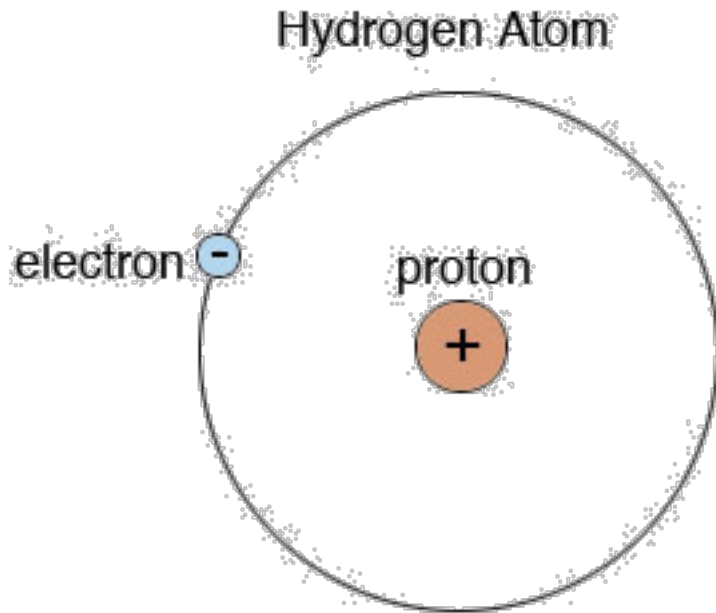


Let's define some units



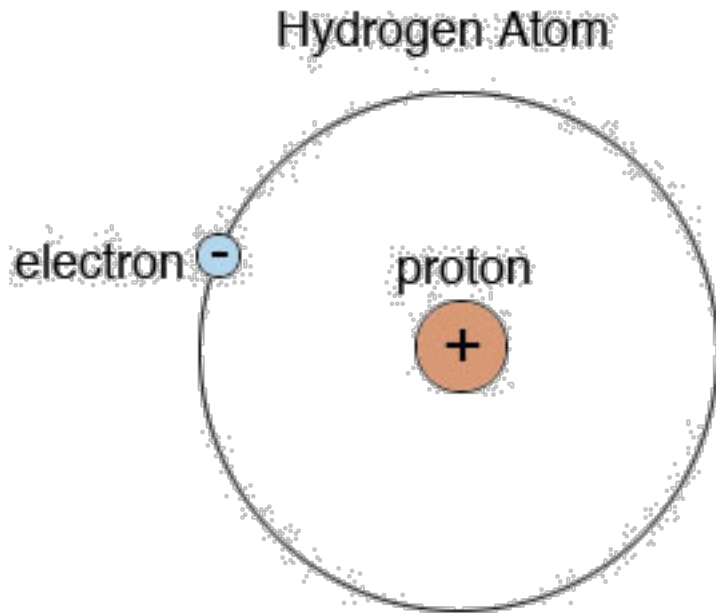
0.15 kg



Electron
mass =
 9×10^{-31} kg



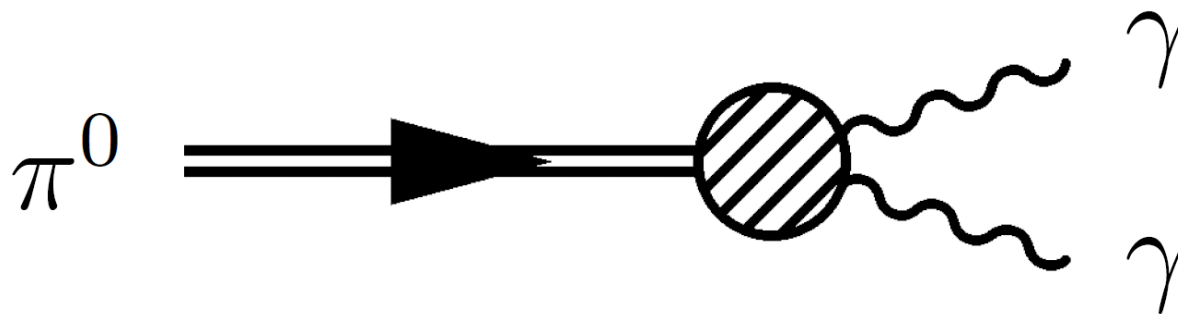
114 meters



Radius of
electron orbit
= 0.5
angstroms =
 5×10^{-11}
meters



This takes 0.4 seconds

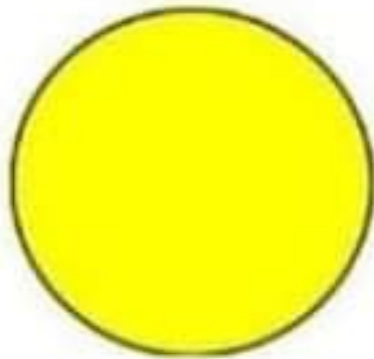


Neutral pion
lifetime =
 8×10^{-17} s

**Do not use
convenient
particle physics
units!**

Smallest things in the Universe

Electron



Quark



X on the mobile ad



by u/xvmir

$$\frac{-\hbar^2}{2m} \frac{\partial^2 u(x)}{\partial x^2} + V(x)u(x) = E u(x)$$

\hbar are pesky and annoying!

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$$E^2 = (pc)^2 + (mc^2)^2$$

so are factors of c everywhere!

$$\hbar = c = 1$$

$$c = 3 \times 10^8 \text{ m/s}$$

$$\hbar = 10^{-34} \text{ J s}$$

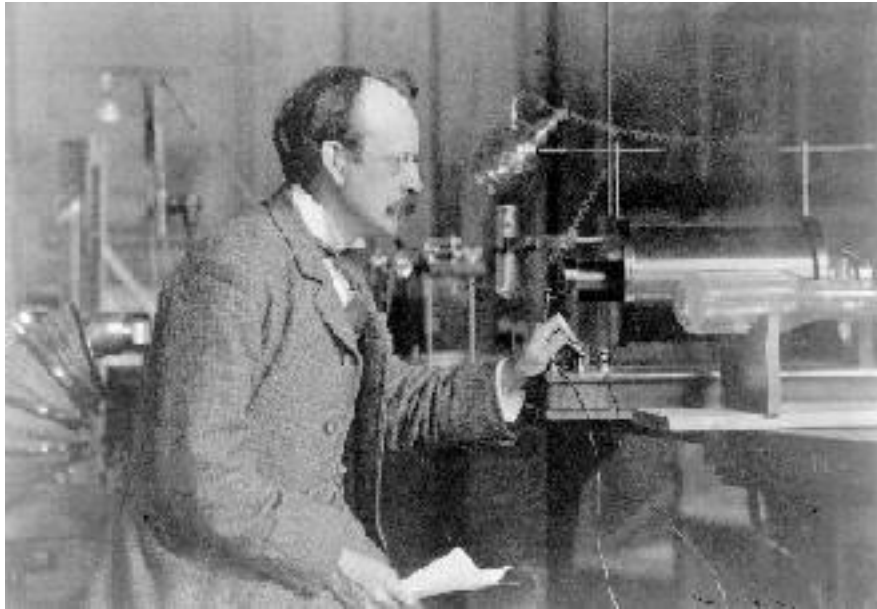
Natural units. Simplifies a lot of notation!

