

# Review of Star Intro

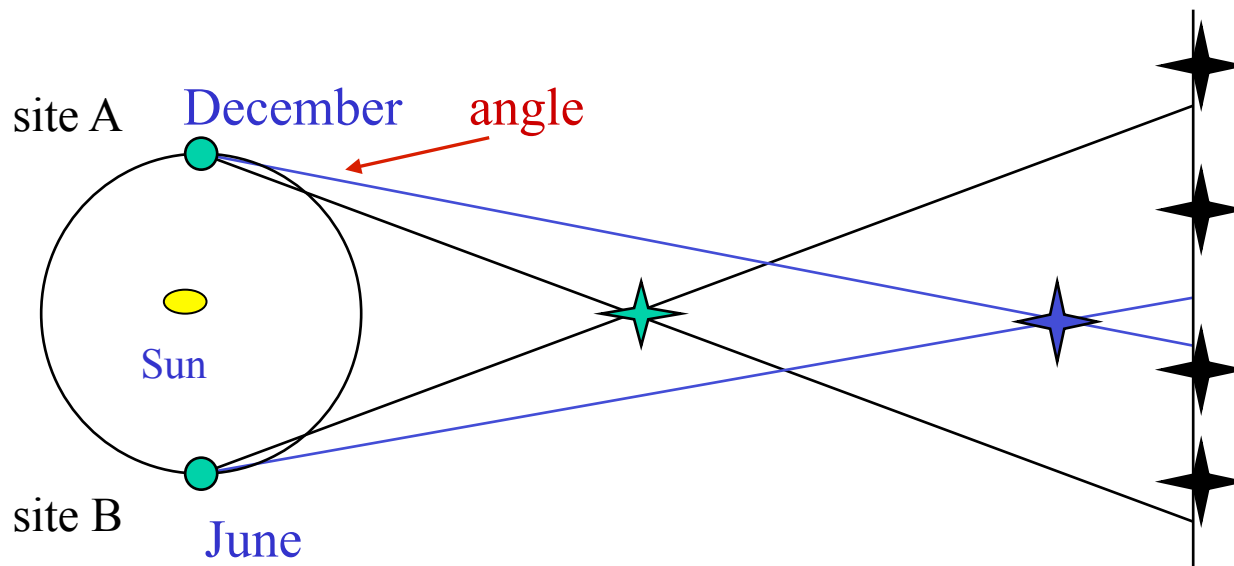
- Parallax - geometric method of determining star distance
- Absolute and apparent luminosity.
- Temperature
- Spectrum: What characterizes the star's surface
  - Is related to its **temperature**
  - Can use **spectral information** to determine **masses** of binary stars..
  - Can use spectral information to determine **absolute luminosity**, then use the **apparent luminosity** to determine **distance**

# Shifting Star Positions

- The orbit of the earth is used as the base.
- Near stars appear to move more than far stars
- Distance = (base length)/angle
- Define: 1 parsec = 1 AU/(angle of 1 second of arc) = 3.3 LY

$$1 \text{ sec arc} = 1 \text{ deg}/3600$$

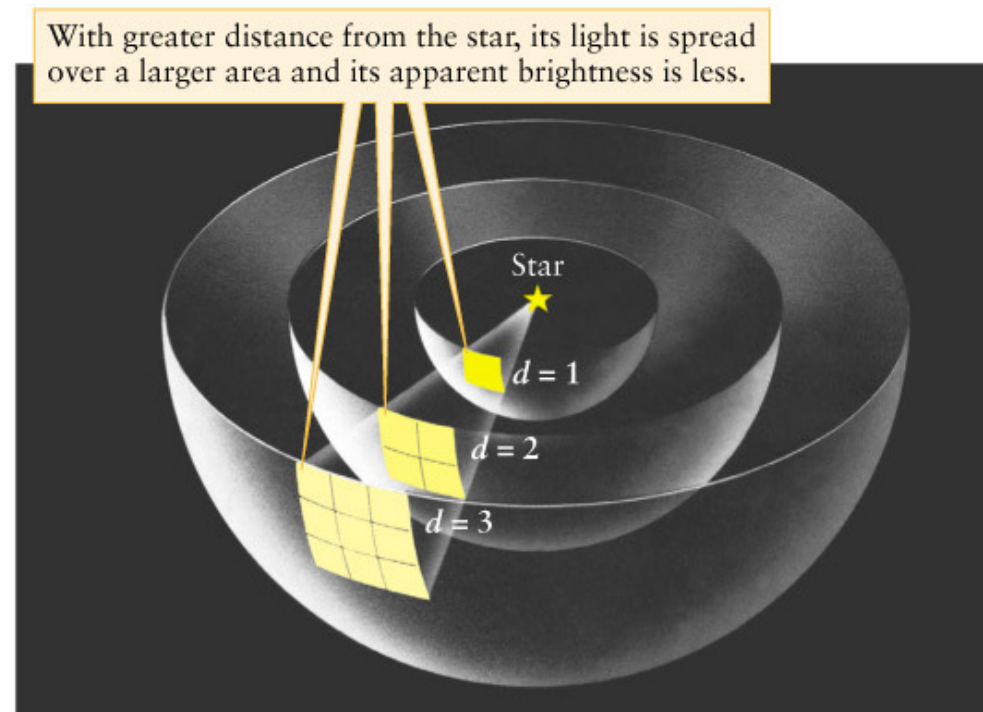
$$\text{PARallax of one arc SECond} = 1 \text{ rad}/206,265$$



# Absolute vs Apparent Brightness

Absolute Brightness/Luminosity means total energy output

Apparent Brightness is what is seen by eye or in a telescope and so depends on distance ( $1/\text{Distance}^2$ )



# Binary Star Systems

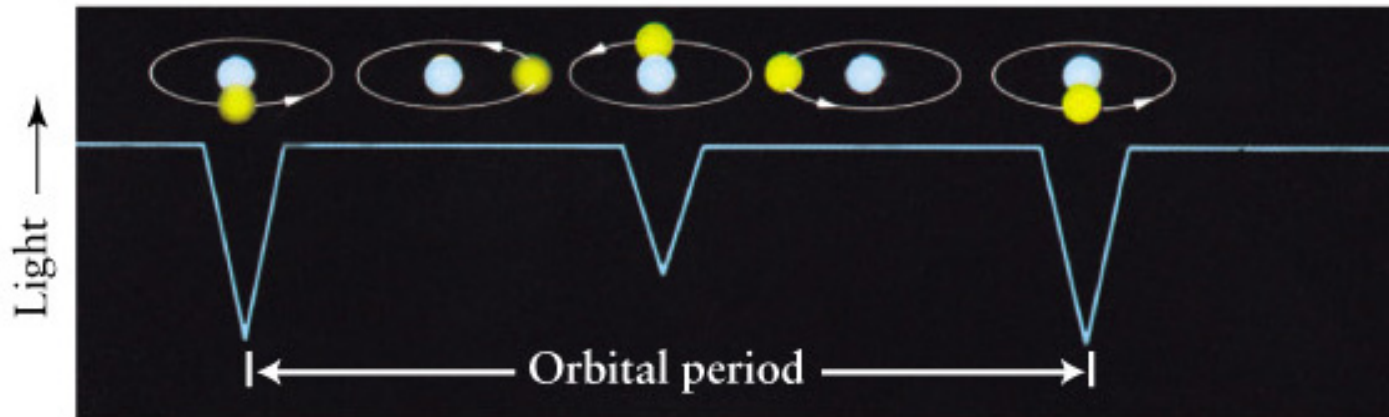
- Many stars come in groups of 2 or 3 that are close (few AU) to each other: BINARY Star Systems
- Gravitationally bound and probably formed at the same time
- SiriusA is 23 times as bright as our Sun  
SiriusB is 0.005 times as bright as the Sun  
Their separation varies from 8 to 31 AU



