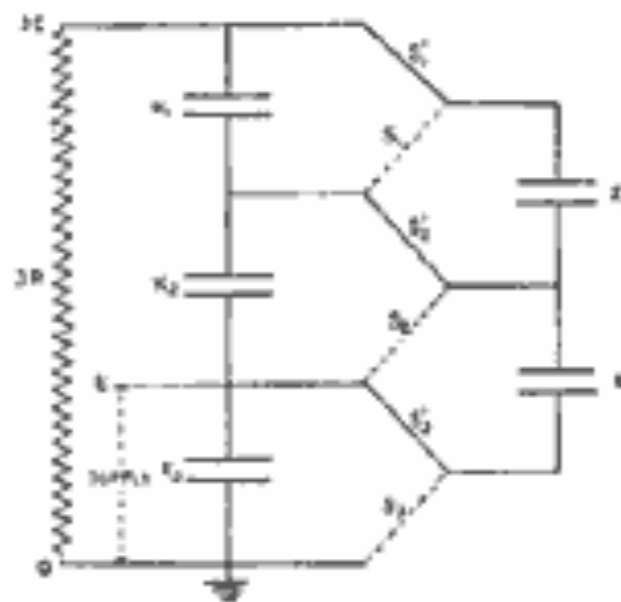
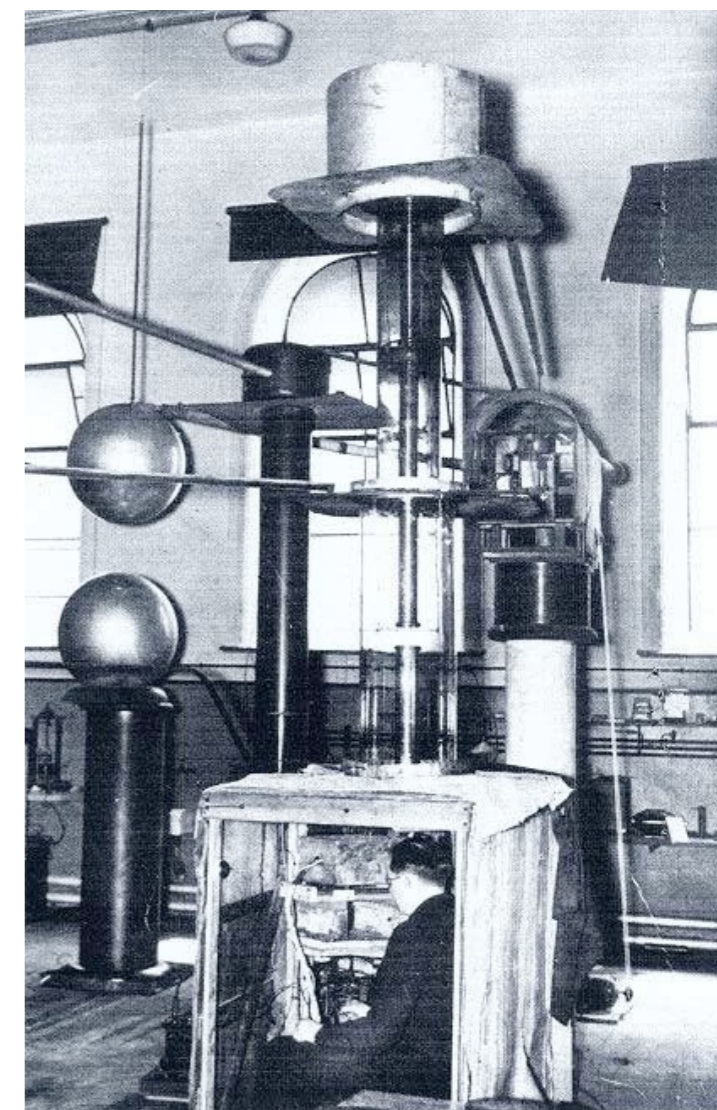


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Converts AC voltage  $V$  to DC voltage  $n \times V$





# Cockcroft and Walton



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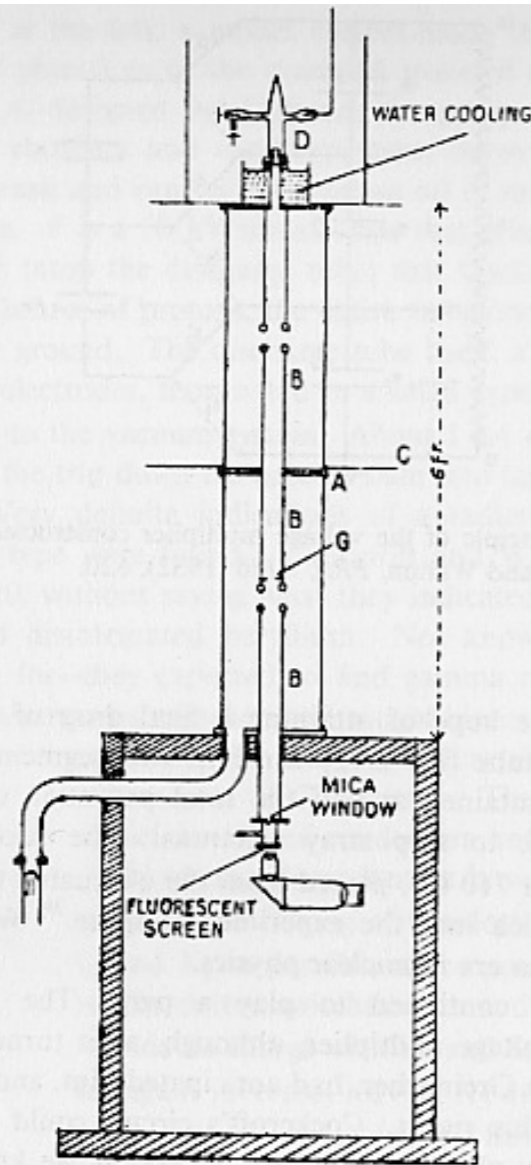
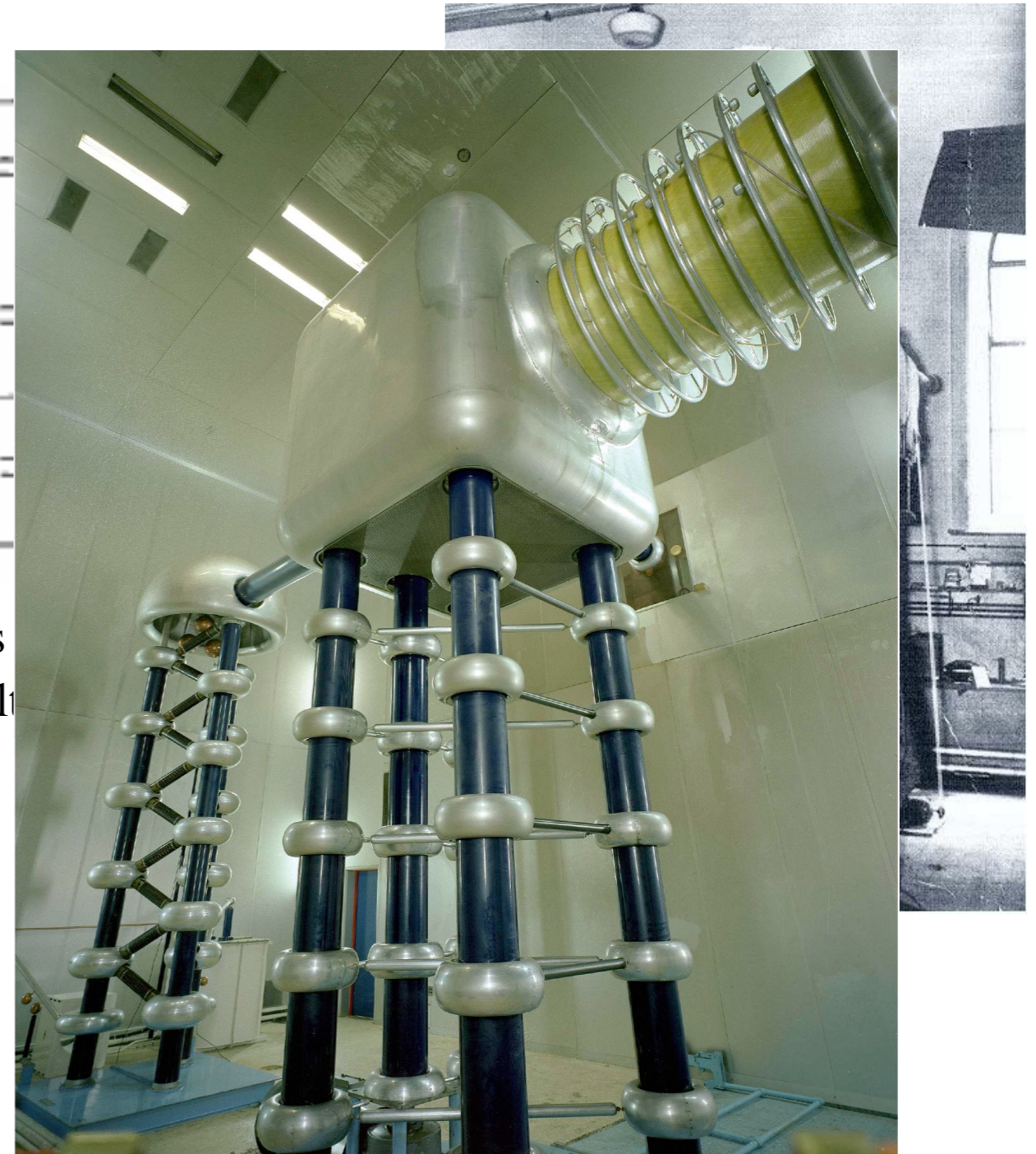


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Converts  
DC volt



*Fermilab (recently decommissioned)*





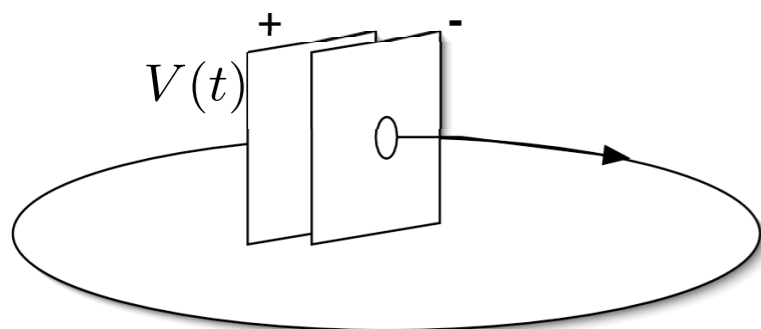
# The Route to Higher Energies

- The need for AC systems
- The Need for AC Systems...