$$1 \text{ GeV} = 10^9 \text{ eV} = 1.6 \times 10^{-10} \text{ J}$$

$$\hbar c = 0.2 \times 10^{-15} \text{ m} = 0.2 \times 10^{-15} \text{ fm}$$

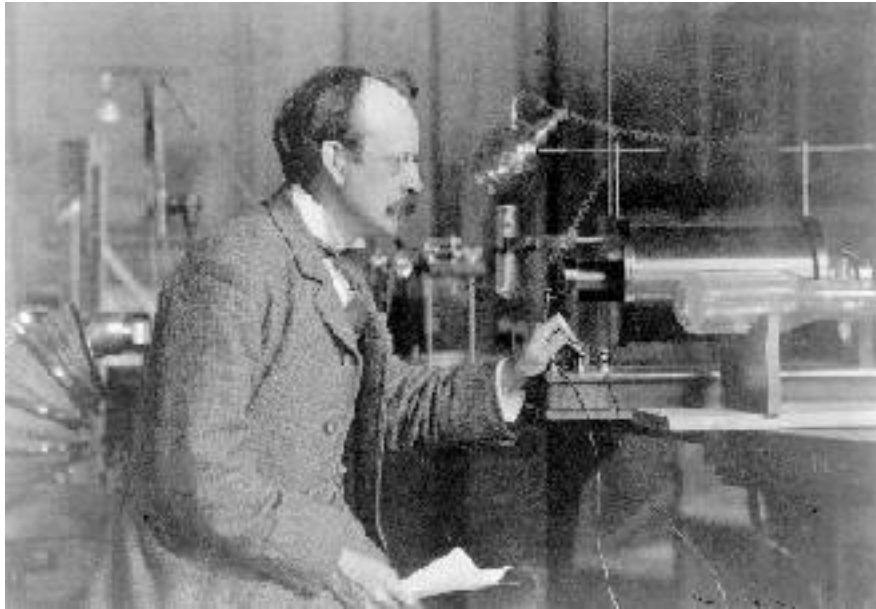
	Not our choice	In our choice of natural units
Energy	GeV	GeV
Momentum	GeV/c	GeV
Mass	GeV/c ²	GeV
Time	\hbar/GeV	GeV ⁻¹
Length	$c\hbar/\text{GeV}$	GeV ⁻¹
Area	$(c\hbar/\text{GeV})^2$	GeV ⁻²

Griffiths disagrees :)



JJ Thompson, who measured the charge to mass ratio of “cathode rays” (aka electrons). Any ideas how he found their velocity and, more importantly, q/m ? (1.1 in Griffiths)

<http://www.phy.cam.ac.uk/history/electron/photos>



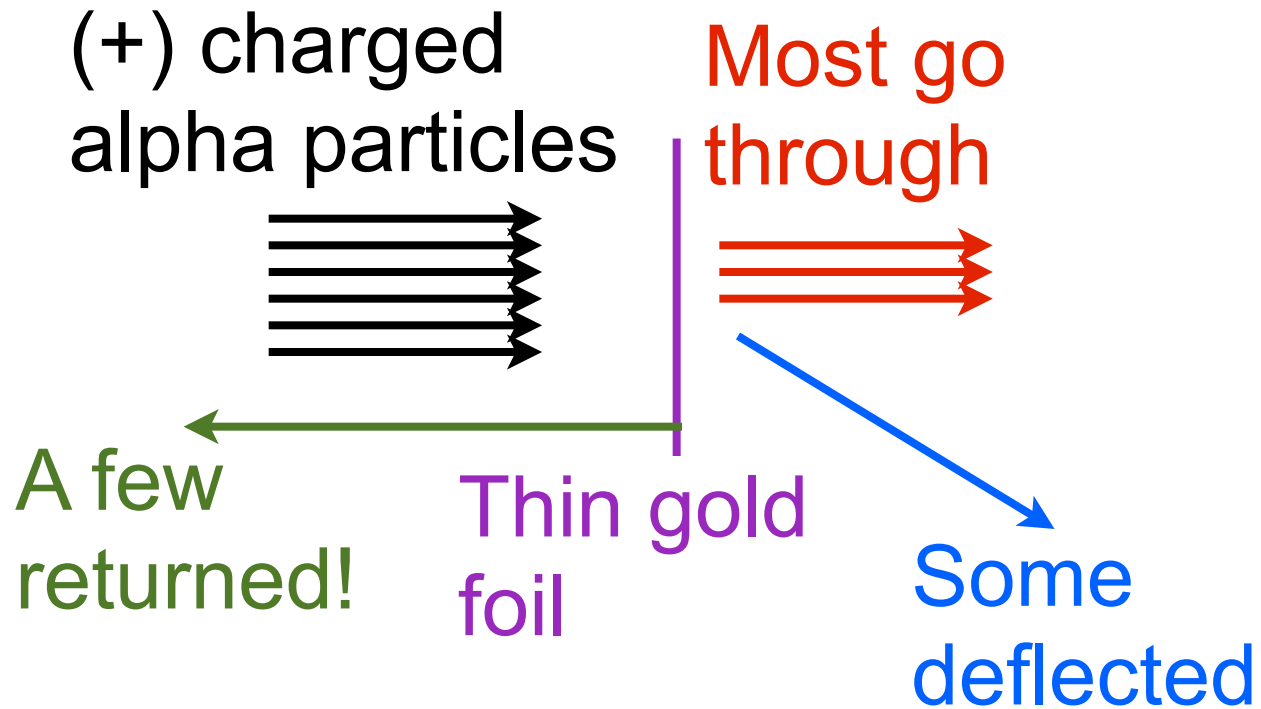
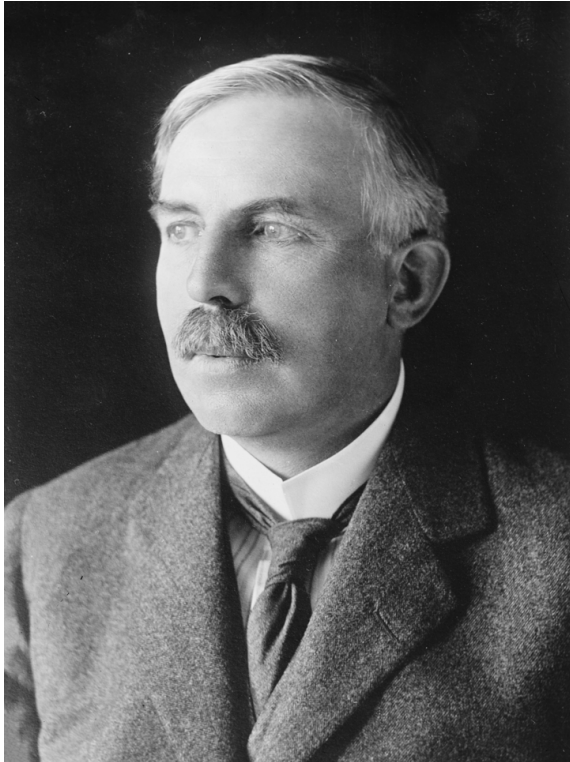
Undelected particle:

$$qE = qvB, v = (E/B)$$

Just magnetic field:

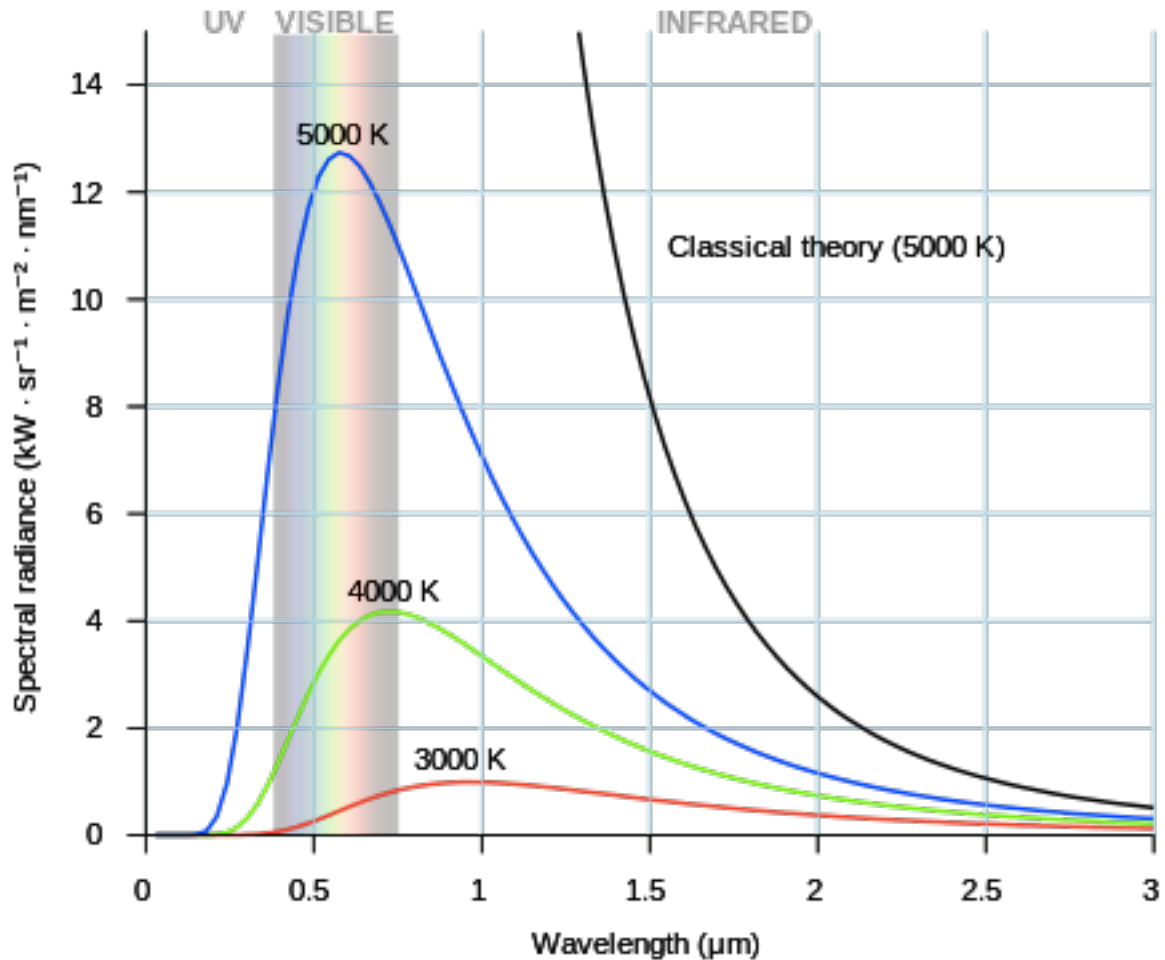
$$qvB = mv^2/R$$

$$(q/m) = v/(BR) = E/(B^2R)$$

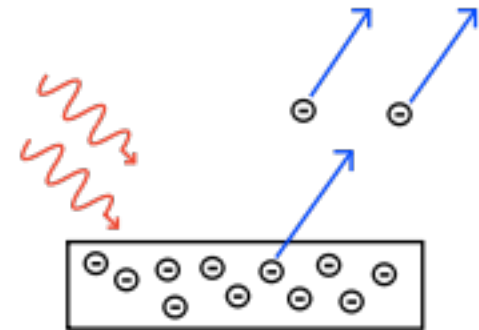
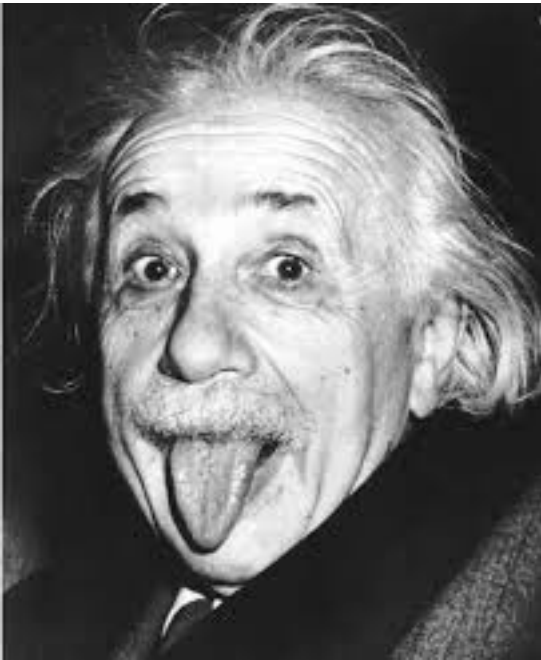


“It was quite the most incredible event that has ever happened to me in my life. It was almost as incredible as if you fired a 15-inch shell at a piece of tissue paper and it came back and hit you.” - led to the idea that positive charge in atom must be concentrated in a small space