# Binary Stars → Stellar Masses

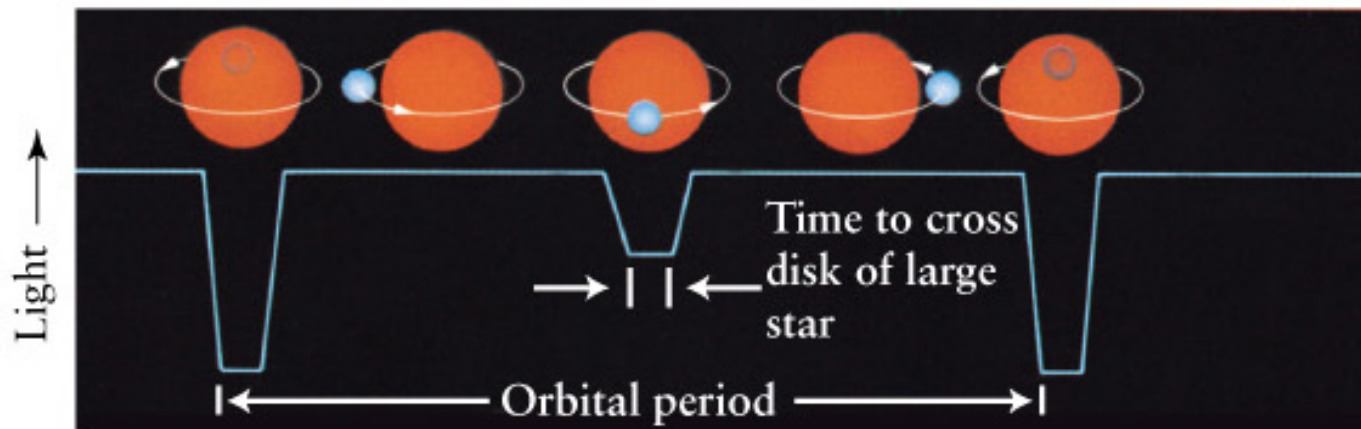
- Visual Binary: If can visually observe **both** stars
- Spectroscopic Binary: If one can only separate into 2 stars by looking at the spectrum (they eclipse each other plus will have different Doppler shifts)
- Measure the **orbital** information like **period** and **separation distance**. Get Mass through Kepler/Newtonian-like methods

# Binary Star Orbits - Eclipses



a Partial eclipse

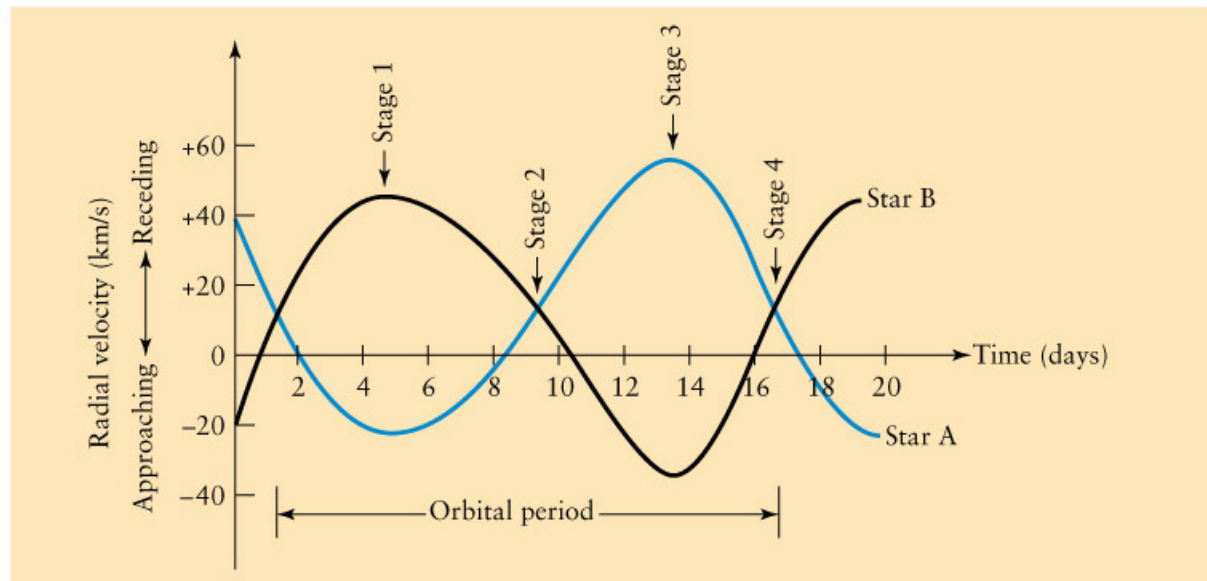
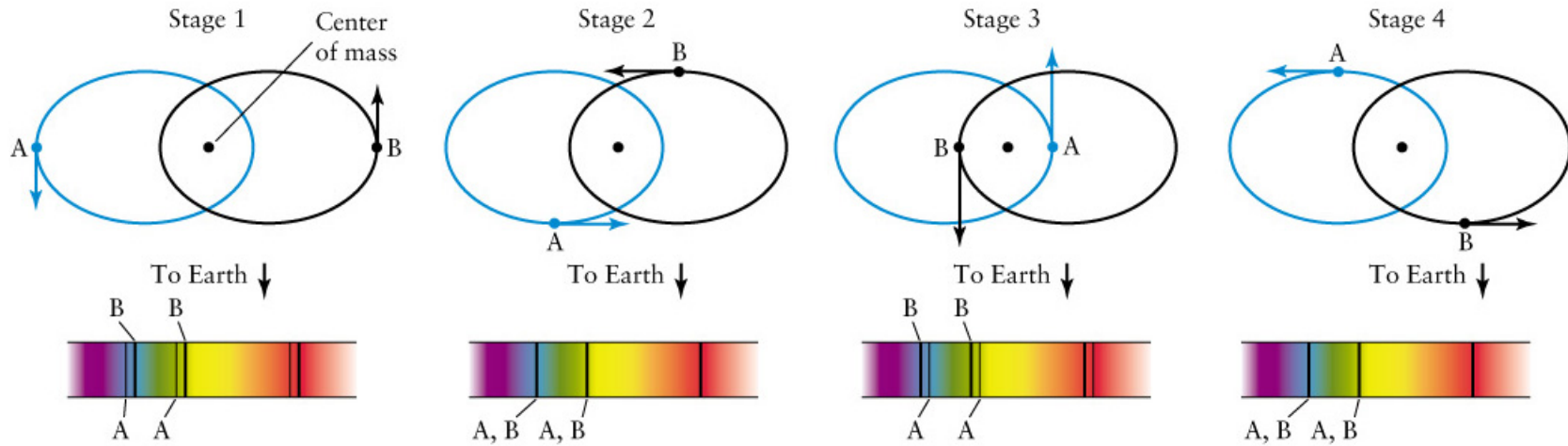
Time →