energy gain =  $q \cdot V$

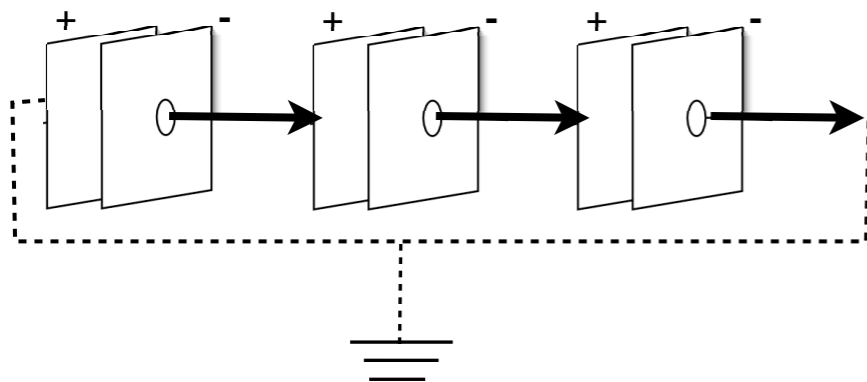
DC systems limited to a few MV

Circular Accelerator



$$\oint (q\vec{E}) \cdot d\vec{s} = \text{work} = \Delta(\text{energy})$$

Linear Accelerator



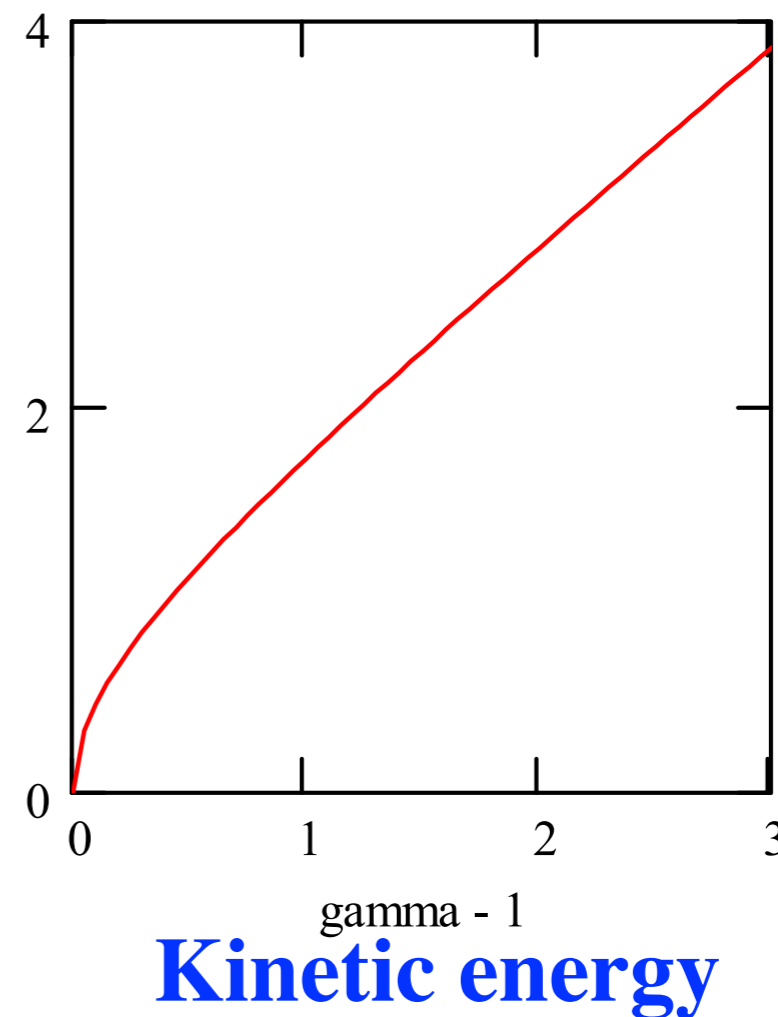
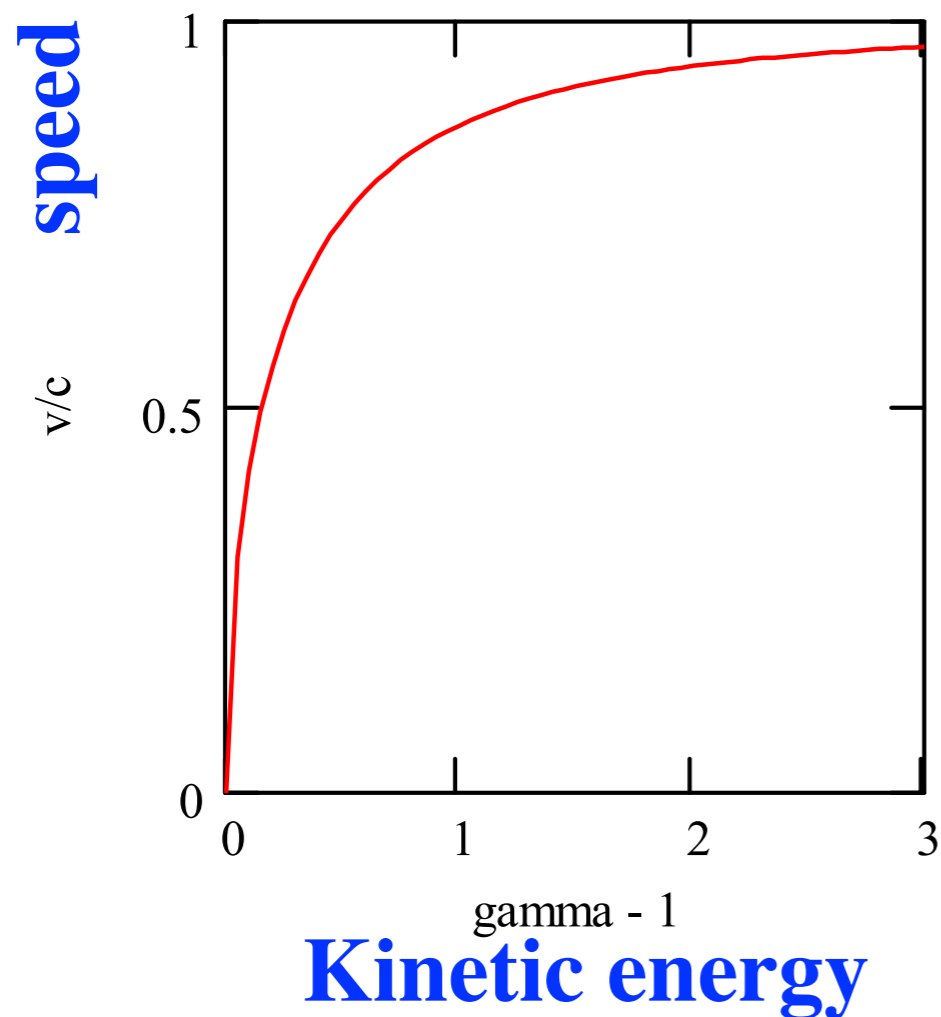
To gain energy, a time-varying field is required:

$$\oint \vec{E} \cdot d\vec{s} = -\frac{\partial}{\partial t} \oint \vec{B} \cdot d\vec{A}$$





# Speed, Momentum vs. Energy



Electron: 0    0.5    1.0    1.5    MeV  
 Proton: 0    1000    2000    3000    MeV

$$\text{gamma} = \frac{1}{\sqrt{1 - (v/c)^2}}$$

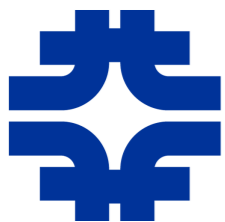
rest energy, $mc^2$ :	
e-	0.5 MeV
p	938 MeV



# Oscillating Fields



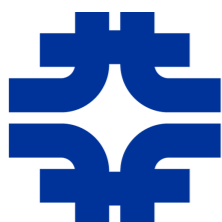
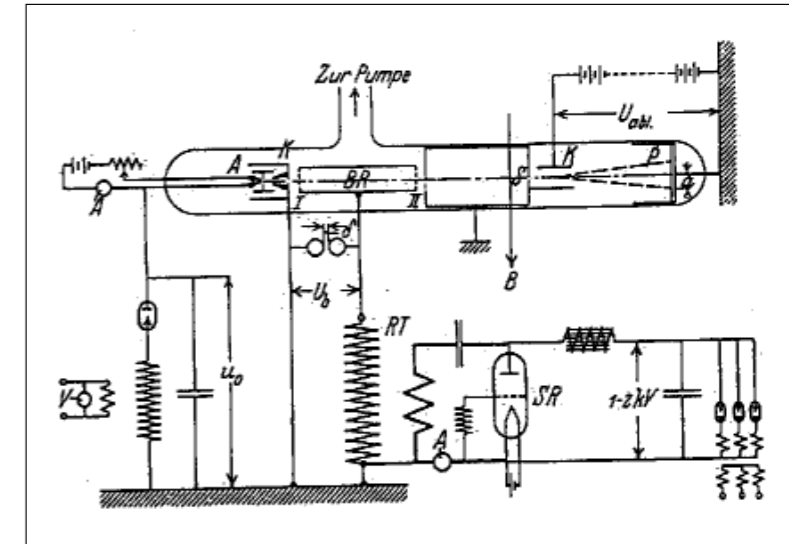
Northern Illinois  
University



# Oscillating Fields

## → The linear accelerator (linac) -- 1928-29

- Wideroe (U. Aachen; grad student!)
  - Dreamt up concept of “Ray Transformer” (later, called the “Betatron”); thesis advisor said was “sure to fail,” and was rejected as a PhD project. Not deterred, illustrated the principle with a “linear” device, which he made to work -- got his PhD in engineering
- 50 keV; accelerated heavy ions ( $K^+$ ,  $Na^+$ )
- utilized oscillating voltage of 25 kV @ 1 MHz



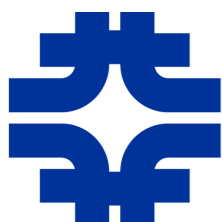
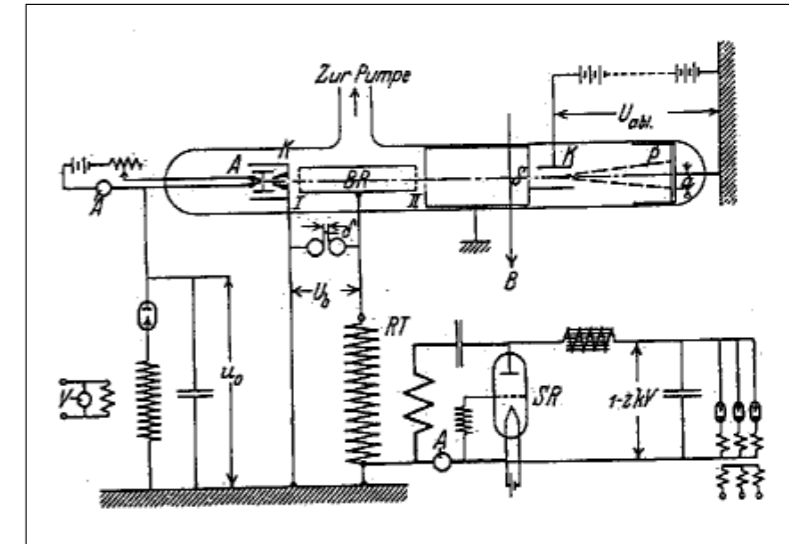
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## → The Cyclotron -- 1930's, Lawrence (U. California)

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- an extended “linac” unappealing -- make it more compact:



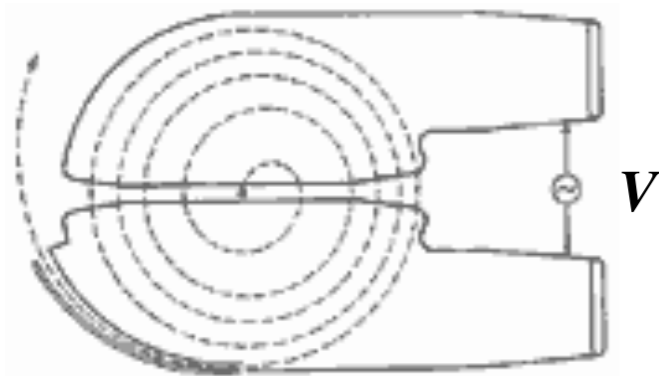
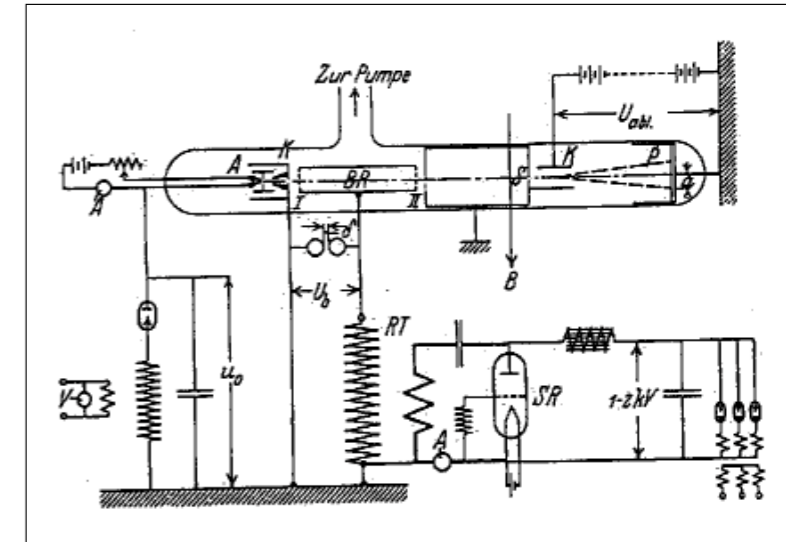
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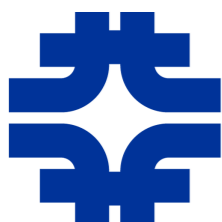
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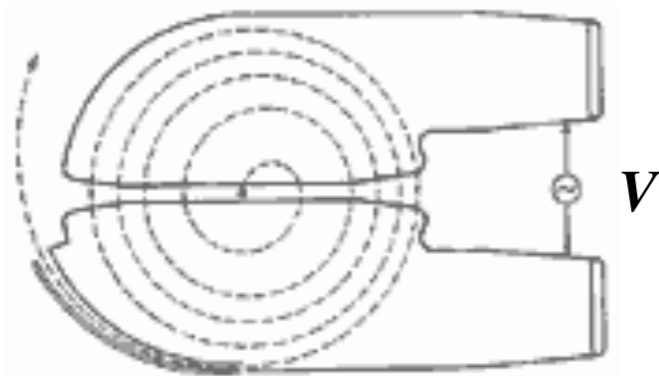
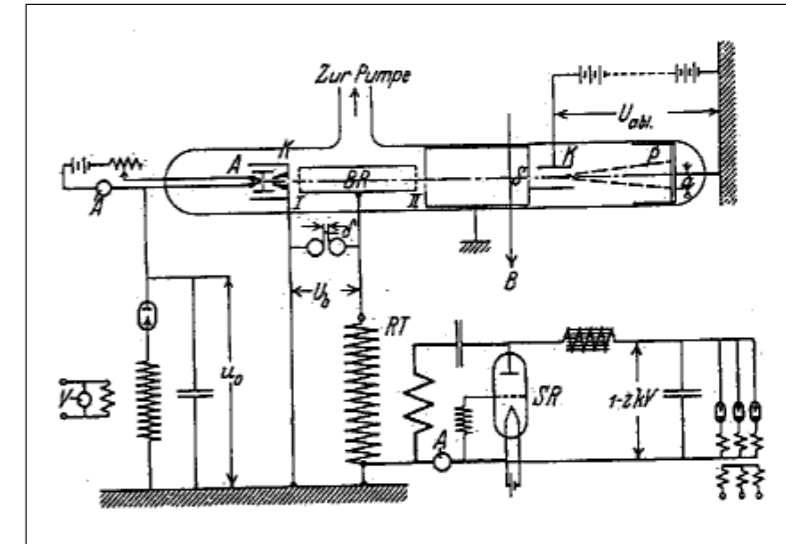
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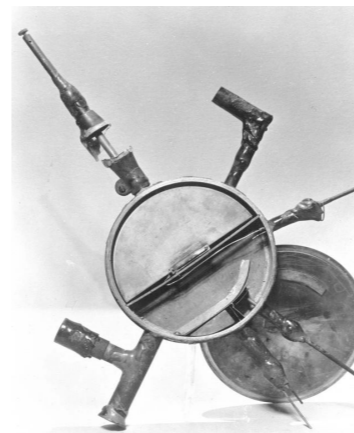
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4.5 inch diameter!