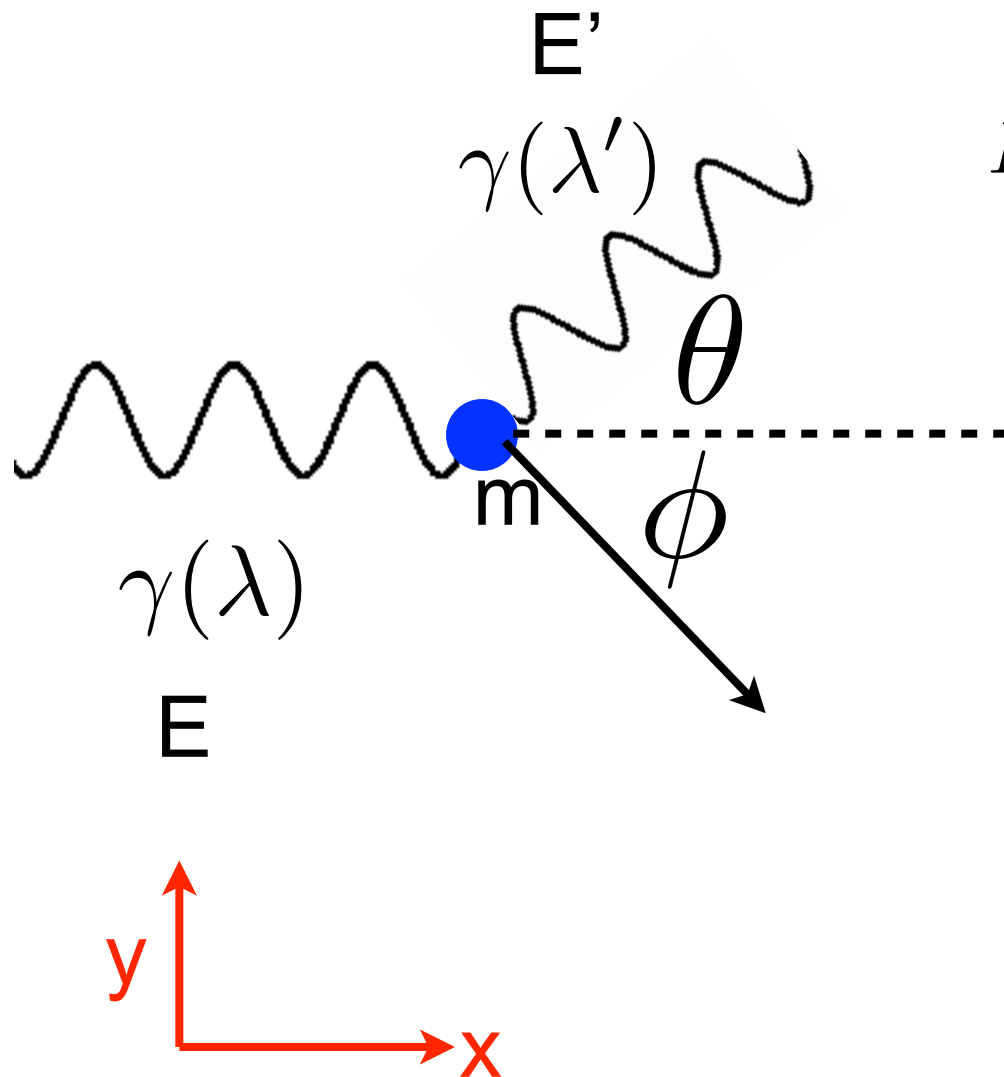
Skipping to Max Planck



Quantization was “a purely formal assumption and I really did not give it much thought except that no matter what the cost, I must bring about a positive end.” (Turns out that Planck didn’t quite realize what he was doing)



A radical idea! The energy of a photon is quantized, and depends on its frequency (color). Higher intensity light will knock out more electrons, but always of the same energy! Isn't light a wave and not a particle?



Conservation of energy

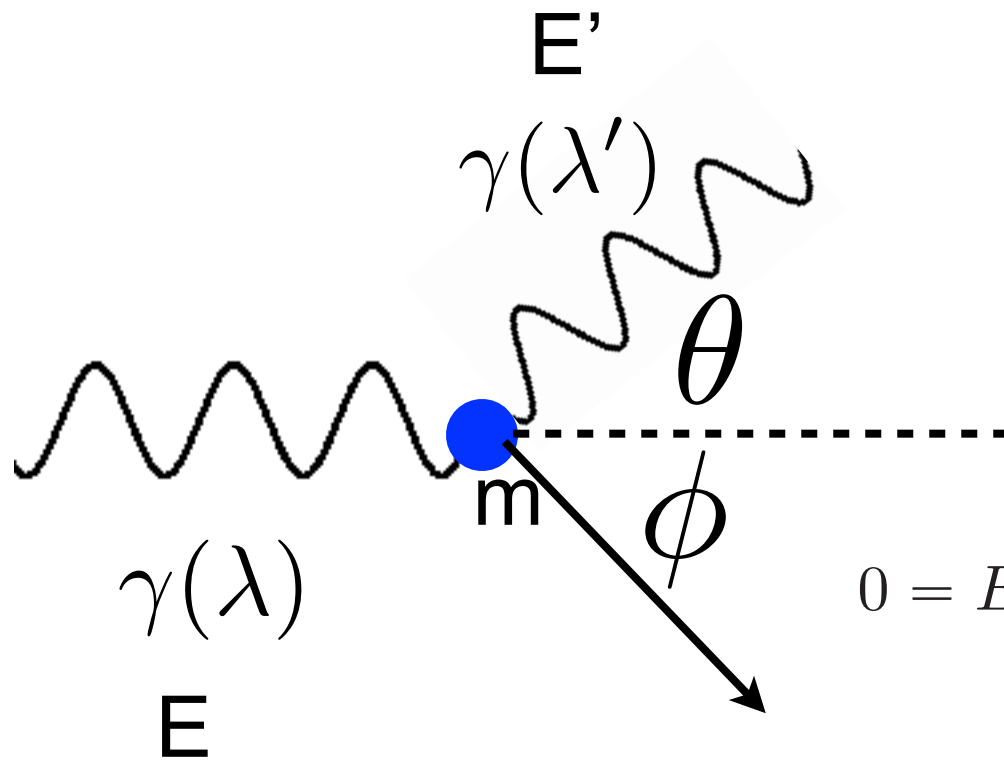
$$E + m = E' + \sqrt{p^2 + m^2}$$

Momentum conservation in x:

$$E = E' \cos \theta + p \cos \phi$$

Momentum conservation in y:

$$0 = E' \sin \theta - p \sin \phi$$



Momentum
conservation in y:

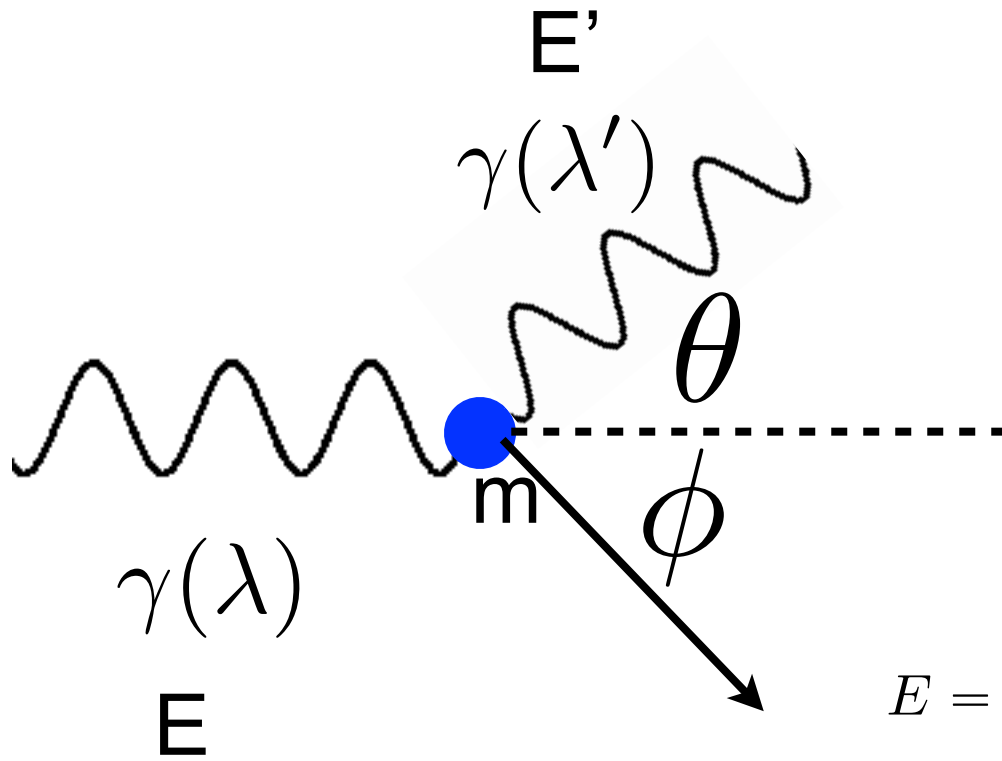
$$0 = E' \sin \theta - p \sin \phi \rightarrow p = \frac{E' \sin \theta}{\sin \phi}$$