b Total eclipse

Time →

# Binary Star Orbits – Doppler Shifts

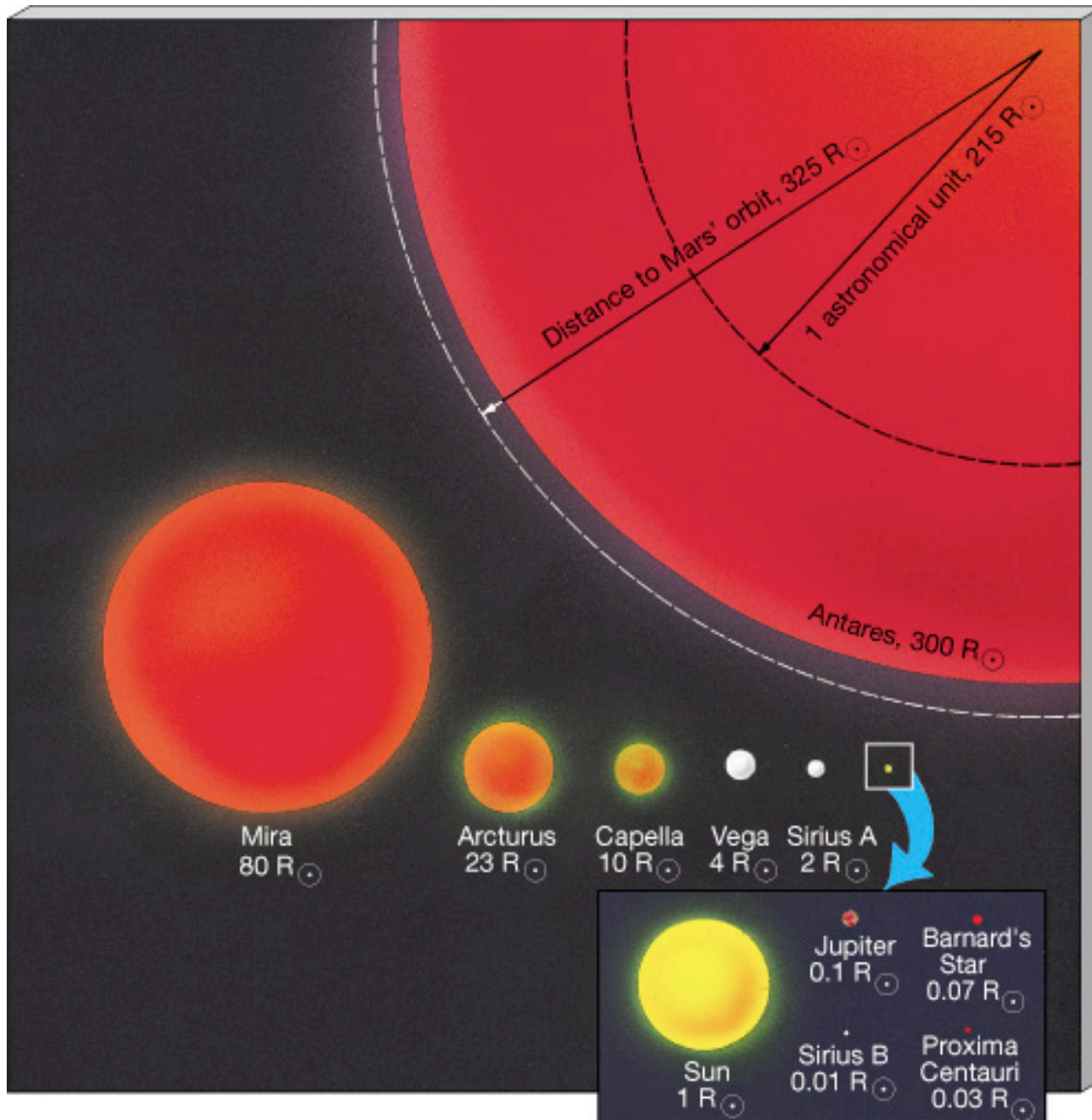


# Stellar Sizes

- For a few close, big stars, they can be seen in a telescope as non-point objects
- Measure **angular size**; if one knows the distance, can get the **actual size** of star  
Example: Betelgeuse 300 times larger radius than the Sun
- If further away but a **binary star**, then can get size of stars when they eclipse each other → length of time one star passes in front or behind each other