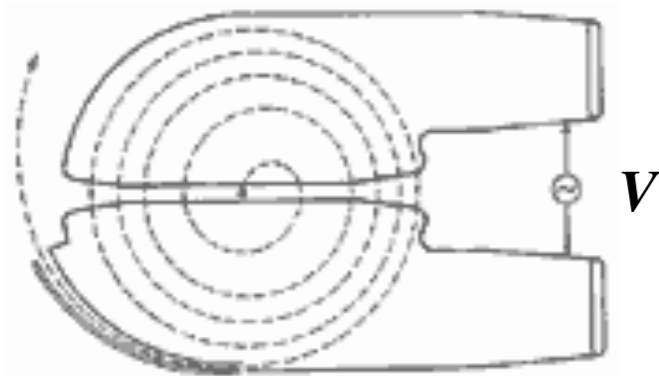
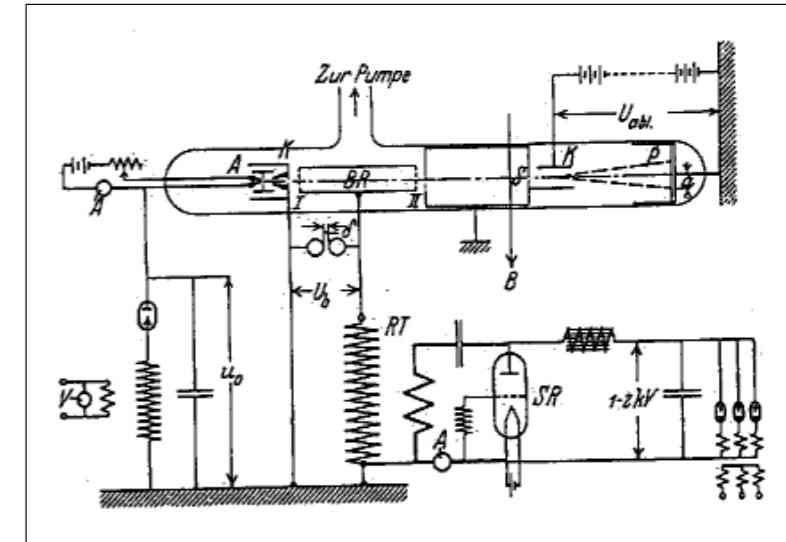
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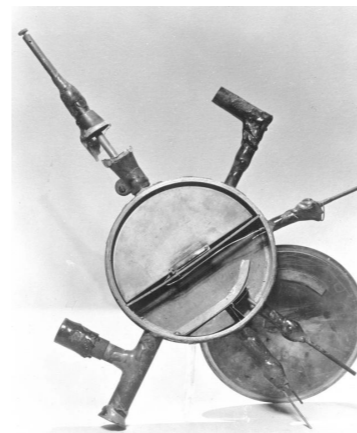
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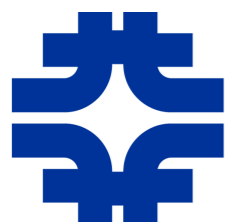
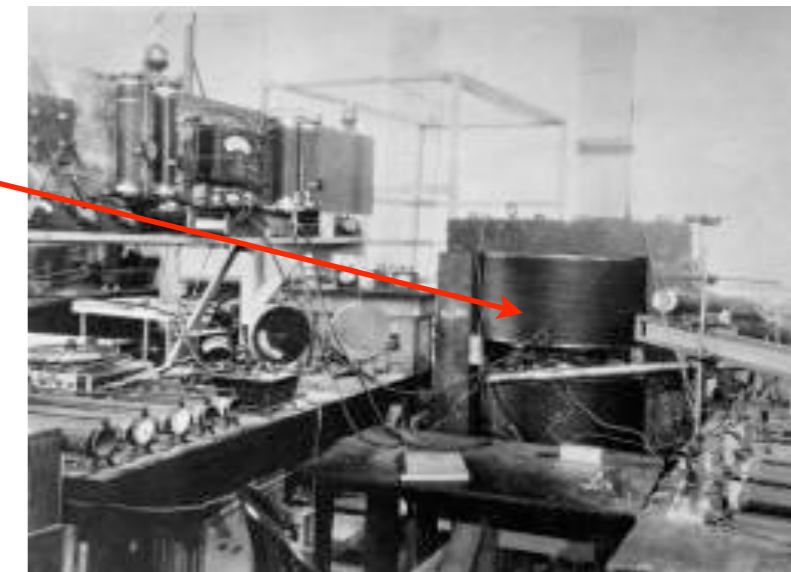


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4.5 inch diameter!



11 inch diameter

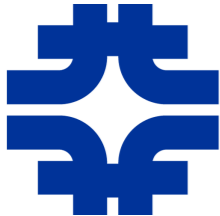




# 60-inch Cyclotron, Berkeley -- 1930's



Northern Illinois University



# 184-inch Cyclotron, Berkeley -- 1940's



Northern Illinois  
University





# 184-inch Cyclotron, Berkeley -- 1940's



Northern Illinois University



# Meeting up with Relativity

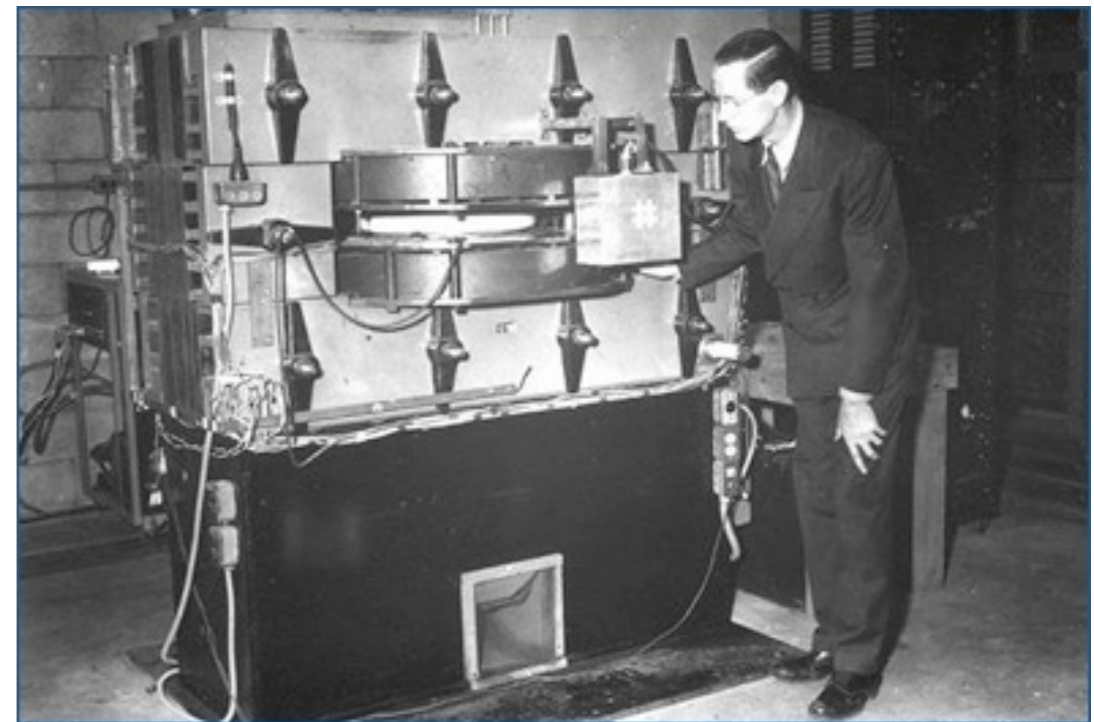
- **The Synchrocyclotron (FM cyclotron) -- 1940's**
  - beams became relativistic (esp. e<sup>-</sup>) --> oscillation frequency no longer independent of momentum; cyclotron condition no longer held throughout process; thus, modulate freq.

- **The Betatron -- 1940, Kerst (U. Illinois)**

- induction accelerator

$$\gg \oint \vec{E} \cdot d\vec{s} = -\frac{\partial}{\partial t} \oint \vec{B} \cdot d\vec{A}$$

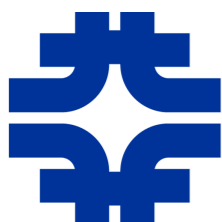
- » used for electrons
- » beam dynamics heavily studied
  - “betatron oscillations”



~ 2 MeV; later models --> 300 MeV

- **The Microtron --1944, Veksler (Russia)**

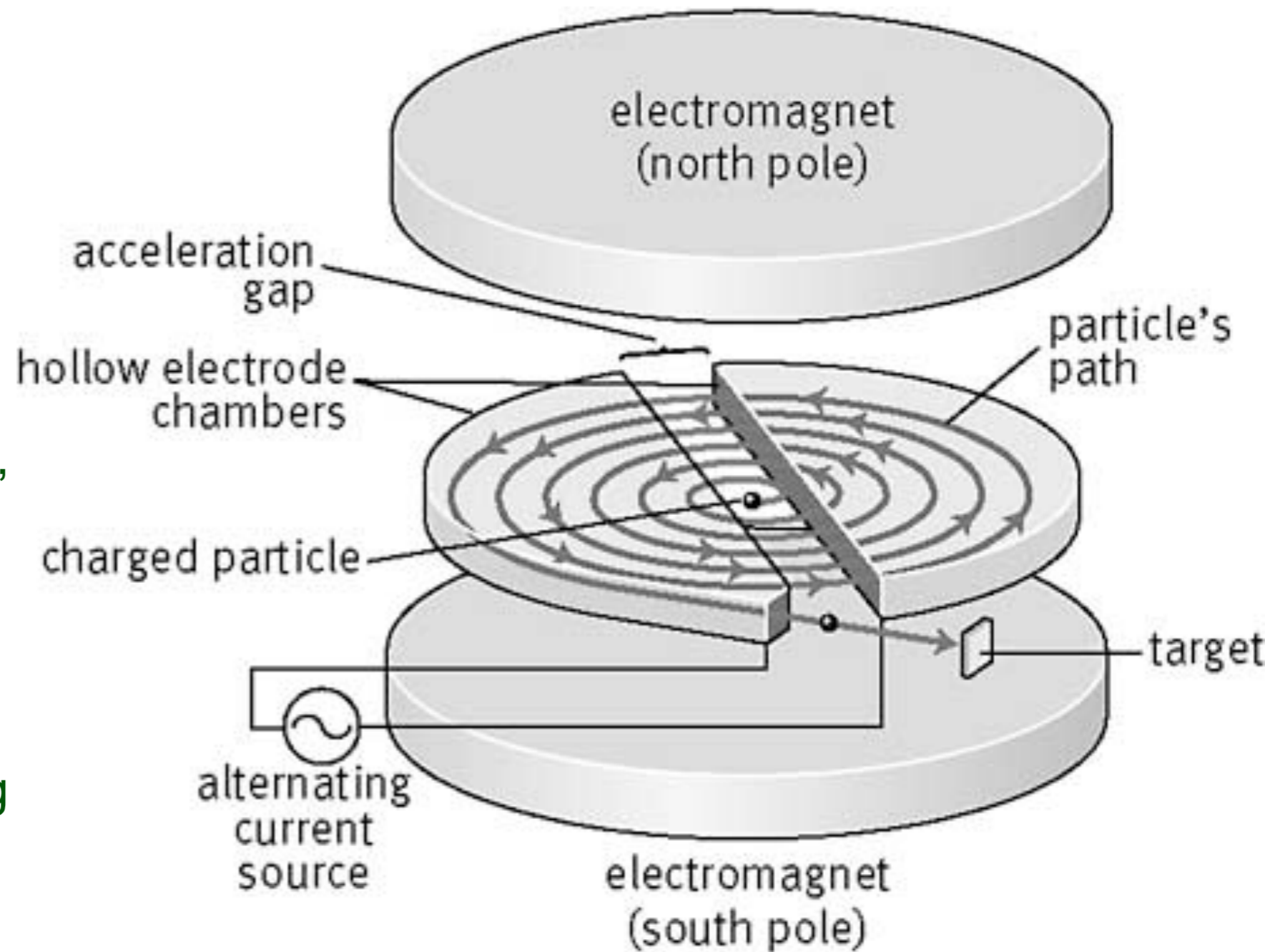
- use one cavity with one frequency, but vary path length each “revolution” as function of particle speed





# Cyclotrons

- Relatively easy to operate and tune (only a few parts).
- Tend to be used for isotope production and places where reliable and reproducible operation are important
- Intensity is moderately high, acceleration efficiency is high, cost low
- Relativity is an issue, so energy is limited to a few hundred MeV/u.
- RIKEN Superconducting Ring Cyclotron 350 MeV/u



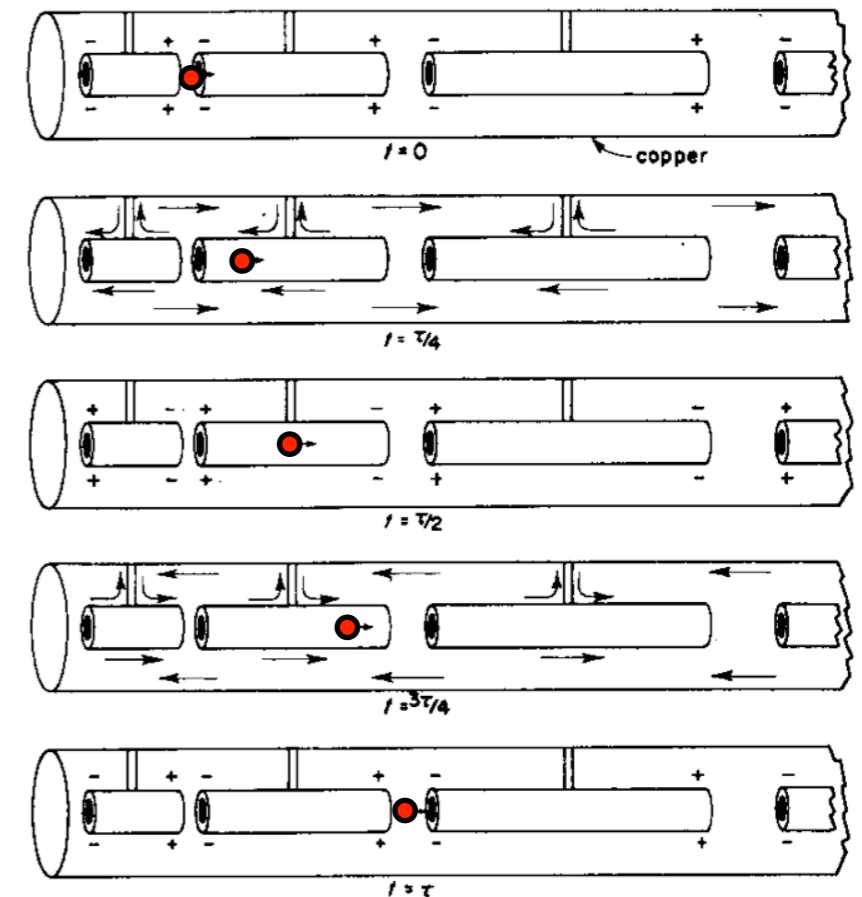
Precision Graphics

<http://images.yourdictionary.com/cyclotron>



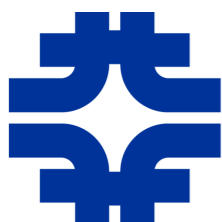
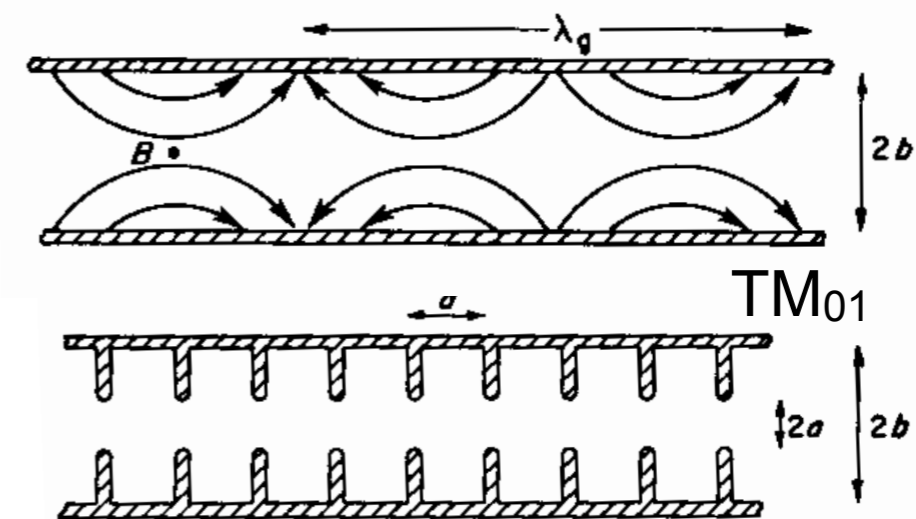
# The “Modern” Linear Accelerator