$$p^2 \sin^2 \phi = E'^2 \sin^2 \theta$$

$$p^2 (1 - \cos^2 \phi) = E'^2 \sin^2 \theta$$

$$\cos \phi = \sqrt{1 - \frac{E'^2}{p^2} \sin^2 \theta}$$

Momentum
conservation in x:



$$E = E' \cos \theta + p \cos \phi$$

$$E = E' \cos \theta + p \sqrt{1 - \frac{E'^2}{p^2} \sin^2 \theta}$$

$$(E - E' \cos \theta)^2 = p^2 \left(1 - \frac{E'^2}{p^2} \sin^2 \theta \right)$$

$$E^2 + E'^2 \cos^2 \theta - 2EE' \cos \theta = p^2 - E'^2 \sin^2 \theta$$

$$p^2 = E^2 + E'^2 - 2EE' \cos \theta$$

Conservation of energy again

$$E + m = E' + \sqrt{p^2 + m^2}$$

$$(E + m - E') = \sqrt{p^2 + m^2} \quad \text{Plug in } p^2$$

$$(E + m - E')^2 = E^2 + E'^2 - 2EE' \cos \theta + m^2$$

$$E^2 + E'^2 + m^2 + 2mE - 2mE' - 2EE' = E^2 + E'^2 - 2EE' \cos \theta + m^2$$

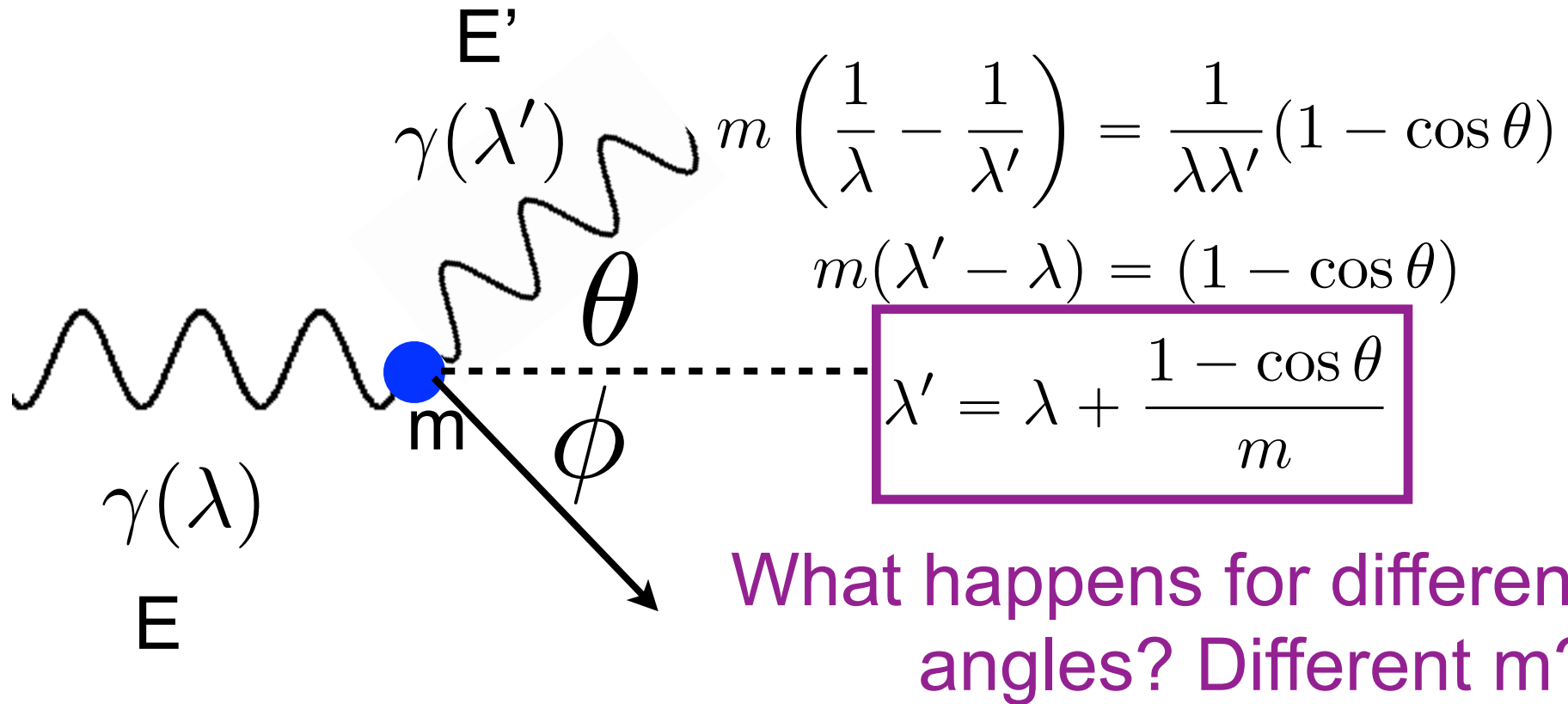
$$2mE - 2mE' = 2EE'(1 - \cos \theta)$$

$$m \left(\frac{1}{\lambda} - \frac{1}{\lambda'} \right) = \frac{1}{\lambda \lambda'} (1 - \cos \theta)$$

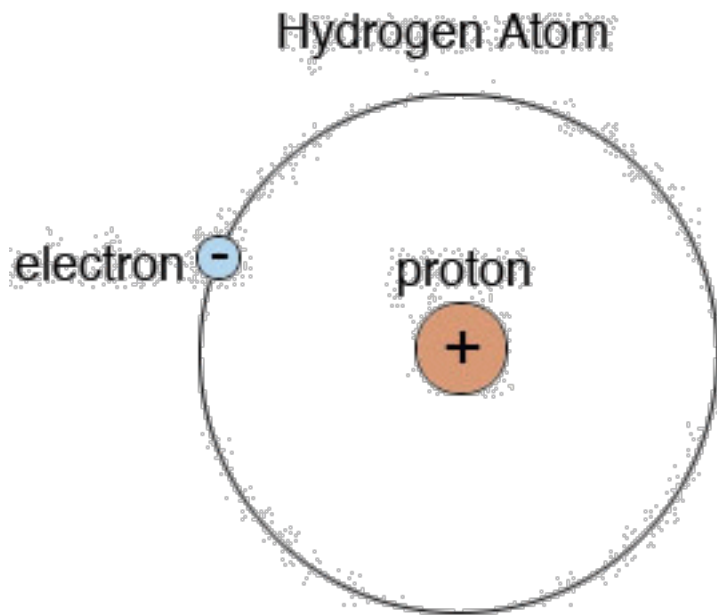
$$E = \frac{1}{\lambda}$$
$$E' = \frac{1}{\lambda'}$$