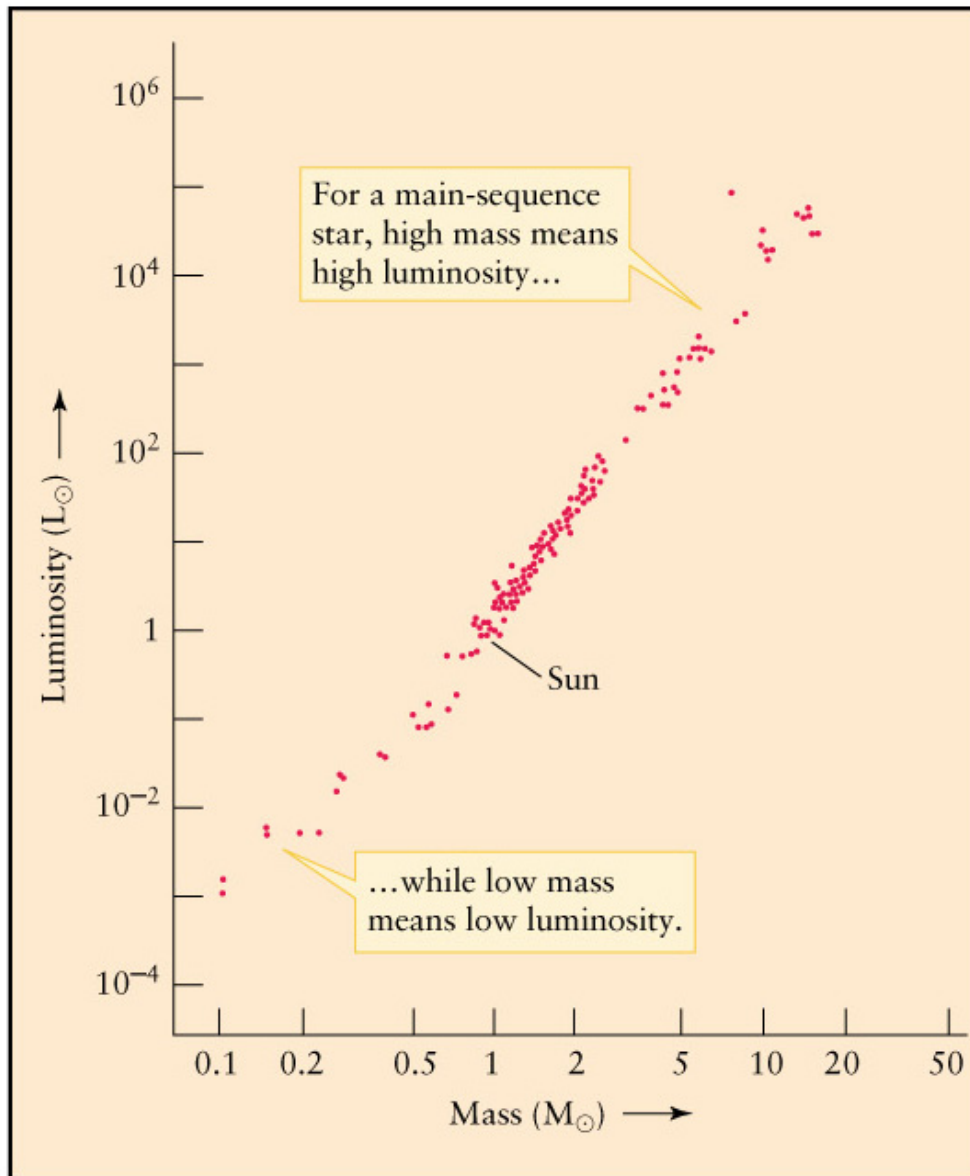
# Stellar Sizes



# Mass vs Luminosity

always on these plots it is the Absolute Luminosity of the star

High mass → High brightness



# Surface Temperature of Stars

- Continuous spectrum and the **peak wavelength** tells temperature

$$\lambda(\text{max}) = \text{constant}/\text{Temp}$$

where  $\lambda = \text{wavelength}$

- OR measure relative intensity at a few wavelengths like

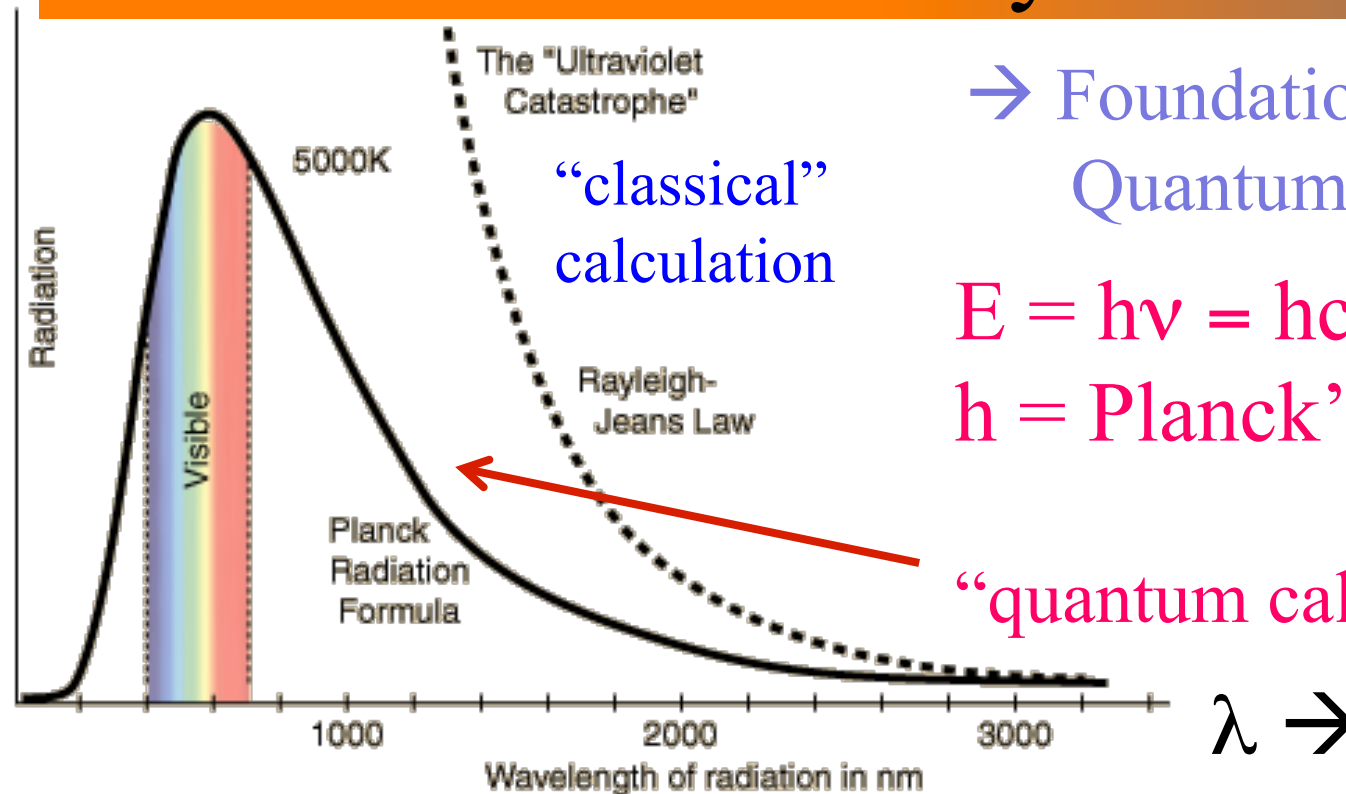
RED

GREEN

BLUE

→ Easy to do