- Alvarez -- 1946 (U. California)
  - cylindrical cavity with drift tubes
  - particles “shielded” as fields change sign
  - most practical for protons, ions
  - GI surplus equip. from WWII Radar technology

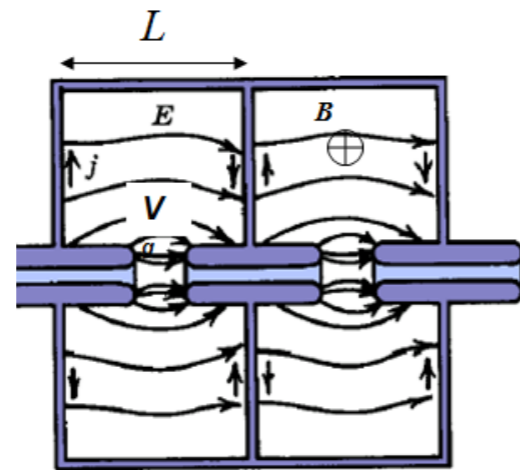


- Traveling-Wave Electron Accelerator -- c.1950 (Stanford, + Europe)

- $TM_{01}$  waveguide arrangement
- iris-loaded cylindrical waveguide
  - » match phase velocity w/ particle velocity...



# Radio-frequency Resonant Cavities



$$\oint \vec{E} \cdot d\vec{r} = -\frac{d\Phi_B}{dt}$$

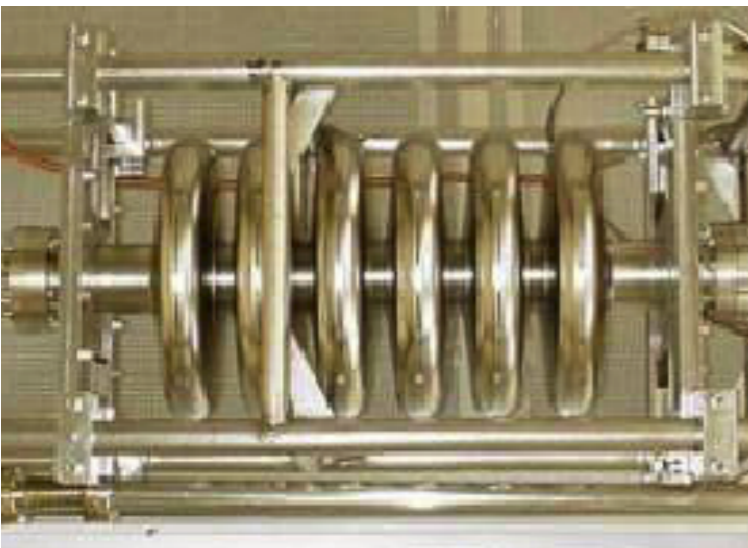
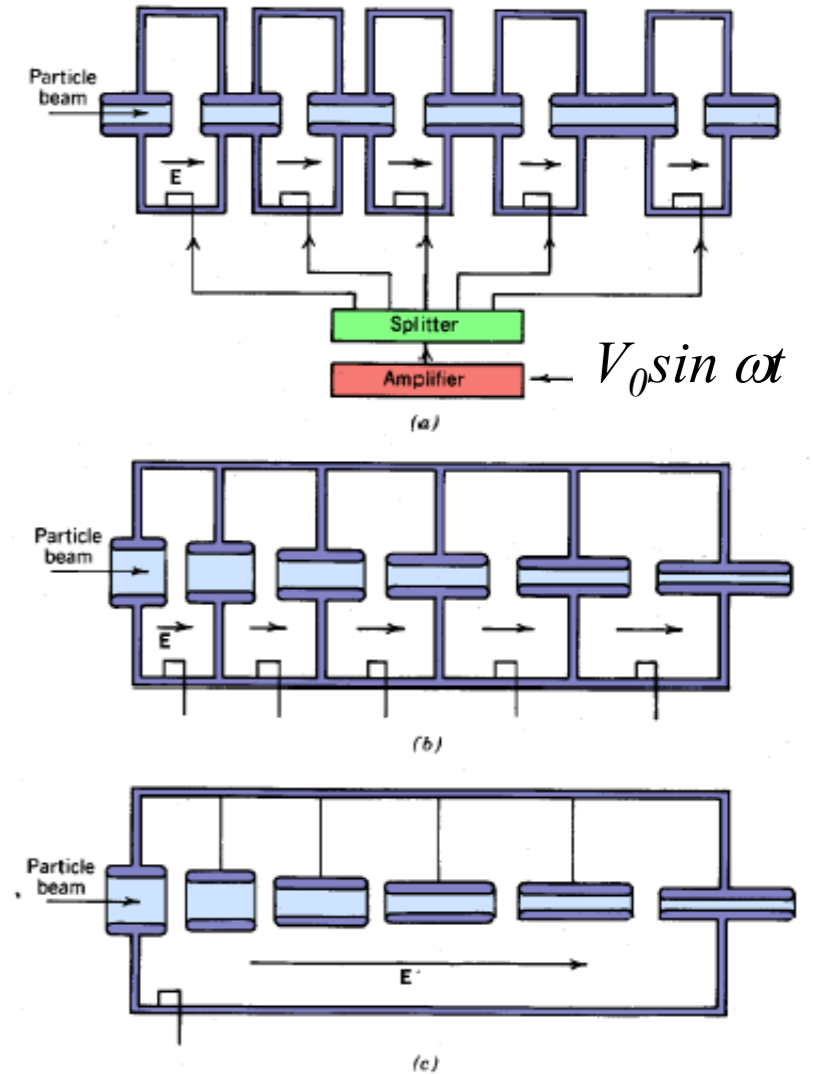
Time varying: we can use many cavities in series!

- Resonant cavities reduce rf power consumption, increase gradient and efficiency
- Long cavities (with many gaps) are generally more efficient

**Accelerating field**  $E_a = V_g/L$

**Stored EM energy**  $U \propto E_a^2$

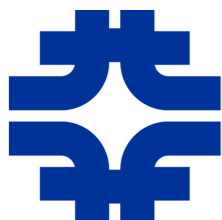
**Quality Factor**  $Q = \omega U/P = I/R_s$



A. Facco –FRIB and INFN

SRF Low-beta Accelerating Cavities for FRIB

MSU 4/10/2011



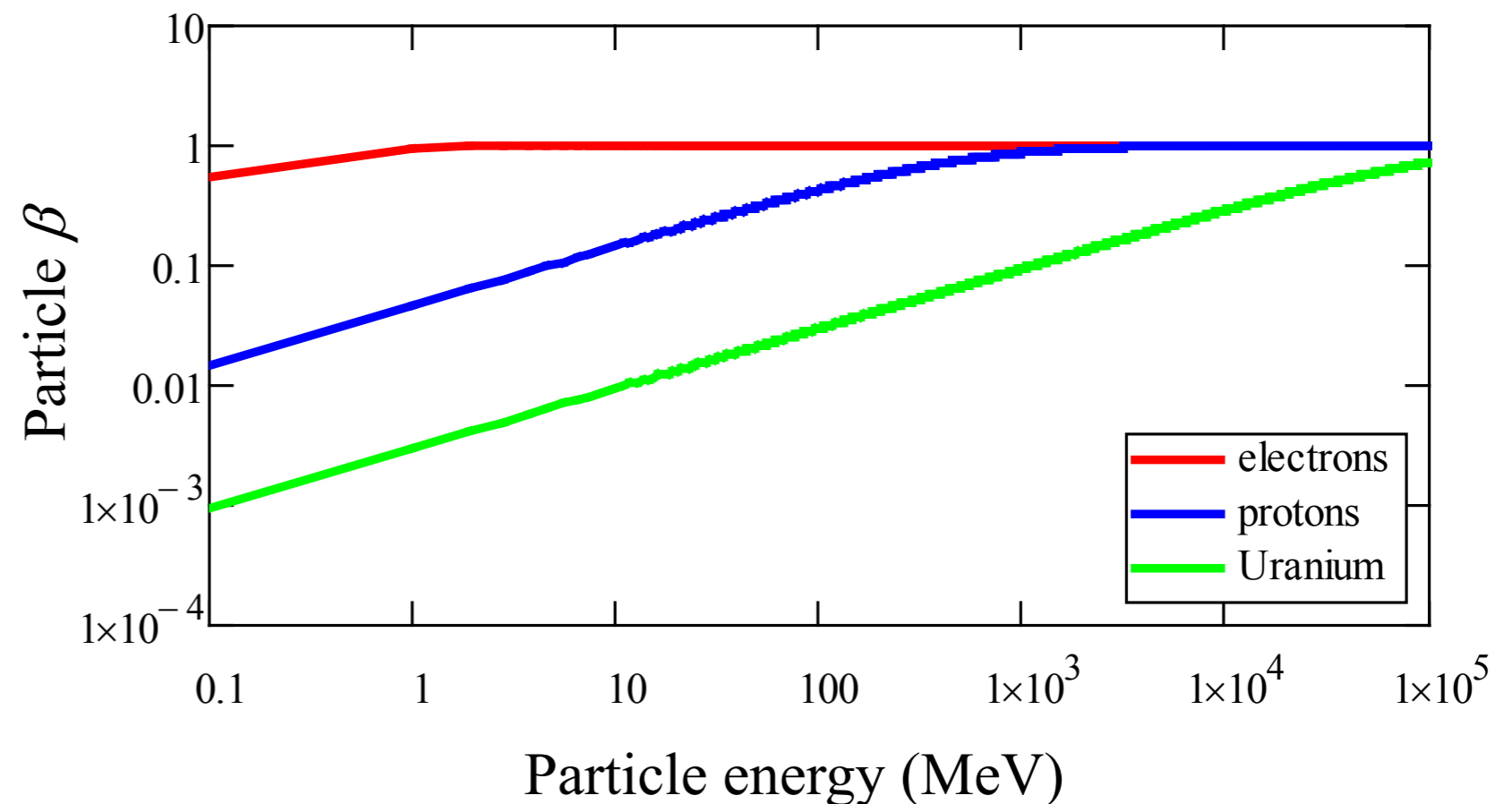
# Different Arrangements for Different Particles



- Accelerating system used will depend upon the evolution of the particle velocity along the system
  - electrons reach a constant velocity at relatively low energy
    - » thus, can use one type of resonator
  - heavy particles reach a constant velocity only at very high energy
    - » thus, may need different types of resonators, optimized for different velocities

*Particles rest mass:*

- $e$       $0.511 \text{ MeV}$
- $p$       $938 \text{ MeV}$
- $^{239}\text{U}$       $\sim 220000 \text{ MeV}$

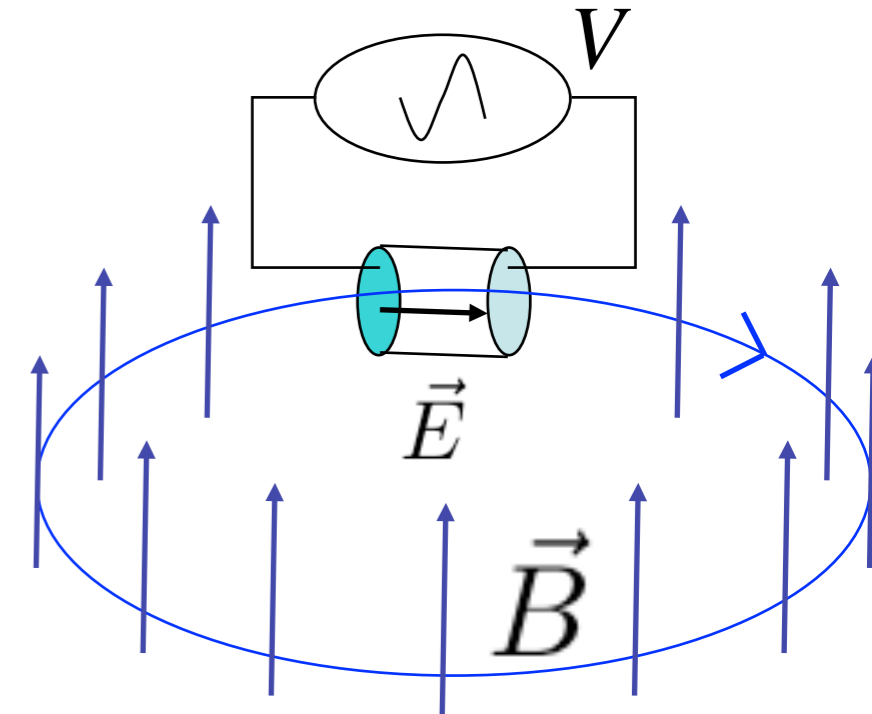
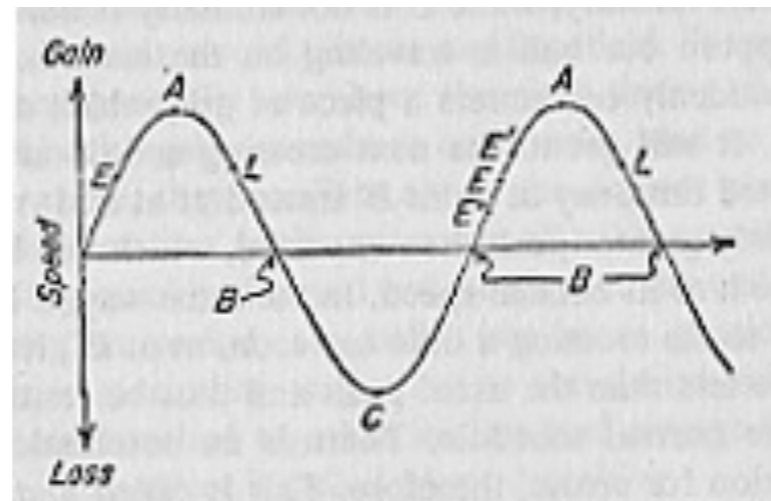