Nice to have these units

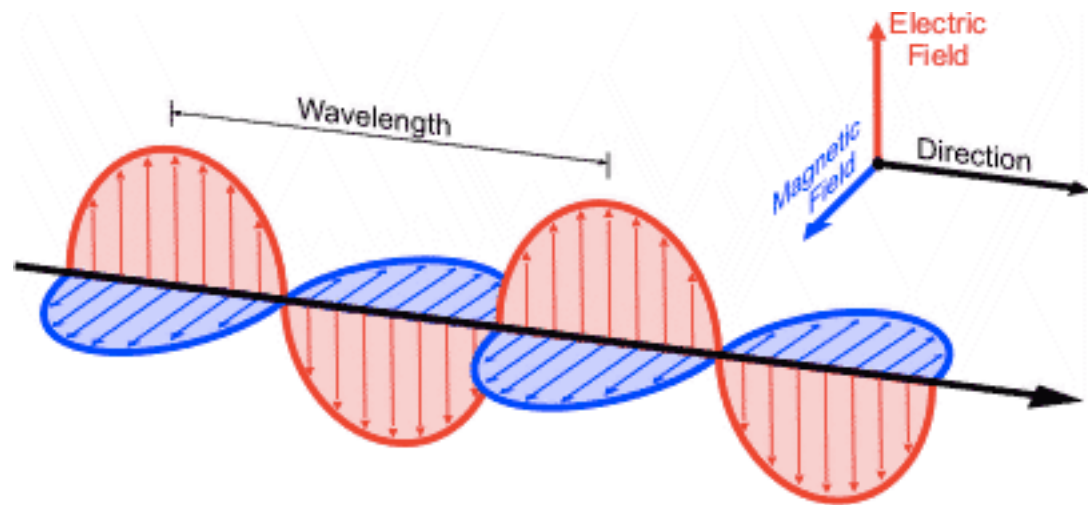
Finishing up

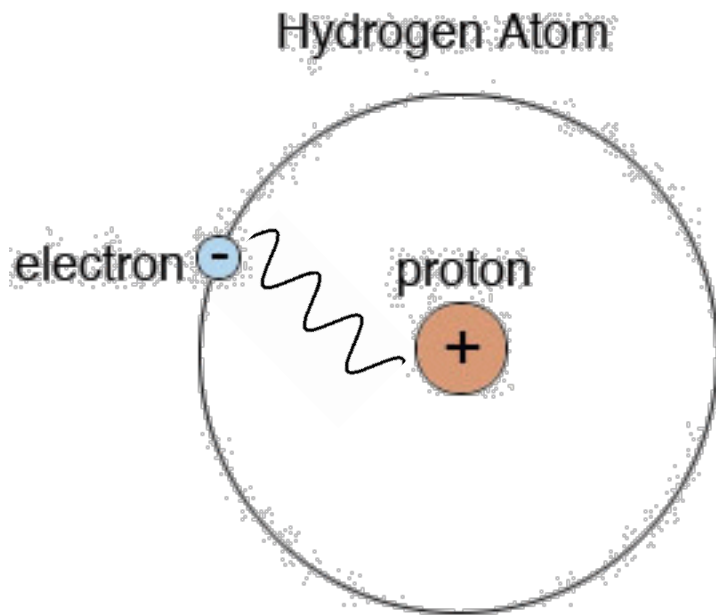


Note that this assumes particles of light, aka photons! No discussion of waves or interference



Photon as a wave



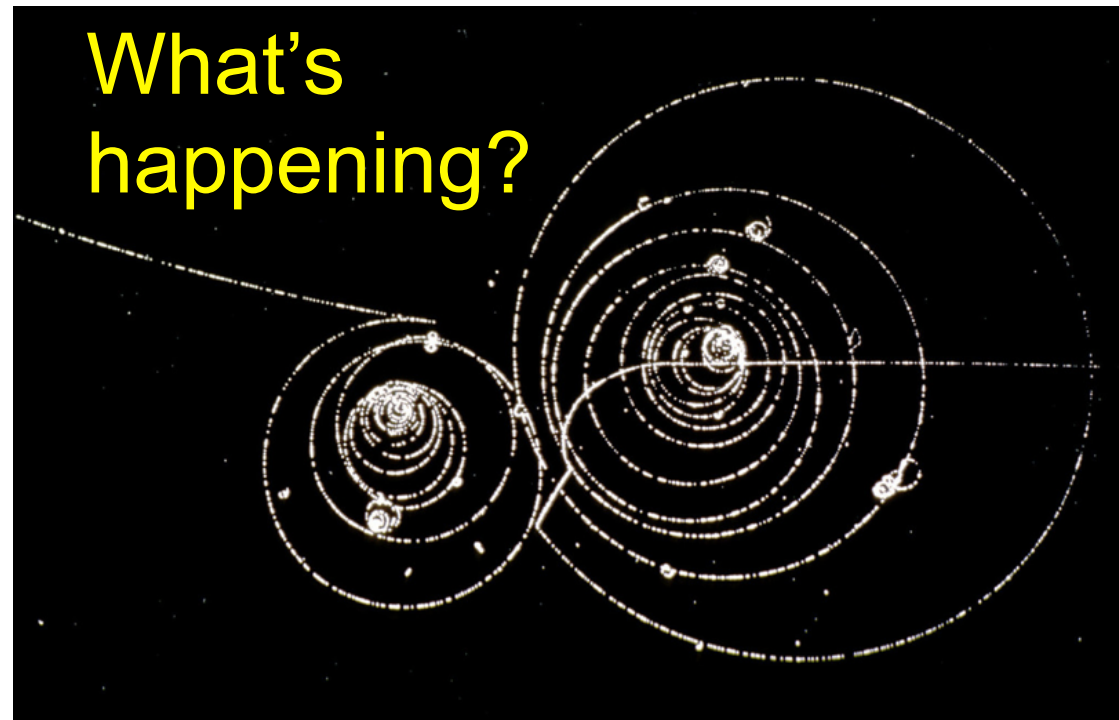


Photon as a particle (classical). But what we really mean is that the field is quantized (here providing an attractive force), and the quantized unit of the field transmits some momentum from one object to another

Early particle detectors - cloud and bubble chambers

A **cloud chamber** is a collection of supersaturated vapor of alcohol or water. A charge particle can ionize the vapor; the subsequent ions act as seeds for condensation. Magnetic fields can give the charge and momenta of objects. Need to literally take pictures of the chambers!