# More on “Blackbody” Radiation



→ Foundation of modern Quantum theory

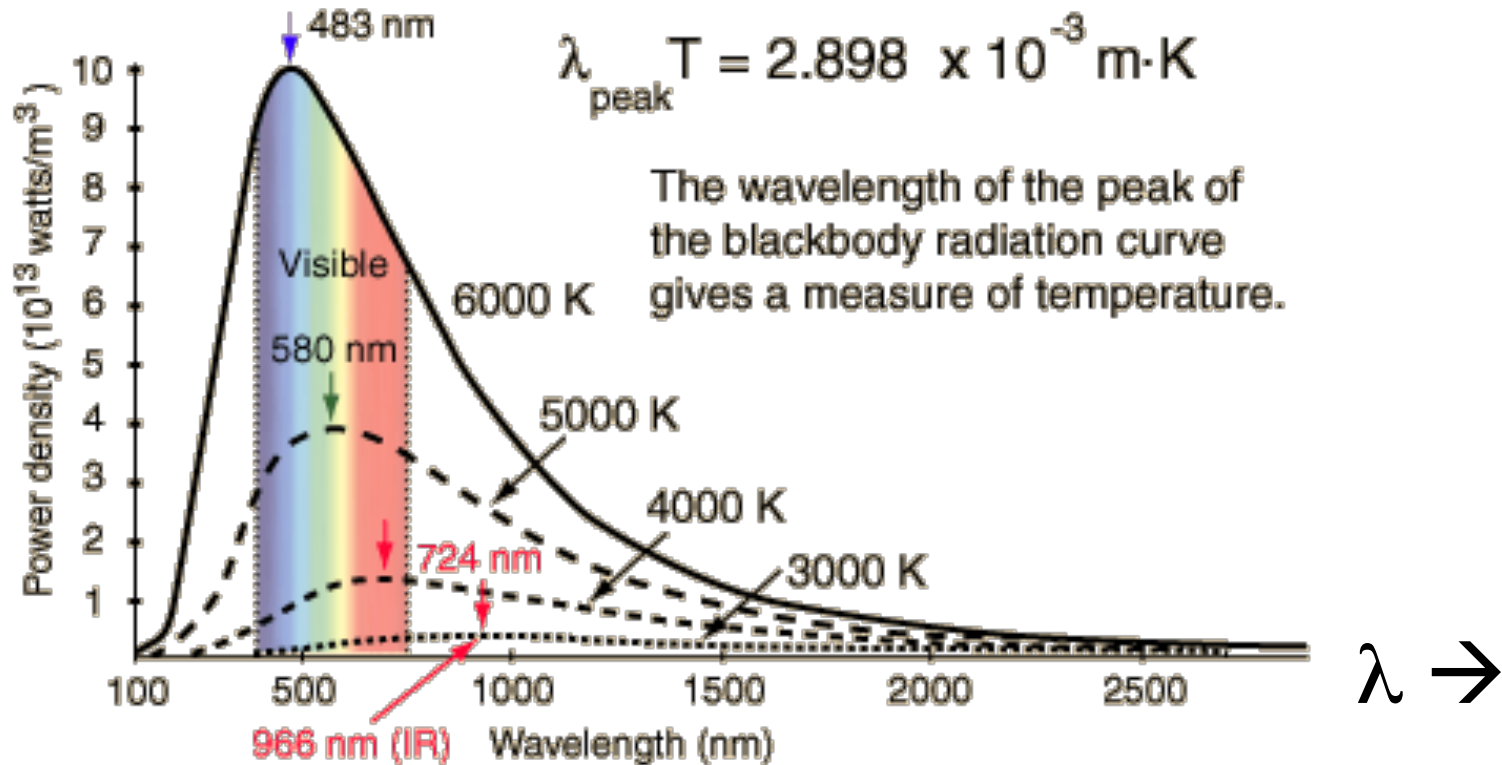
$$E = h\nu = hc/\lambda$$

$h$  = Planck's constant

“quantum calculation”

In order to explain the frequency distribution of radiation from a hot cavity, Planck proposed the **ad hoc** assumption that the radiant energy could exist only in **discrete quanta** which were proportional to the frequency. In which case, higher modes would be less populated and avoid the “ultraviolet catastrophe”.