# For Highest Elementary Particle Energies...



- ... the **Synchrotron** -- late 1940's
  - RF powered cavity(ies); Radar power sources
  - keep  $R = \text{const.}$ ; increase  $B (= p/eR)$
  - 1<sup>st</sup> in U.S. was at G.E. research lab, 70 MeV
- principal of phase stability
  - McMillan (U. California), ...
  - ... and Veksler (again)



- arrive late, gain energy; arrive early, get less --
  - » **restoring force -> energy oscillation**
- as strength of  $B$  raised adiabatically, the oscillations will continue about the “*synchronous*” momentum, defined by  $p/e = B \cdot R$  for constant  $R$  :

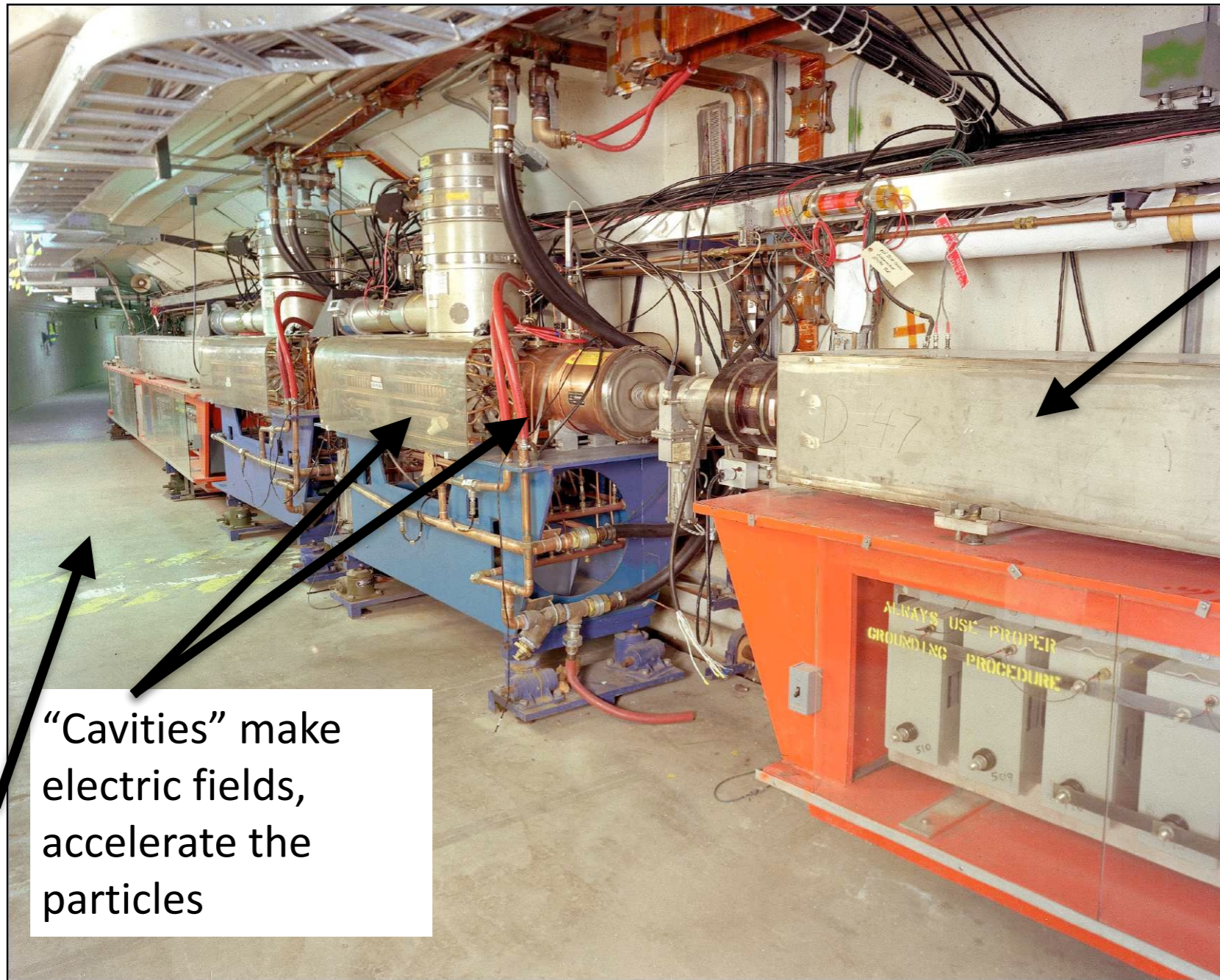


## Synchrotron Oscillations

# A Synchrotron



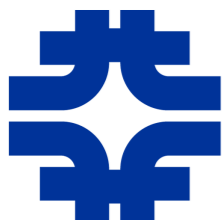
Northern Illinois University



“Cavities” make electric fields, accelerate the particles

Magnets steer the particles in a circle

Booster Synchrotron, Fermilab (Batavia, IL)

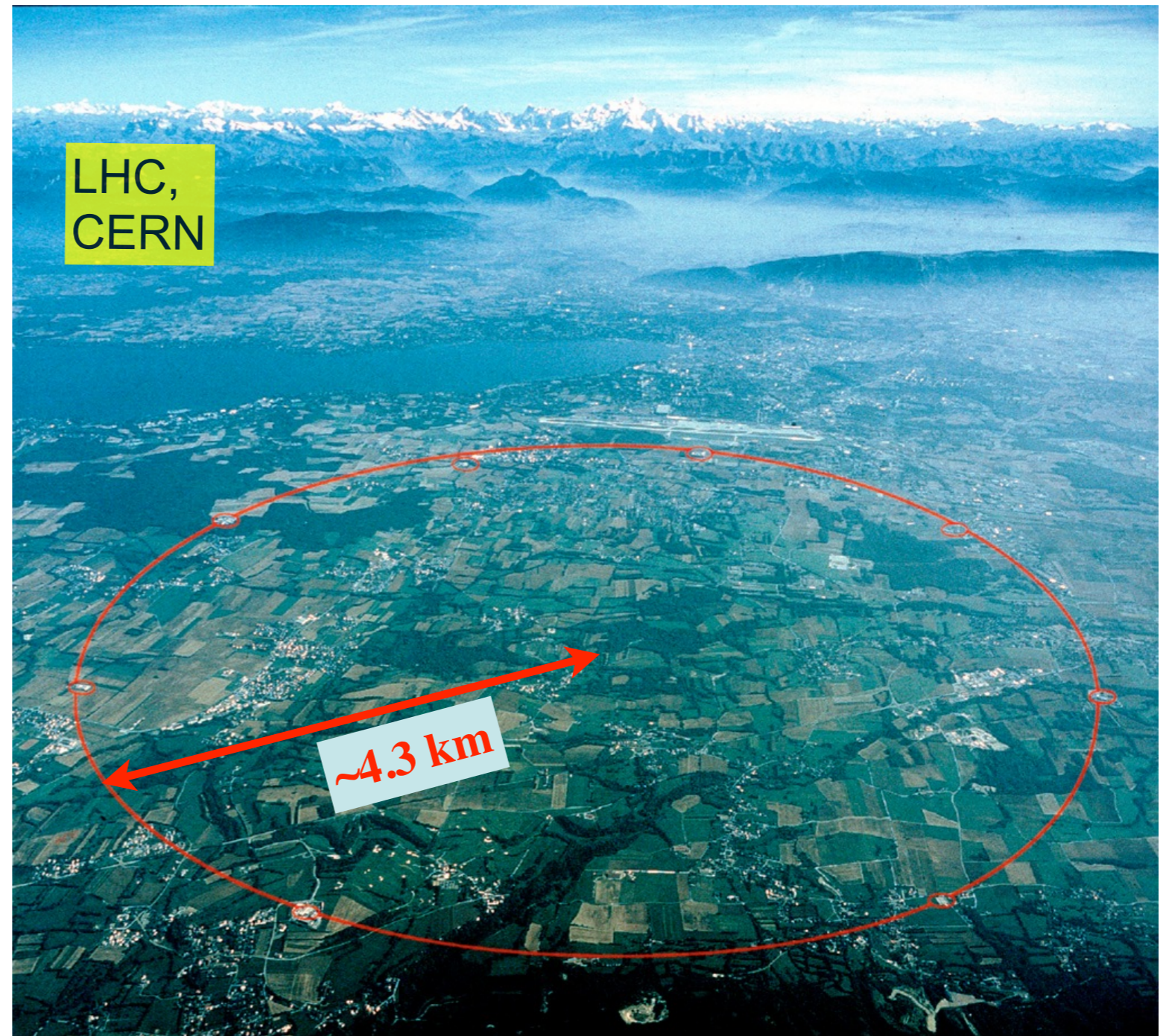




# The Large Colliders



Northern Illinois University





# Fixed Target Energy vs. Collider Energy



Northern Illinois  
University

- Beam/target particles:

$$E_0 \equiv mc^2$$

before

after



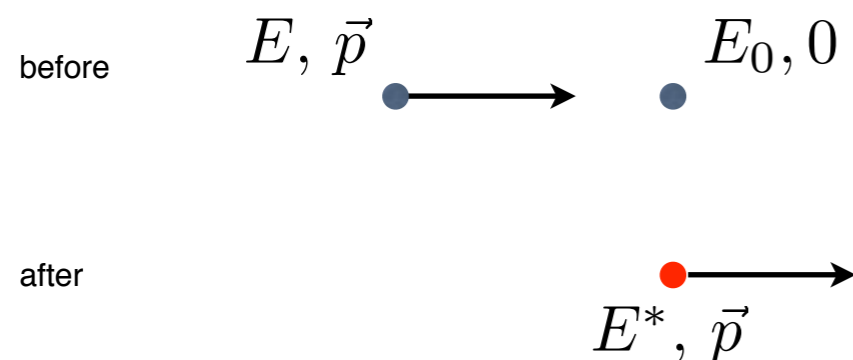


# Fixed Target Energy vs. Collider Energy

- Beam/target particles:

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Fixed Target





# Fixed Target Energy vs. Collider Energy

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Fixed Target



$$\begin{aligned}
 E^{*2} &= (m^*c^2)^2 + (pc)^2 &= [E_0 + E]^2 \\
 & &= E_0^2 + 2E_0E + (E_0^2 + (pc)^2) \\
 m^*c^2 &= \sqrt{2} E_0 [1 + \gamma_{FT}]^{1/2}
 \end{aligned}$$





# Fixed Target Energy vs. Collider Energy

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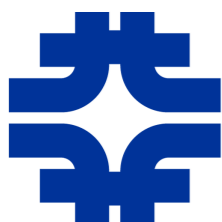
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Fixed Target

Collider



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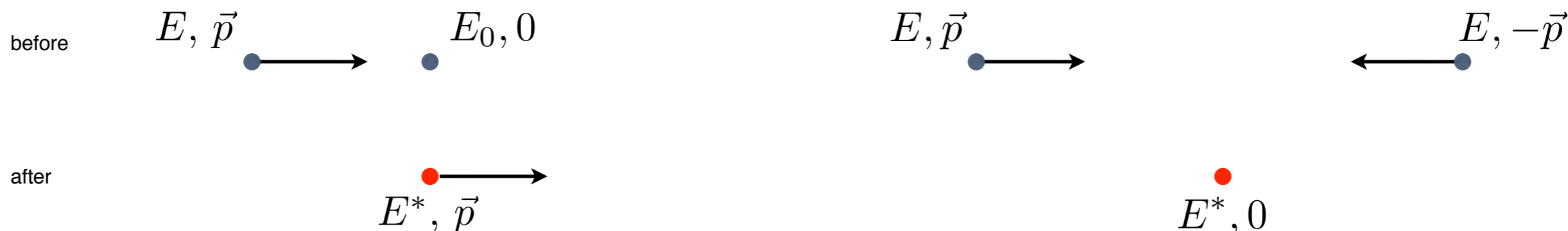
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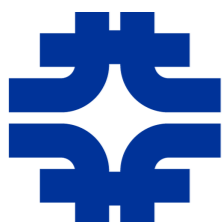
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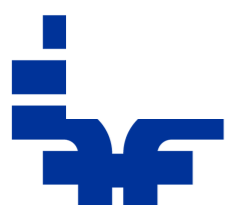
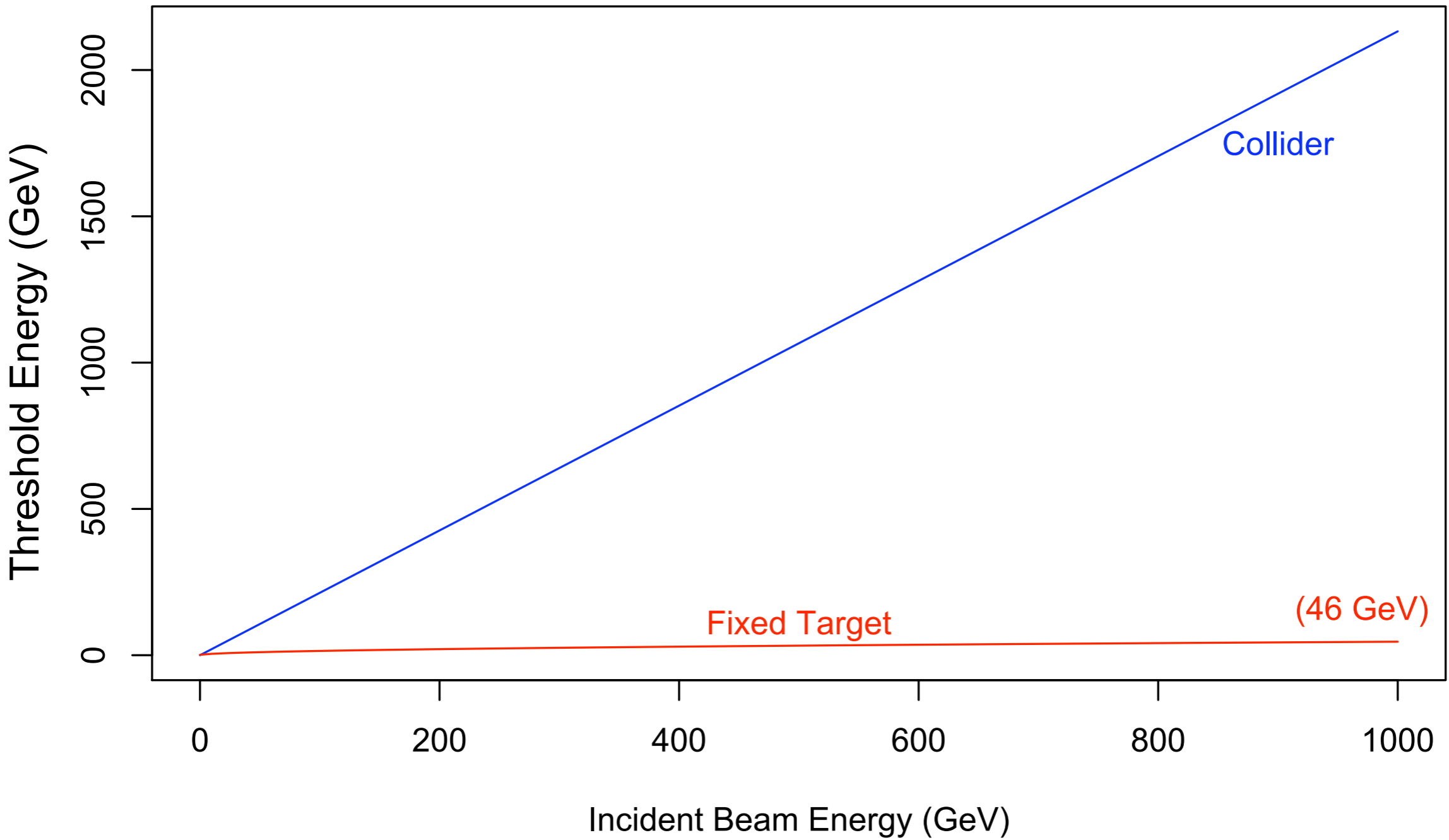
$$\begin{aligned}
 m^*c^2 &= 2E \\
 &= 2E_0\gamma_{coll}
 \end{aligned}$$