Bubble chamber is similar, except it uses superheated liquid instead



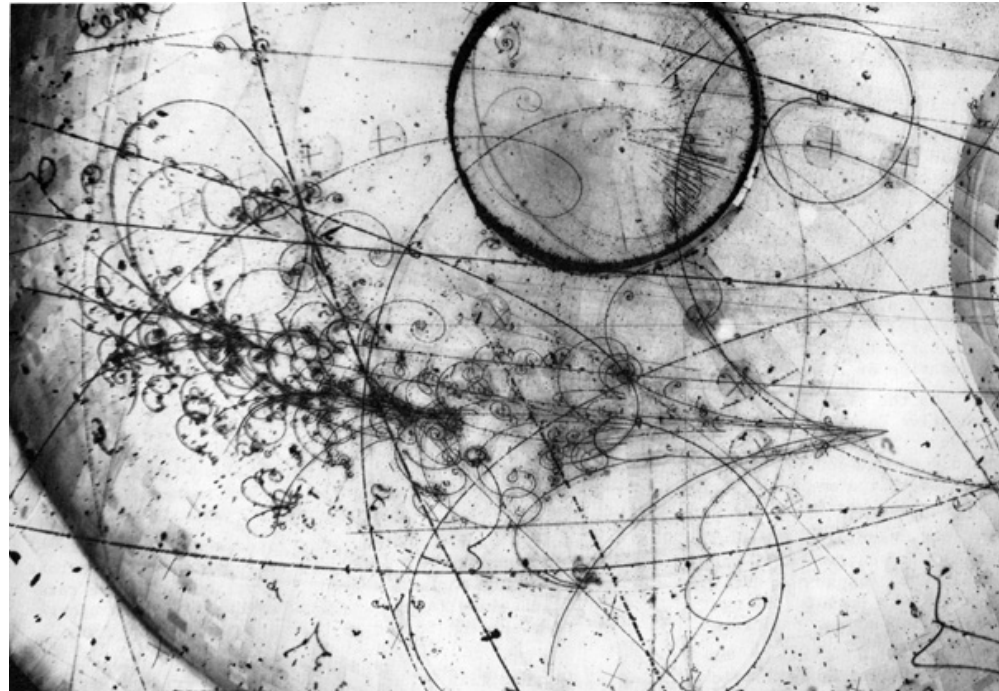
Early particle detectors - cloud and bubble chambers

Glaser invented the bubble chamber (and won a Nobel prize for it).

“Legend has it that while he was on the faculty of the University of Michigan, Glaser was chilling with colleagues over a cold beer, observed the stream of bubbles in his glass, and was inspired to build a device that could track subatomic particles with bubbles. Glaser himself later refuted this story; beer was not his inspiration, although he did use it as a liquid in early prototypes.”

<http://www.aps.org/publications/apsnews/201001/physicshistory.cfm>

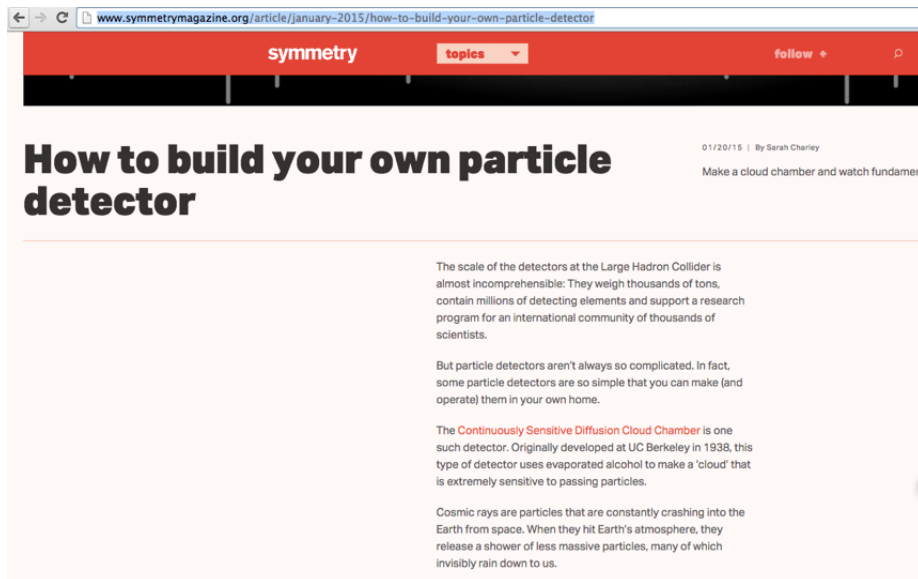
FNAL bubble chamber photo



What's going on here?

Early particle detectors - cloud and bubble chambers

<http://www.symmetrymagazine.org/article/january-2015/how-to-build-your-own-particle-detector>



If anyone knows any enterprising undergrads looking for work, we tried building one a few years ago, but didn't really spend the time or effort. This would be a lot of fun



Strong meson (intermediate mass) must be the nuclear force carrier with mass ~ 150 MeV. See Griffiths HW 1.2 for why this was only a vague estimate - any ideas how he got it (if you haven't read the textbook?)

There are two such mesons observed in cosmic rays:

$$\pi, \mu$$

VERY different interactions with atomic nuclei (one feels the strong nuclear force, the other does not)

From Griffiths

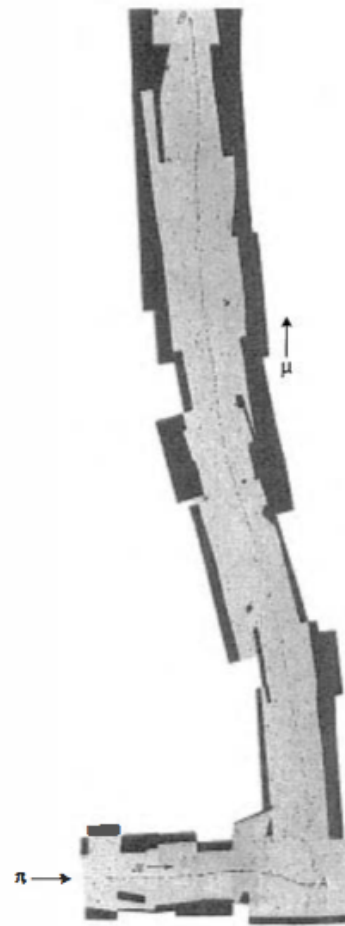


Fig. 1.3 One of Powell's earliest pictures showing the track of a pion in a photographic emulsion exposed to cosmic rays at high altitude. The pion (entering from the left) decays into a muon and a neutrino (the latter is electrically neutral, and leaves no

track). (Source: Powell, C. F., Fowler, P. H. and Perkins, D. H. (1959) *The Study of Elementary Particles by the Photographic Method* Pergamon, New York. First published in (1947) *Nature* 159, 694.)