# Wien's Displacement Law

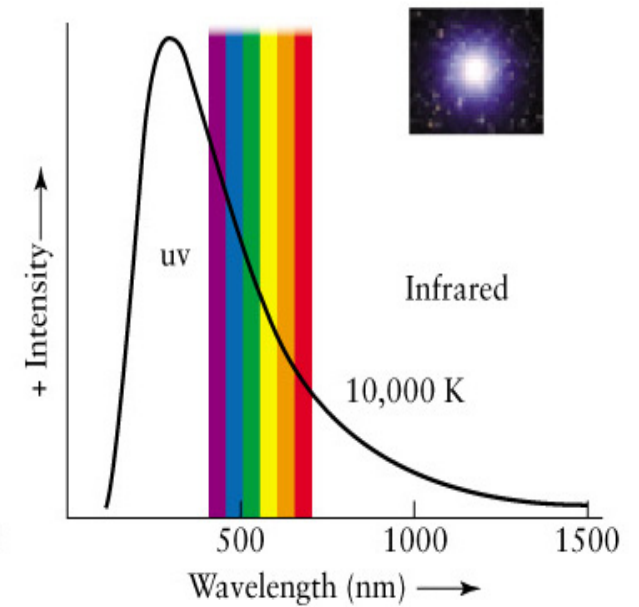
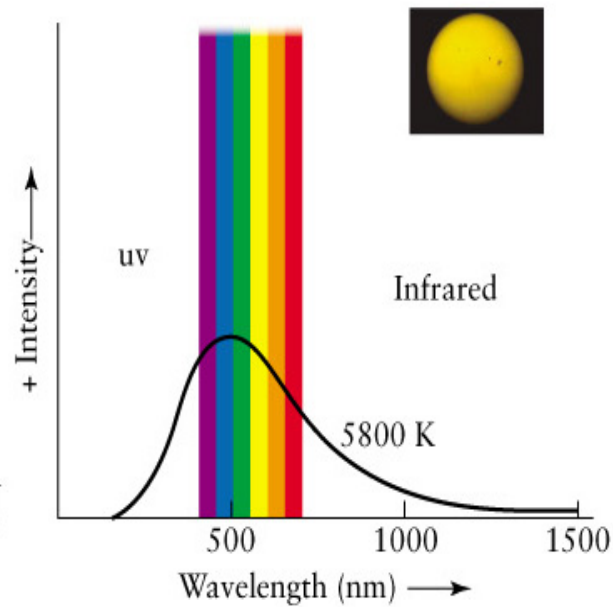
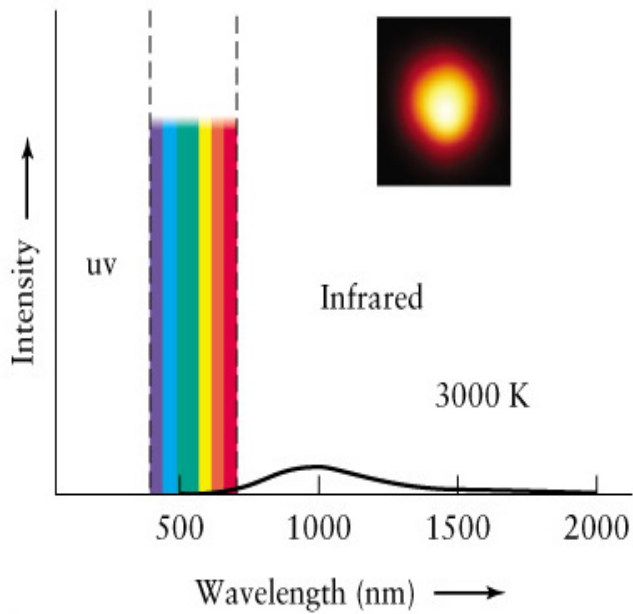


When the temperature of a **blackbody radiator increases**, the overall **radiated energy increases** and the **peak** of the radiation curve moves to **shorter** wavelengths.

The product of the **peak wavelength** and the **temperature** is found to be a constant.



HST image. “add” together images taken with different color filters

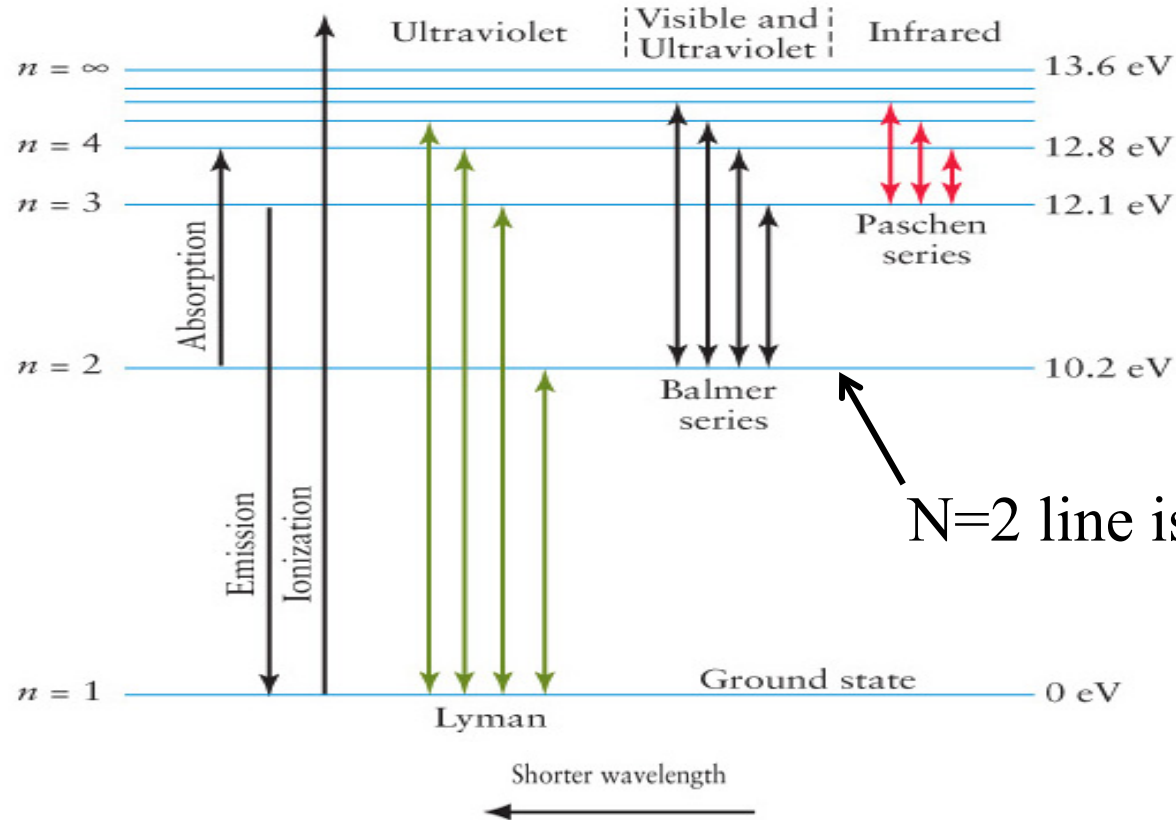


# Spectral Classes

Light passing through a star's atmosphere gives dark line **absorption** spectrum. Tells:

- What atoms are present
- Motion of the star by the Doppler shift of the absorption lines
- Temperature of the photosphere by **relative intensity** of different absorption lines and by amounts of different molecules and ions

# Quantum Mechanical Model of H Atom

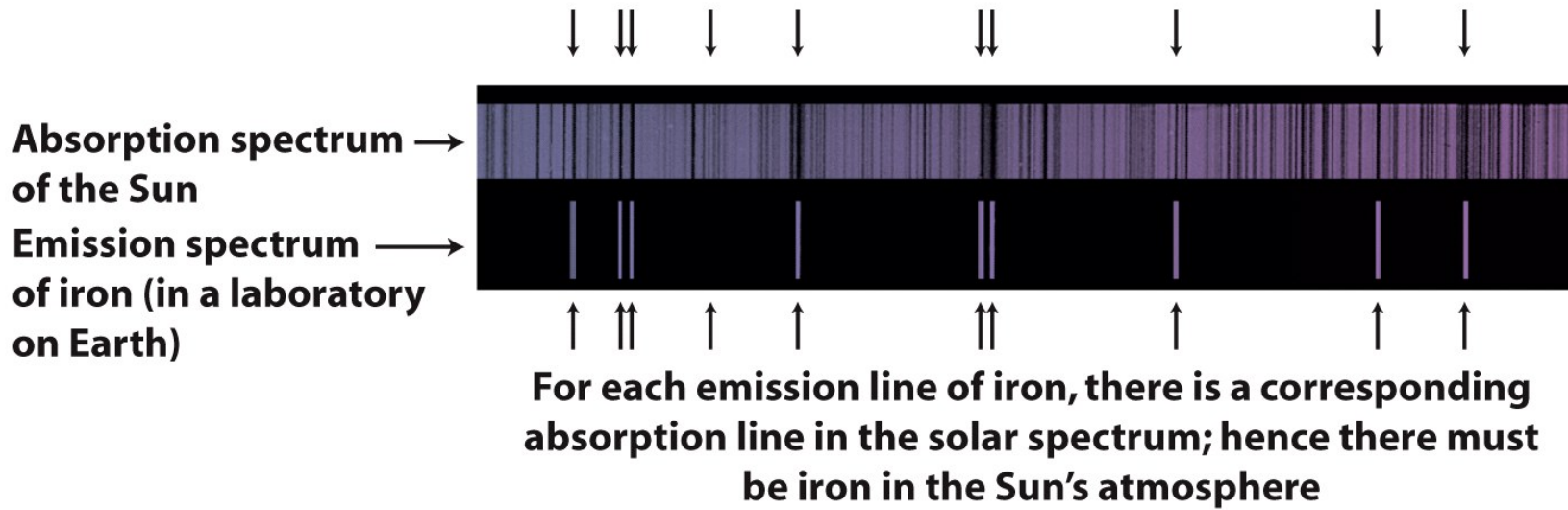


## Balmer Lines in the Spectrum of a Star

This portion of the spectrum of the star Vega shows eight Balmer lines, from  $H_\alpha$  at 656.3 nm through  $H_\theta$  at 388.9 nm.