# Fixed Target Energy vs. Collider Energy

## Nucleon-Nucleon Collisions





# Fixed Target Energy vs. Collider Energy

- Beam/target particles:

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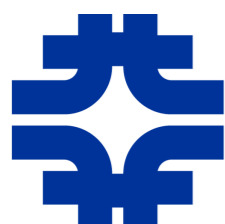
Fixed Target

Collider



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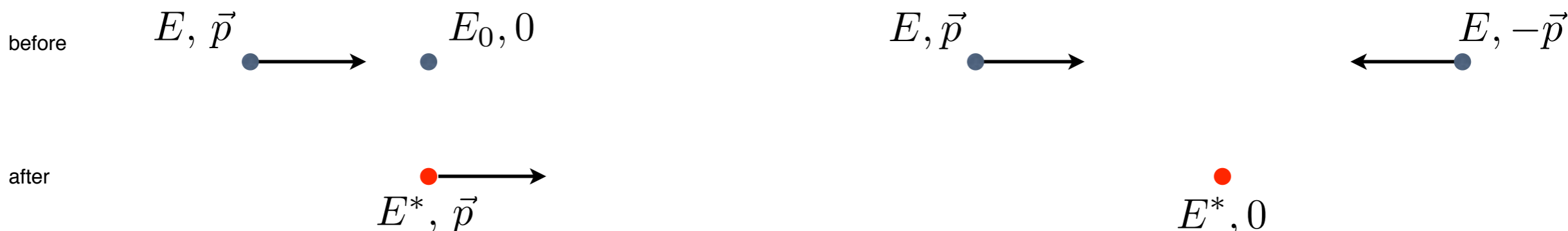
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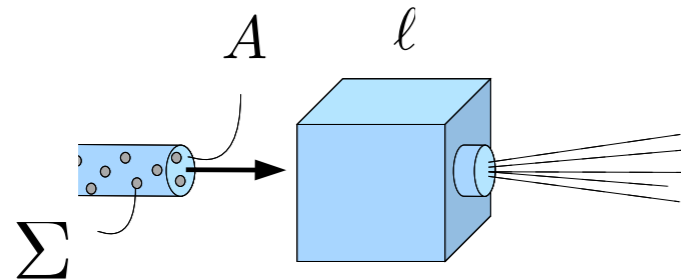
100,000 TeV FT synch. == 14 TeV LHC



# Luminosity

- Experiments want “collisions/events” -- rate?

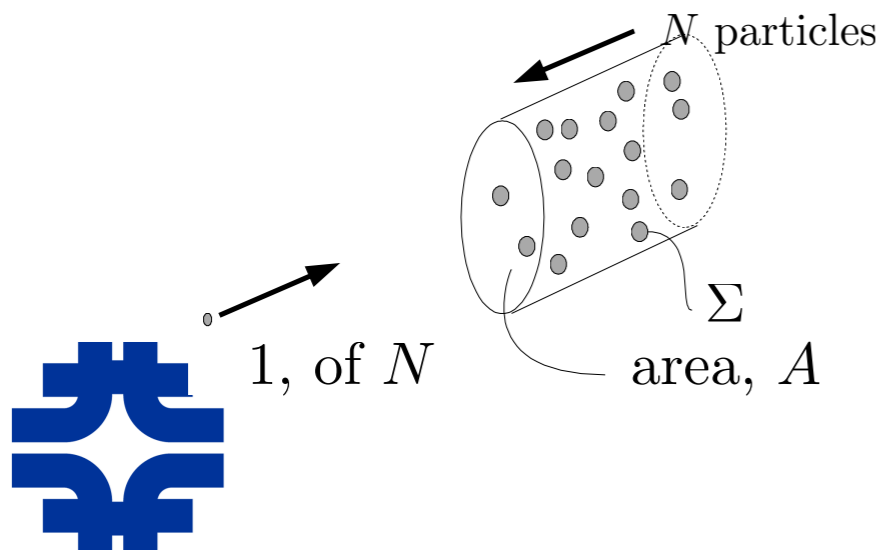
- Fixed Target Experiment:



$$\begin{aligned} \mathcal{R} &= \left( \frac{\Sigma}{A} \right) \cdot \rho \cdot A \cdot l \cdot N_A \cdot \dot{N}_{beam} \\ &= \rho N_A l \dot{N}_{beam} \cdot \Sigma \\ &\equiv \mathcal{L} \cdot \Sigma \end{aligned}$$

*ex.:*  $\mathcal{L} = \rho N_A l \dot{N}_{beam} = 10^{24} / \text{cm}^3 \cdot 100 \text{ cm} \cdot 10^{13} / \text{sec} = 10^{39} \text{ cm}^{-2} \text{ sec}^{-1}$

- Bunched-Beam Collider:



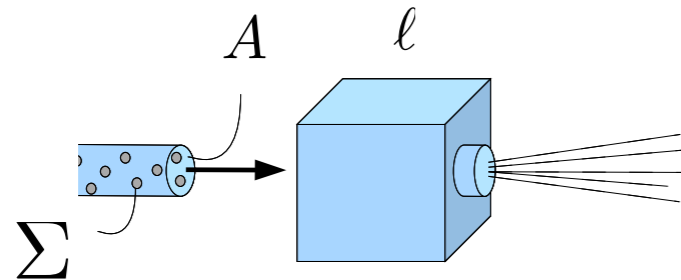
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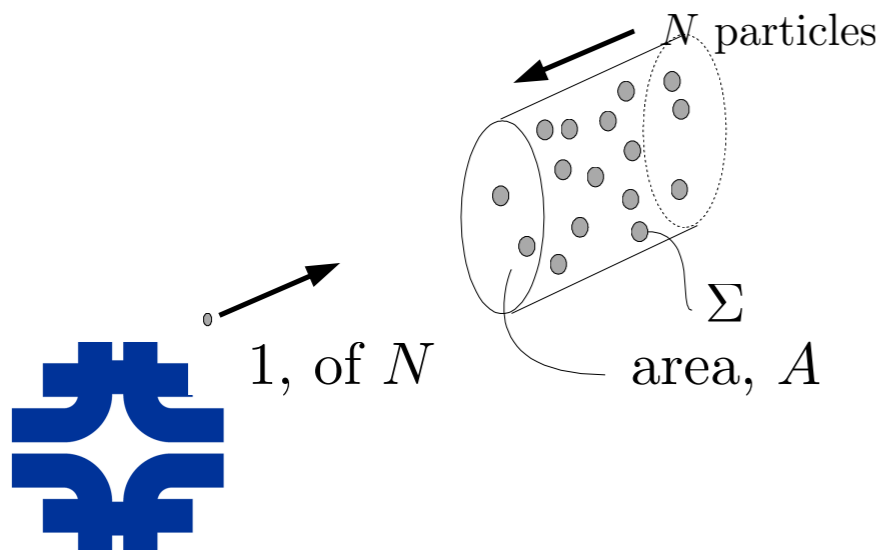
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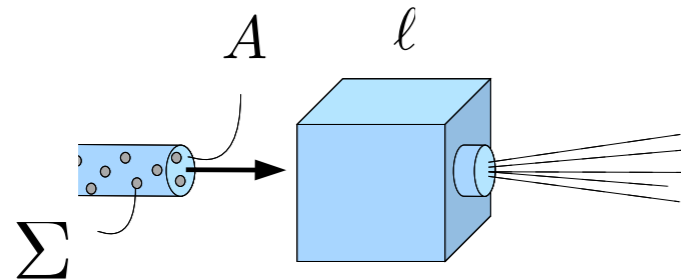


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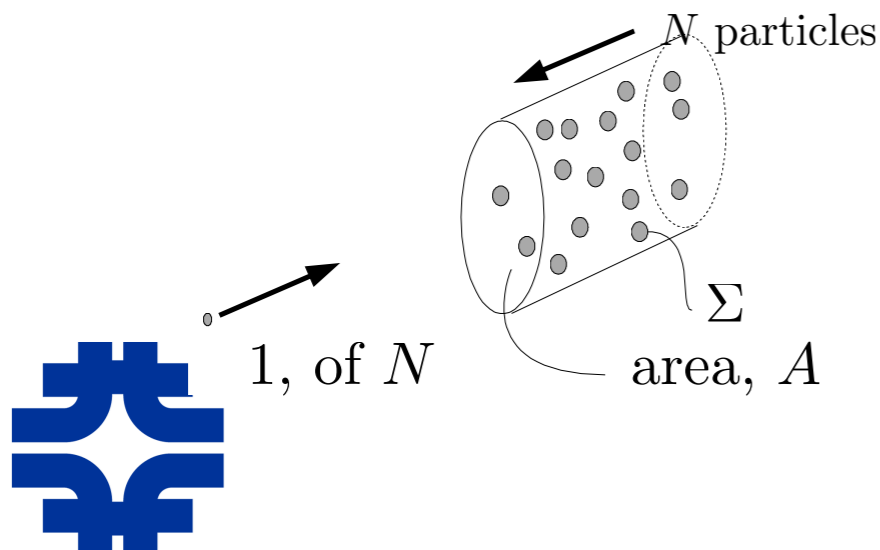
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$(10^{34} \text{ cm}^{-2} \text{ sec}^{-1} \text{ for LHC})$

# Integrated Luminosity

- Bunched beam is natural in collider that “accelerates” (more later)

$$\mathcal{L} = \frac{f_0 B N^2}{A}$$

$f_0$  = rev. frequency  
 $B$  = no. bunches

- In ideal case, particles are “lost” only due to “collisions”:

$$B \dot{N} = -\mathcal{L} \Sigma n$$

( $n$  = no. of detectors  
receiving luminosity  $\mathcal{L}$ )

- So, in this ideal case,

$$\mathcal{L}(t) = \frac{\mathcal{L}_0}{\left[1 + \left(\frac{n \mathcal{L}_0 \Sigma}{B N_0}\right) t\right]^2}$$

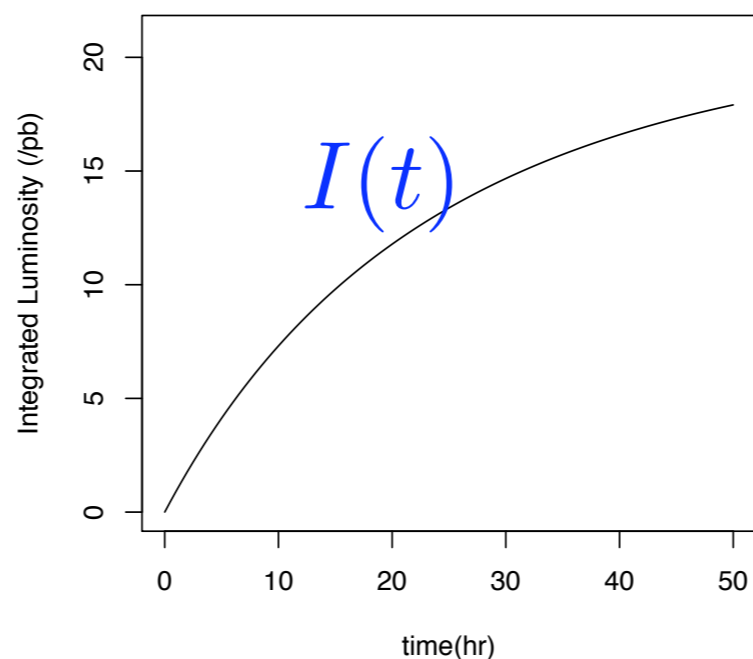
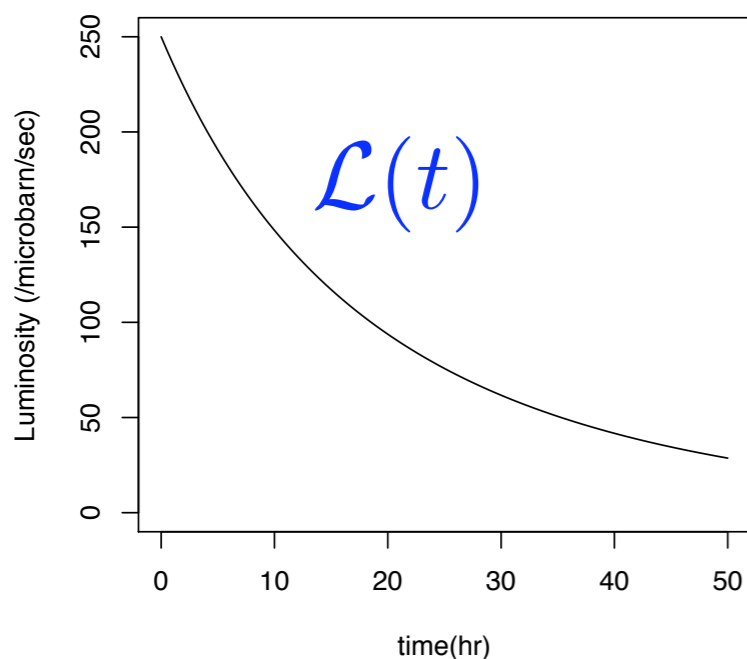




# Ultimate Number of Collisions

- Since  $\mathcal{R} = \mathcal{L} \cdot \Sigma$  then, #events =  $\int \mathcal{L}(t) dt \cdot \Sigma$
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$$I(T) \equiv \int_0^T \mathcal{L}(t) dt = \frac{\mathcal{L}_0 T}{1 + \mathcal{L}_0 T (n\Sigma / BN_0)} = I_0 \cdot \frac{\mathcal{L}_0 T / I_0}{1 + \mathcal{L}_0 T / I_0}$$



asymptotic limit:

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so, ...

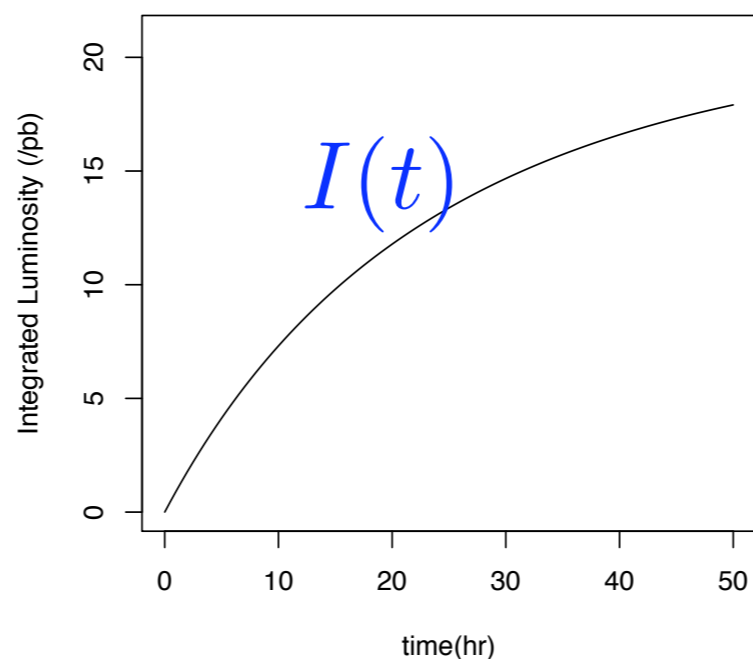
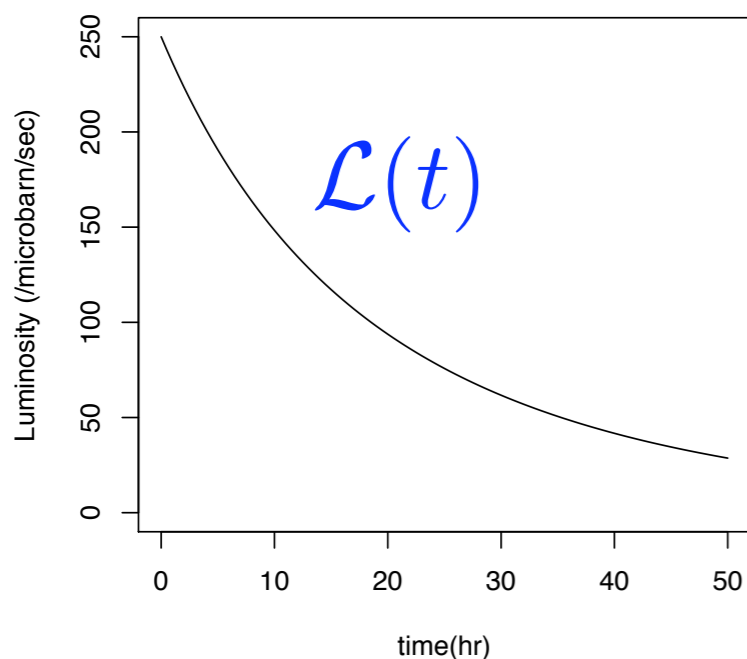
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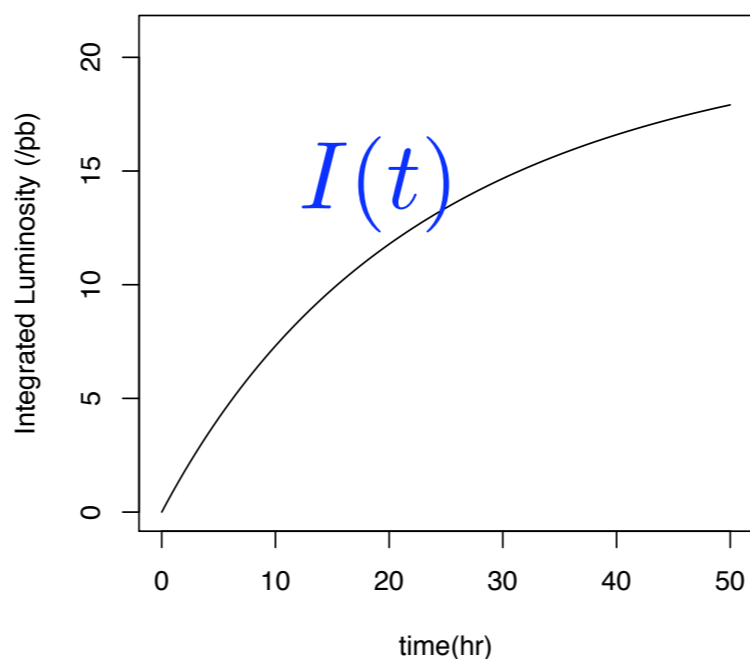
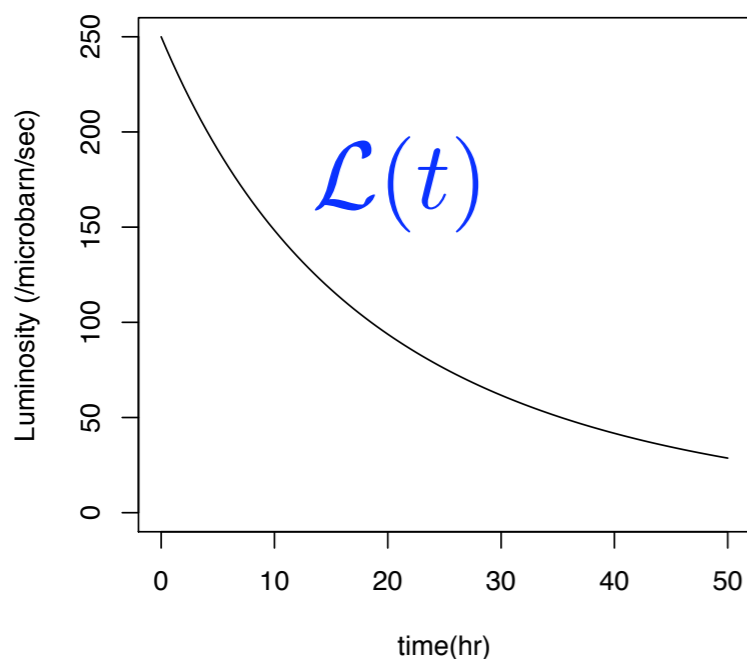
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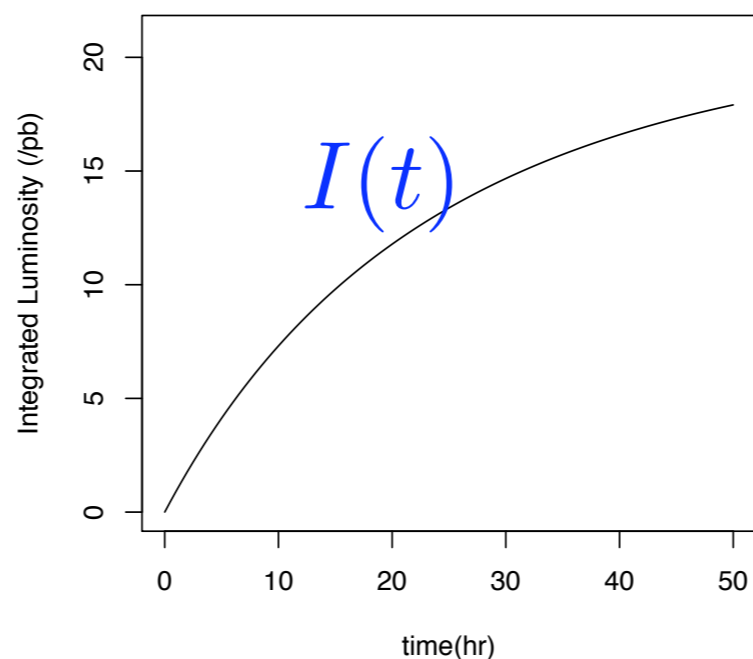
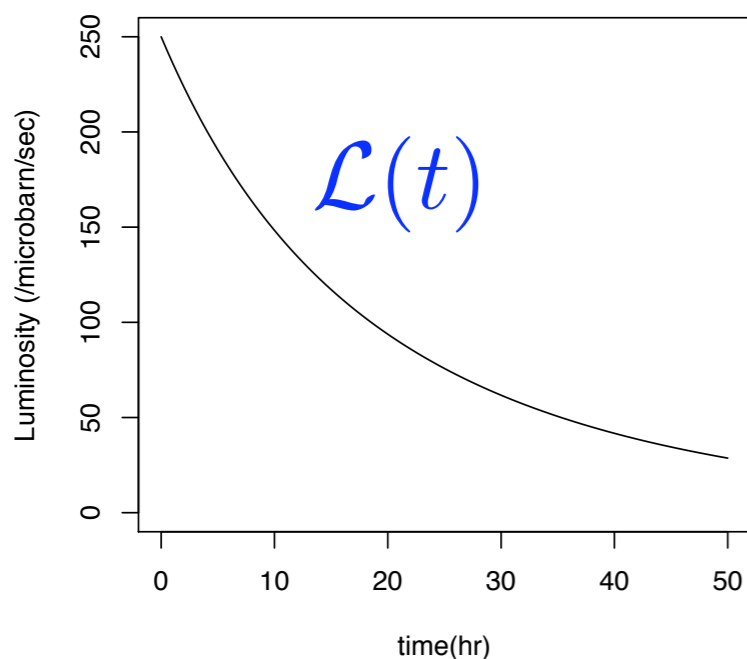




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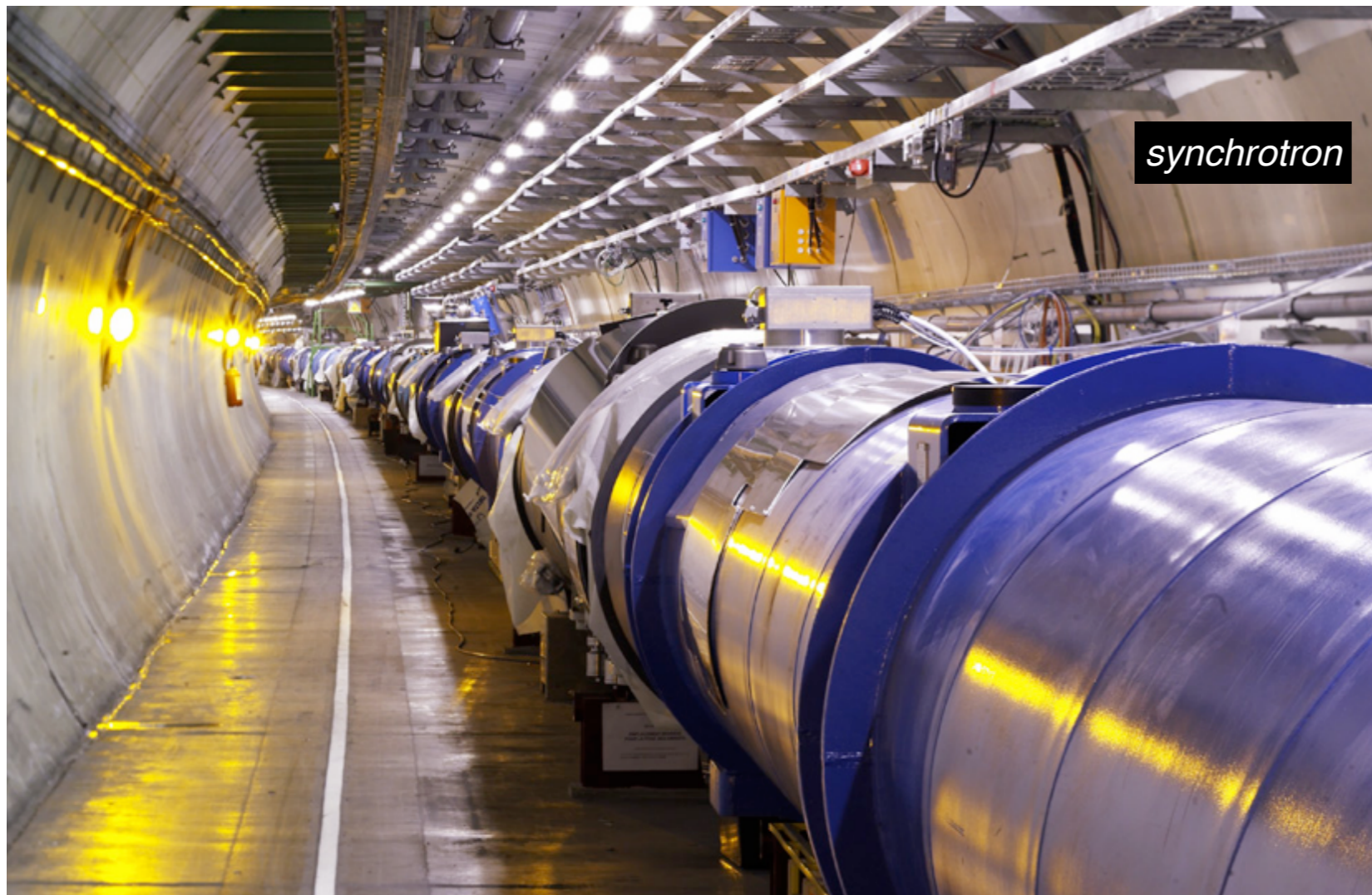
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↓ ↓  
↑