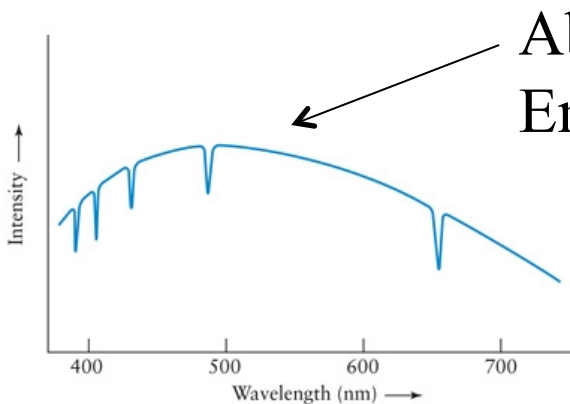
# Spectrum of Sun



a

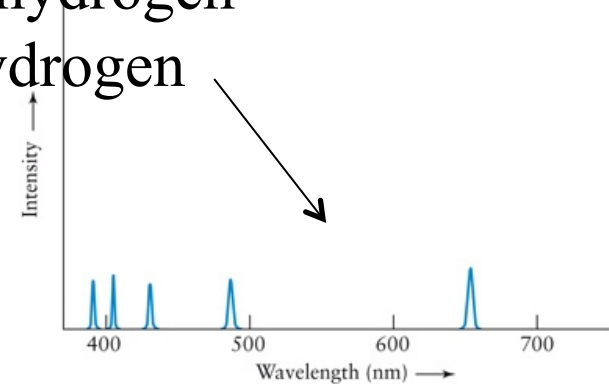


c



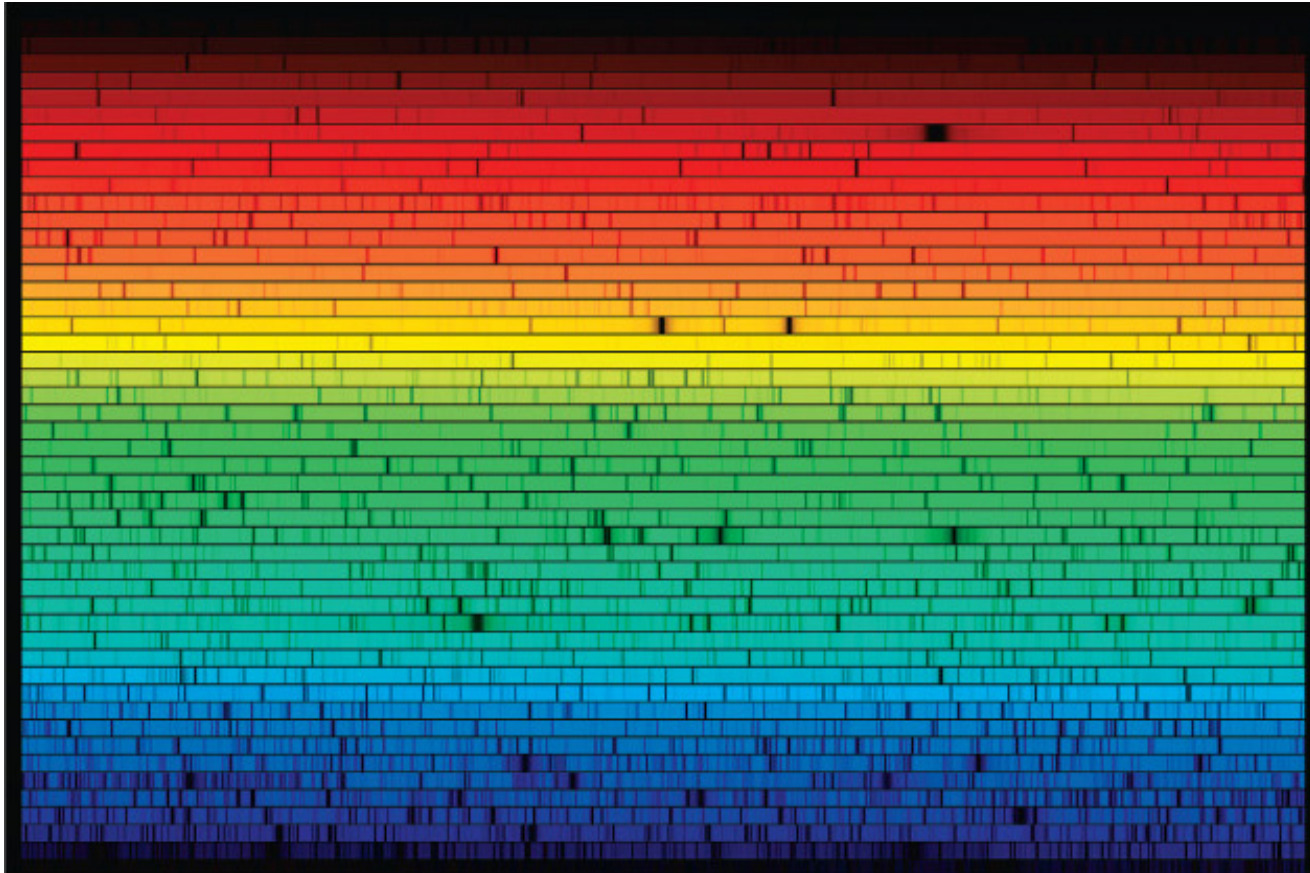
b

Absorption spectrum of hydrogen  
Emission spectrum of hydrogen



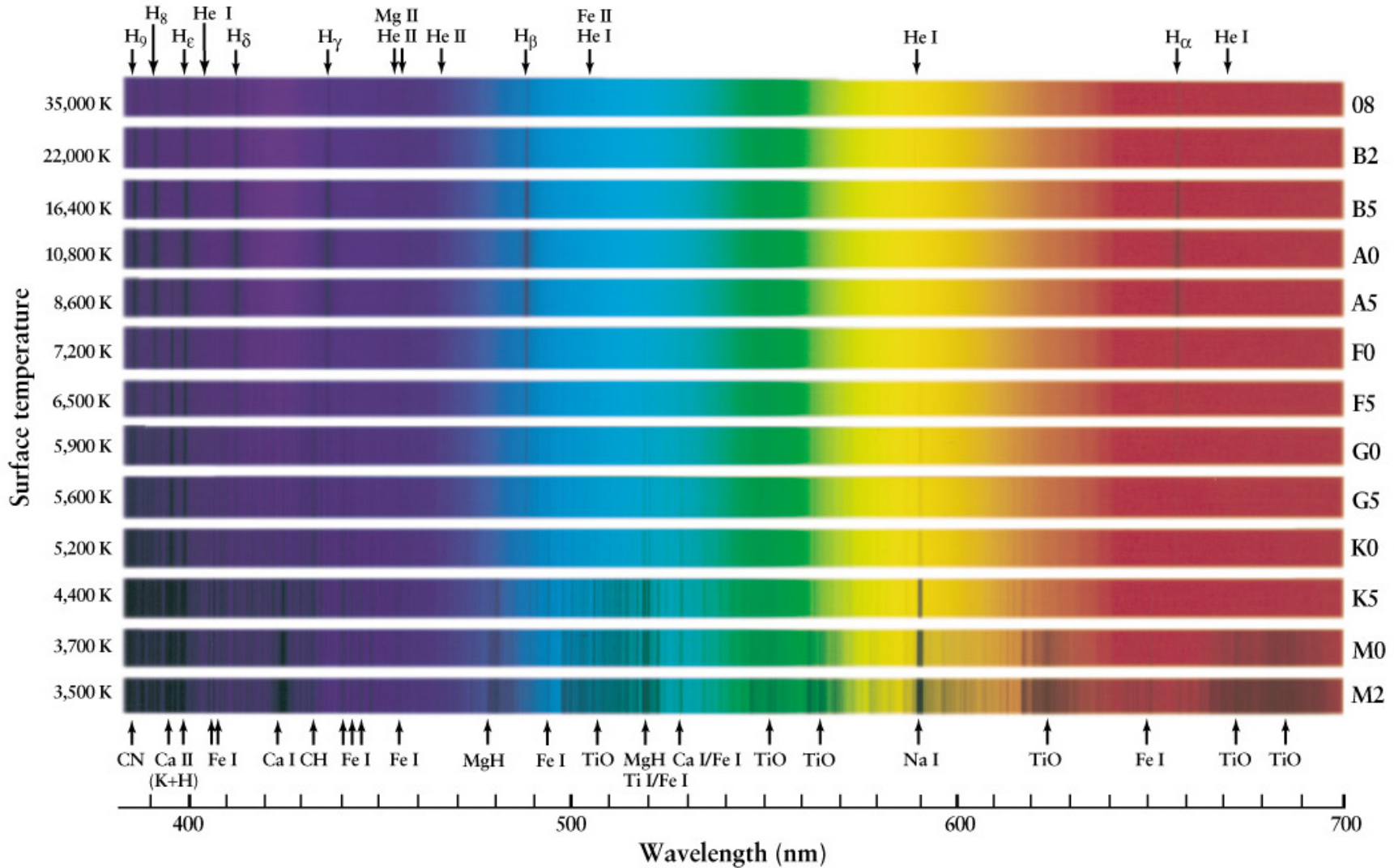
d

# Spectrum of Sun



The combination of lines from the solar spectrum allows us to determine which chemicals are present and in what abundance...

# Spectral Classes



→ Energy is enough to be “excited”, but not ionized ←

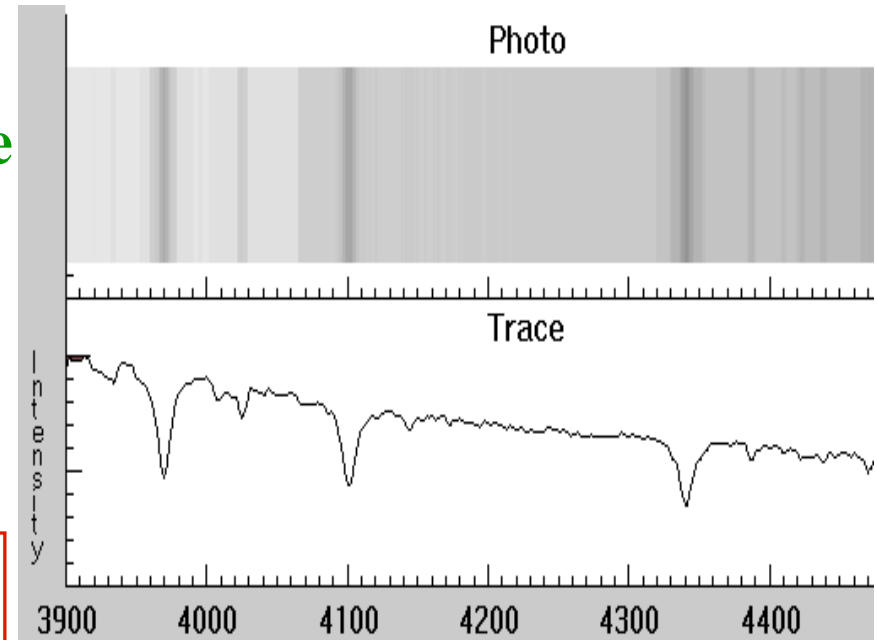
# Stellar Spectroscopy

Spectral classes **originally** ordered A,B,G,M... based on the amount of hydrogen, helium, ionized calcium and metals. absorption in the visible range...

- Now order by **surface temperature**
  - (Cecilia Payne applied Quantum Mechanics).

Spectral Class	Temperature
O oh	hottest
B be	
A a	
F fine	
G girl/guy	
K kiss	
M me	coolest