# Recent Large-Scale Accelerators

## Large Hadron Collider (LHC)



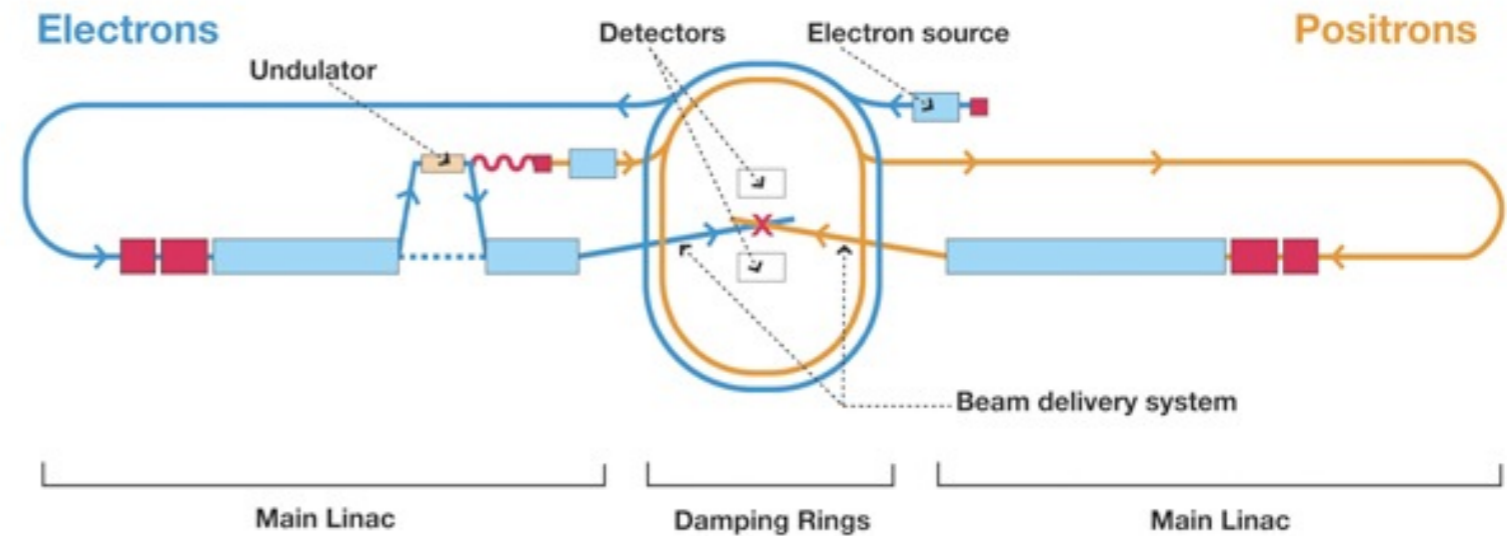
## Spallation Neutron Source (SNS)





# The Linac -- Again

- Linacs for  $e^{\pm}$ 
  - ILC, CLIC
  - avoid synchrotron radiation
  - damping rings produce very small beams at interaction points

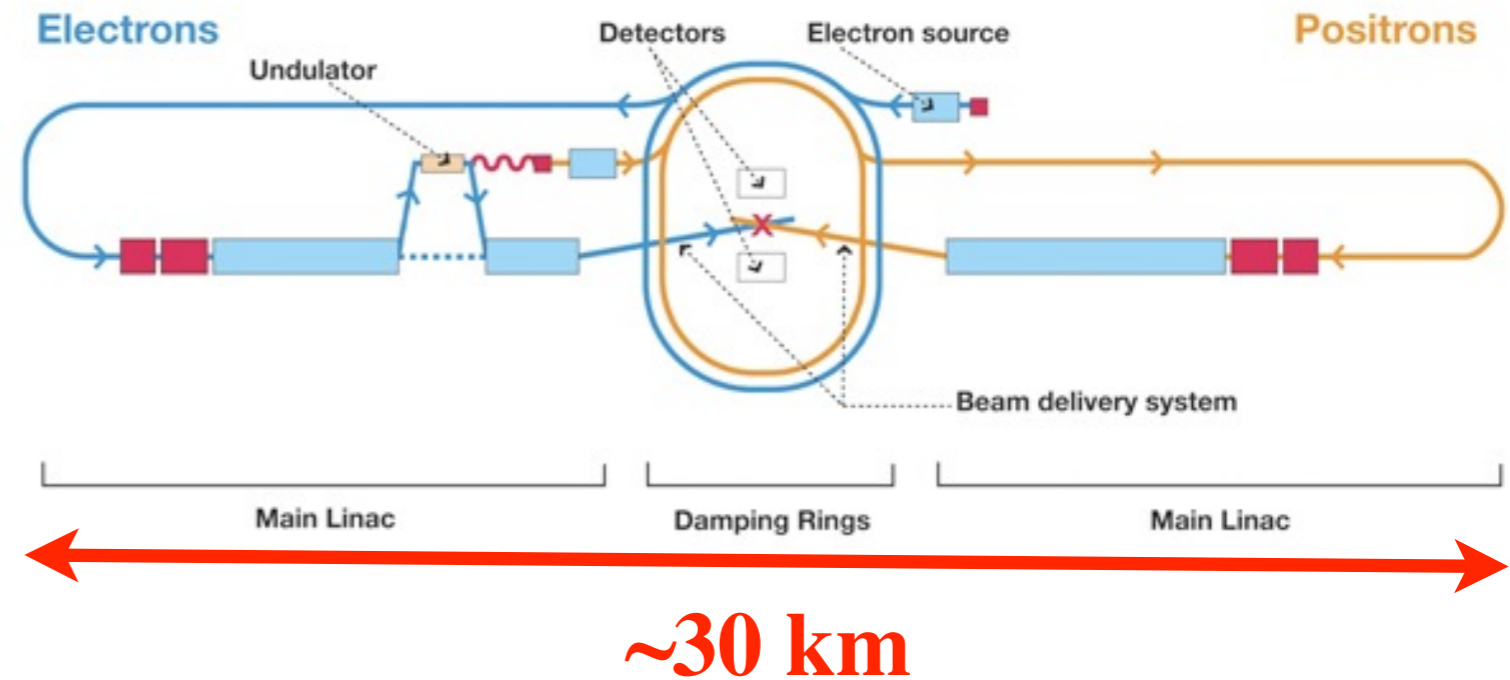


- Resurgent use of Linacs for large  $p$ ,  $N$  accelerators...
  - SNS; FRIB, ESS, neutrino sources
  - high current/intensity/power for use in high rate/statistical experiments
- For flexible program at FRIB --> Superconducting CW Linac
  - very unique features -- low velocities, large range of particle species, high current via multiple charge state acceleration, challenging charge stripping,...



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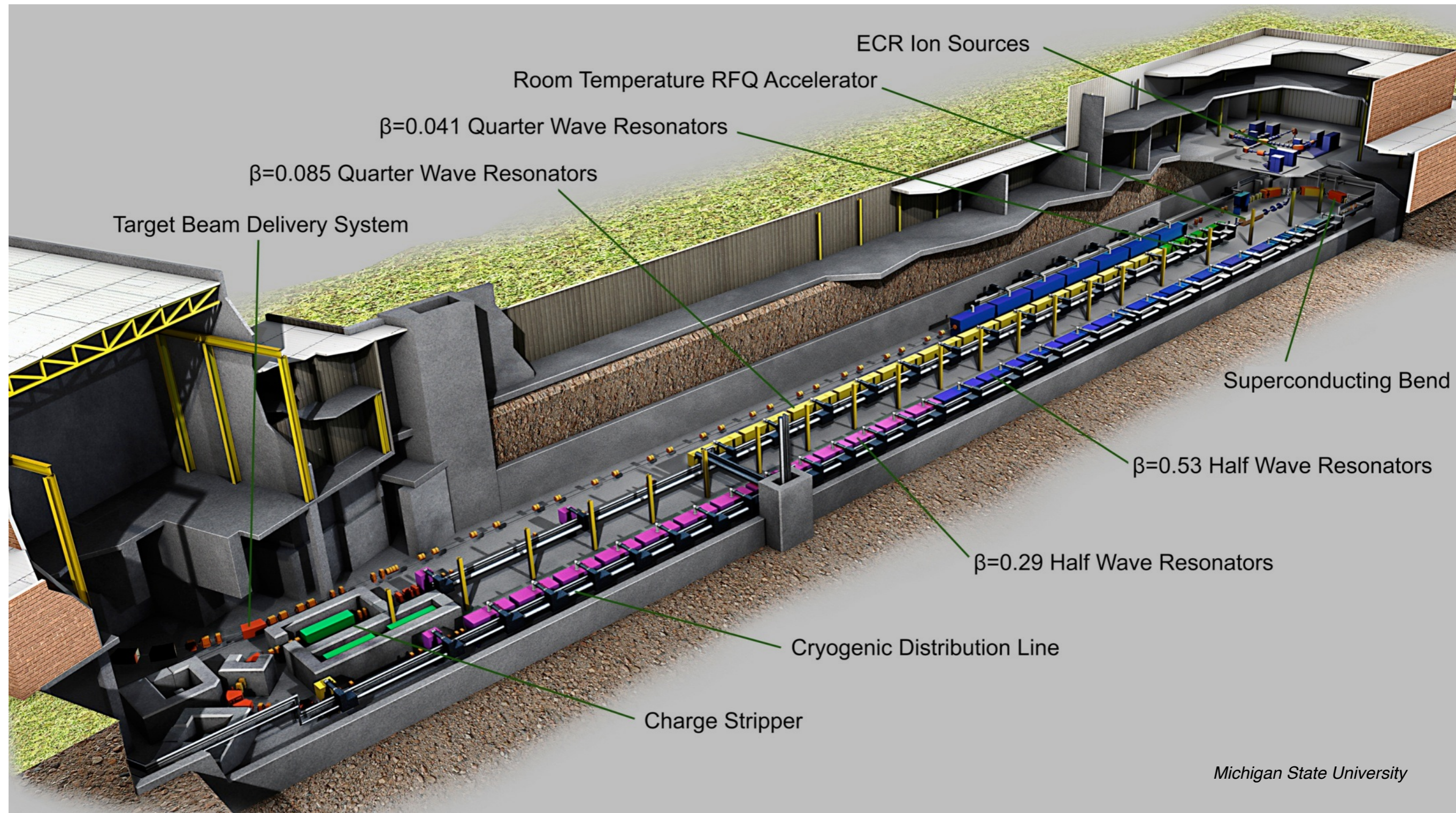




# Facility for Rare Isotope Beams (FRIB)



Northern Illinois University



Michigan State University

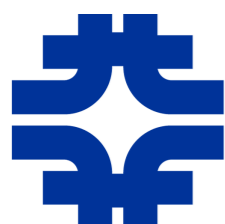




# Light Sources

“Brilliance” is the figure of merit  
Very similar to luminosity:

$$\mathcal{B} = \frac{\text{photons/sec}}{\text{mm}^2 \text{mrad}^2 (0.1\% \text{ BW})}$$



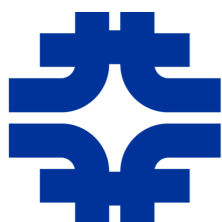




# But Wait, There's More!

- And, of course, not all applications are in high energy or nuclear physics!
- Basic energy sciences as well as industrial applications make up the bulk of our field, in terms of number of accelerators and arguably their direct impact on society
  - ~26,000 accelerators worldwide\*
  - ~1% are research machines with energies above 1 GeV; of the rest, about 44% are for radiotherapy, 41% for ion implantation, 9% for industrial processing and research, and 4% for biomedical and other low-energy research\*

\*Feder, T. (2010). "[Accelerator school travels university circuit](#)". *Physics Today* **63** (2): 20. [Bibcode 2010PhT...63b..20F](#). [doi:10.1063/1.3326981](#)



# Accelerators for America's Future



Northern Illinois University

- Symposium and workshop held in Washington, D.C., October 2009
- 100-page Report available



- 4 INTRODUCTION  
Accelerators for America's Future
- CHAPTER 1  
Accelerators for Energy and the Environment
- CHAPTER 2  
Accelerators for Medicine
- CHAPTER 3  
Accelerators for Industry
- CENTERFOLD  
Adventures in Accelerator Mass Spectrometry
- CHAPTER 4  
Accelerators for Security and Defense
- CHAPTER 5  
Accelerators for Discovery Science
- CHAPTER 6  
Accelerator Science and Education
- SUMMARY  
Technical, Program and Policy

Areas of R&D identified by each working group. All areas are of importance to each working group. Color coding indicates areas with greatest impact.

R&D Need	Energy & Environment	Medicine	Industry	Security & Defense	Discovery Science
Reliability	High	High	High	Medium	High
Beam Power/RF	High	Medium	High	High	High
Beam Transport and Control	Medium	High	Medium	High	Medium
Efficiency	High	Medium	High	High	High
Gradient (SRF and other)	Medium	High	High	High	High
Reduced Production Costs	High	High	High	Medium	High
Simulation	High	High	Medium	High	Medium
Lasers	High	Medium	Medium	High	High
Size	Medium	High	High	Medium	High
Superconducting Magnets	Medium	High	High	High	Medium
Targetry	High	High	Medium	Medium	Medium
Particle Sources	Medium	Medium	High	Medium	Medium

Color code: Increased priority (indicated by a vertical color scale from blue to red on the right side of the table).



<http://www.acceleratorsamerica.org/>