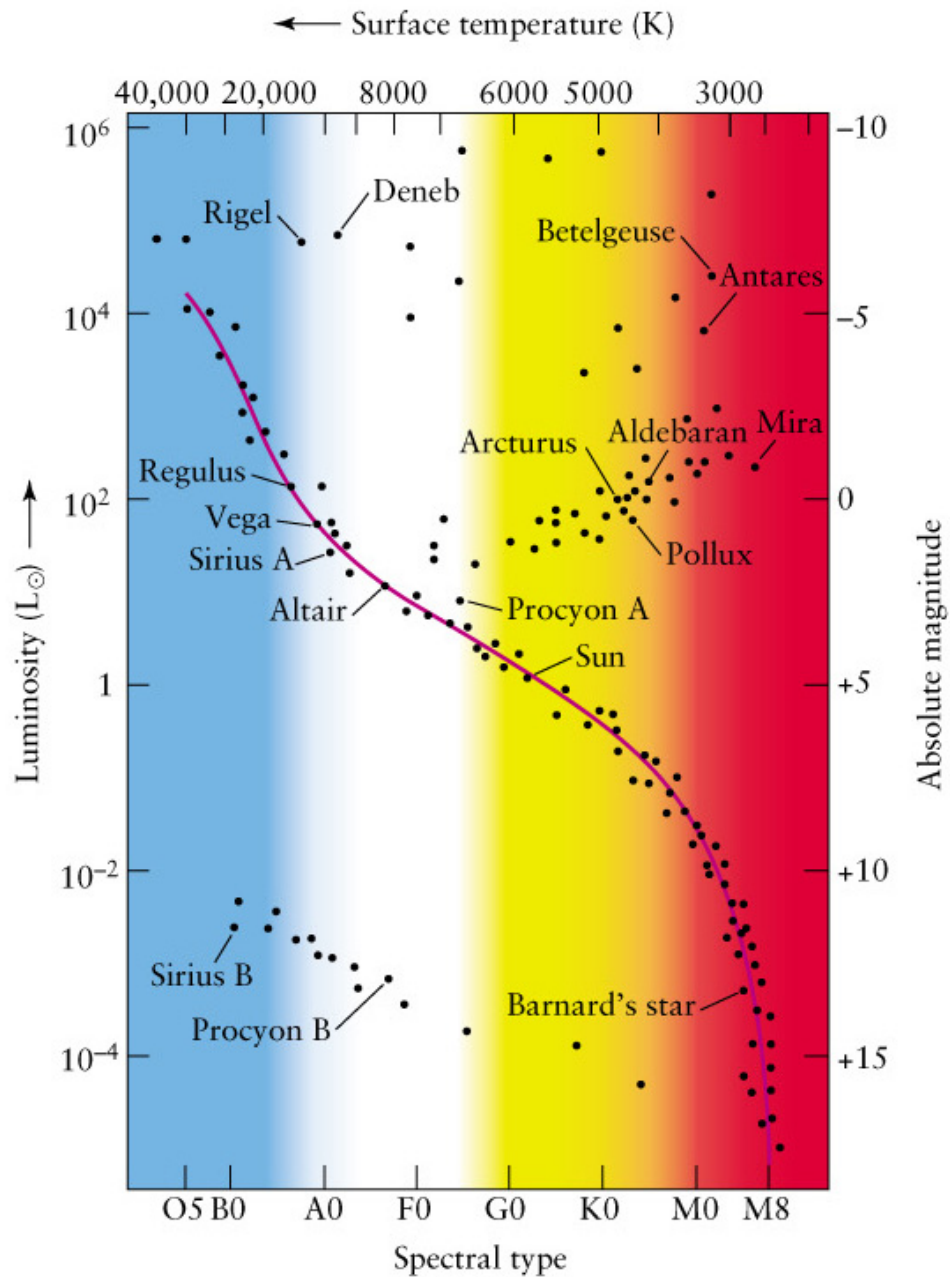
Don't need to know



**1910s: Annie Jump Cannon** and others working at Harvard developed an empirical scheme for classifying the spectra

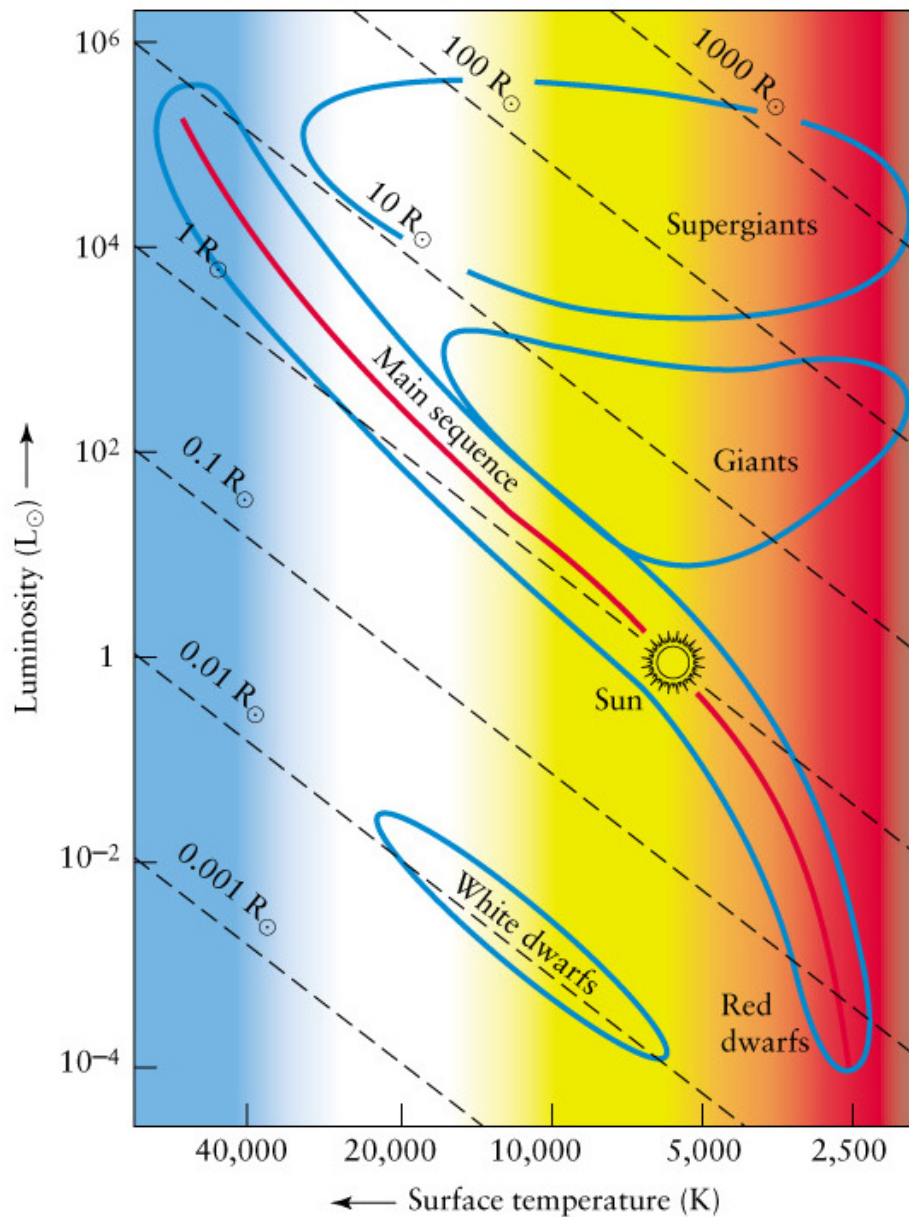
# Hertzprung-Russell Diagram

Plot Luminosity  
versus surface  
temperature



# Hertzprung-Russell Diagram

Stars with larger sizes are brighter than a smaller star with the same surface temperature

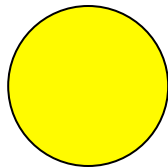


# Temperature vs Luminosity vs Radius of Stars

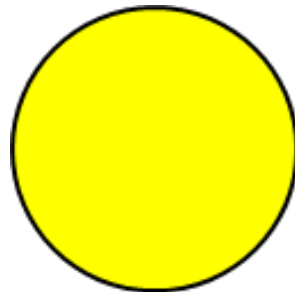
Energy emitted by surface of star due to EM radiation is

Energy/(surface area) =  $\sigma T^4$ . Examples:

- Two stars. Same temperature and radius  $\rightarrow$  same Luminosity
- Two stars. Same temperature. Radius(B) = 2xRadius(A).  
So surface area(B) = 4x surface area(A)  $\rightarrow$   
Luminosity(B) = 4xLum(A)



Radius = 1



Radius = 2

# Temperature vs Luminosity vs Radius of Stars

Energy emitted by surface of star due to EM radiation is

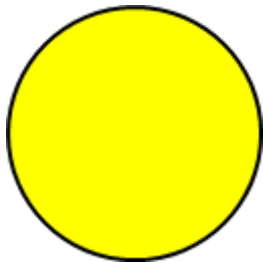
Energy/(surface area) =  $\sigma T^4$ . Examples:

- Two stars. Same radius. Temperature(B) = 2xTemp(A).

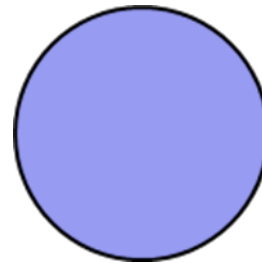
$$(\text{Energy/Area})_B = 2^4 \times (\text{Energy/Area})_A \quad \sim \text{ or } \sim$$

$$(\text{Energy/Area})_B = 16 \times (\text{Energy/Area})_A$$

$$\rightarrow \text{Luminosity(B)} = 16 \times \text{Lum(A)}$$



Temp = 6000



Temp = 12,000



# Hertzprung-Russell Diagram

- Most stars are on a “line” called the MAIN SEQUENCE with
  - hot surface temp  $\leftrightarrow$  large radius
  - medium temp  $\leftrightarrow$  medium radius
  - cool surface temp  $\leftrightarrow$  small radius
- There are also stars with cool surface temperature but very large radius: RED GIANTS
- Stars with hot surface temperature but very small radius: WHITE DWARVES

## Key Properties of Main Sequence Stars

Mass/ $M_{\text{Sun}}$	Luminosity/ $L_{\text{Sun}}$	Effective Temperature (K)	Radius/ $R_{\text{Sun}}$	Main sequence lifespan (yrs)
0.10	$3 \times 10^{-3}$	2,900	0.16	$2 \times 10^{12}$
0.50	0.03	3,800	0.6	$2 \times 10^{11}$
0.75	0.3	5,000	0.8	$3 \times 10^{10}$
1.0	1	6,000	1.0	$1 \times 10^{10}$
1.5	5	7,000	1.4	$2 \times 10^9$
3	60	11,000	2.5	$2 \times 10^8$
5	600	17,000	3.8	$7 \times 10^7$
10	10,000	22,000	5.6	$2 \times 10^7$
15	17,000	28,000	6.8	$1 \times 10^7$
25	80,000	35,000	8.7	$7 \times 10^6$
60	790,000	44,500	15	$3.4 \times 10^6$

# Spectroscopic Parallax

- If we use well-understood close stars to determine the overall brightness scale of a specific class of star, then measuring the spectrum can be used to give the distance for stars  $> 500$  LY away
  1. Determine Surface Temperature + spectral class of star
  2. Determine where on HR diagram should go
  3. Read off absolute luminosity from HR diagram
  4. Measure apparent luminosity and calculate distance
- works best if many close-by stars