1931 Anderson discovers antiparticles

From Griffiths

Hypothesized
by Dirac
(we'll see
why in a few
chapters)

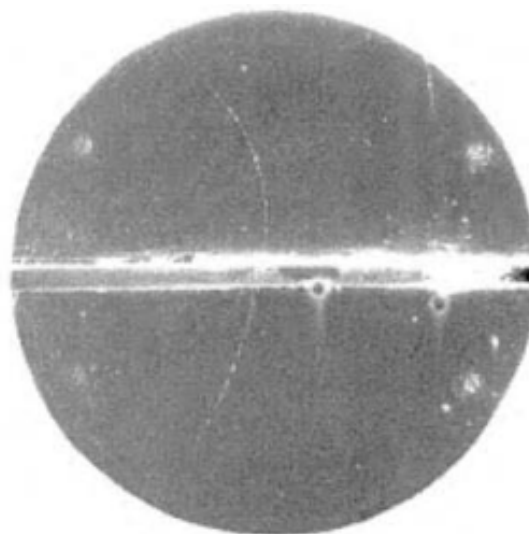
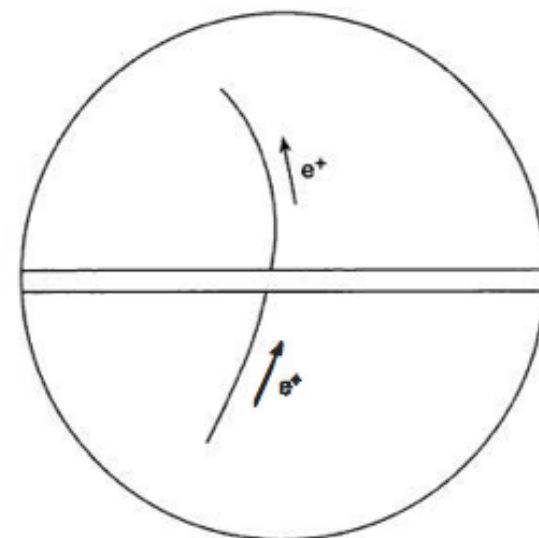


Fig. 1.4 The positron. In 1932, Anderson took this photograph of the track left in a cloud chamber by a cosmic ray particle. The chamber was placed in a magnetic field (pointing into the page), which caused the particle to travel in a curve. But was it a negative charge traveling downward or a positive charge traveling upward? In order to distinguish, Anderson had placed a lead plate across the center of the chamber (the thick horizontal line in the photograph). A



particle passing through the plate slows down, and subsequently moves in a tighter circle. By inspection of the curves, it is clear that this particle traveled upward, and hence must have been positively charged. From the curvature of the track and from its texture, Anderson was able to show that the mass of the particle was close to that of the electron. (Photo courtesy California Institute of Technology.)

Protons vs
anti-proton

$$p = (uud)$$

$$\bar{p} = (\bar{u}\bar{u}\bar{d})$$

Neutron vs anti-
neutron (note:
neutron has no net
electric charge!)

$$n = (udd)$$

$$\bar{n} = (\bar{u}\bar{d}\bar{d})$$

$$e^+ \text{ vs } e^-$$

$$\gamma = \bar{\gamma}$$

$A + B \rightarrow C + D \rightarrow$ If this then
also...

$$A \rightarrow \bar{B} + C + D$$

$$A + \bar{C} \rightarrow \bar{B} + D$$

$\gamma + e^- \rightarrow \gamma + e^-$ Implies

$$e^+ + e^- \rightarrow \gamma + \gamma$$

$$\gamma + \gamma \rightarrow e^+ + e^-$$

$A + B \rightarrow C + D \rightarrow$ If this then
also...

$$A \rightarrow \overline{B} + C + D$$

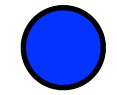
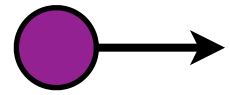
$$A + \overline{C} \rightarrow \overline{B} + D$$

All that it tells us is whether there are any symmetry rules or conservation laws forbidding such a reaction (ie whether the **dynamics** are possible). Says nothing about the **kinematics**

$$A \rightarrow B + e^{-}$$

$$n \rightarrow p + e^{-}$$

What is the energy of the electron in this decay?

 m_A  m_B  m_e

Initially, in center
of mass frame, everything
is at rest, $\mathbf{p} = 0$

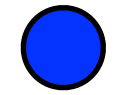
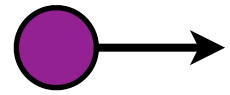
After decay

$$E = m_A$$

$$p = 0$$

$$E = \sqrt{m_B^2 + p_B^2} + \sqrt{m_e^2 + p_e^2}$$

Conservation of momentum: $p_B = p_e = p$

 m_A  m_B  m_e

Initially, in center
of mass frame, everything
is at rest, $p = 0$

After decay

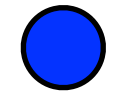
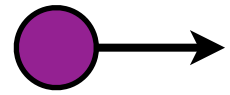
$$E = \sqrt{m_B^2 + p^2} + \sqrt{m_e^2 + p^2} = m_A$$

$$m_B^2 + p^2 + m_e^2 + p^2 + 2\sqrt{(m_B^2 + p^2)(m_e^2 + p^2)} = m_A^2$$

$$2\sqrt{(m_B^2 + p^2)(m_e^2 + p^2)} = m_A^2 - m_B^2 - m_e^2 - 2p^2$$

$$4(m_B^2 + p^2)(m_e^2 + p^2) =$$

$$m_A^4 + m_B^4 + m_e^4 + 4p^4 - 2m_A^2 m_B^2 - 2m_A^2 m_e^2 - 4m_A^2 p^2 + 2m_B^2 m_e^2 + 4m_B^2 p^2 + 4m_e^2 p^2$$

 m_A  m_B  m_e

Initially, in center
of mass frame, everything
is at rest, $p = 0$

After decay

$$\begin{aligned}
 &4m_B^2 m_e^2 + 4m_B^2 p^2 + 4m_e^2 p^2 + 4p^4 = \\
 &m_A^4 + m_B^4 + m_e^4 + 4p^4 - 2m_A^2 m_B^2 - 2m_A^2 m_e^2 - 4m_A^2 p^2 + 2m_B^2 m_e^2 + 4m_B^2 p^2 + 4m_e^2 p^2 \\
 &m_A^4 + m_B^4 + m_e^4 - 2m_A^2 m_B^2 - 2m_A^2 m_e^2 - 4m_A^2 p^2 - 2m_B^2 m_e^2 = 0 \\
 &p^2 = \frac{1}{4} (m_A^2 + (m_B^4 + m_e^4 - 2m_B^2 m_e^2)/m_A^2 - 2m_B^2 - 2m_e^2)
 \end{aligned}$$

Energy of electron is completely specified, but we observe a range of energies in neutron decay! Must be missing some object: neutrinos!

$$\begin{aligned}
 &4m_B^2 m_e^2 + 4m_B^2 p^2 + 4m_e^2 p^2 + 4p^4 = \\
 &m_A^4 + m_B^4 + m_e^4 + 4p^4 - 2m_A^2 m_B^2 - 2m_A^2 m_e^2 - 4m_A^2 p^2 + 2m_B^2 m_e^2 + 4m_B^2 p^2 + 4m_e^2 p^2 \\
 &m_A^4 + m_B^4 + m_e^4 - 2m_A^2 m_B^2 - 2m_A^2 m_e^2 - 4m_A^2 p^2 - 2m_B^2 m_e^2 = 0 \\
 &p^2 = \frac{1}{4} (m_A^2 + (m_B^4 + m_e^4 - 2m_B^2 m_e^2)/m_A^2 - 2m_B^2 - 2m_e^2)
 \end{aligned}$$

Energy of electron is completely specified, but we observe a range of energies in neutron decay! Must be missing some object: neutrinos!

From
Griffiths

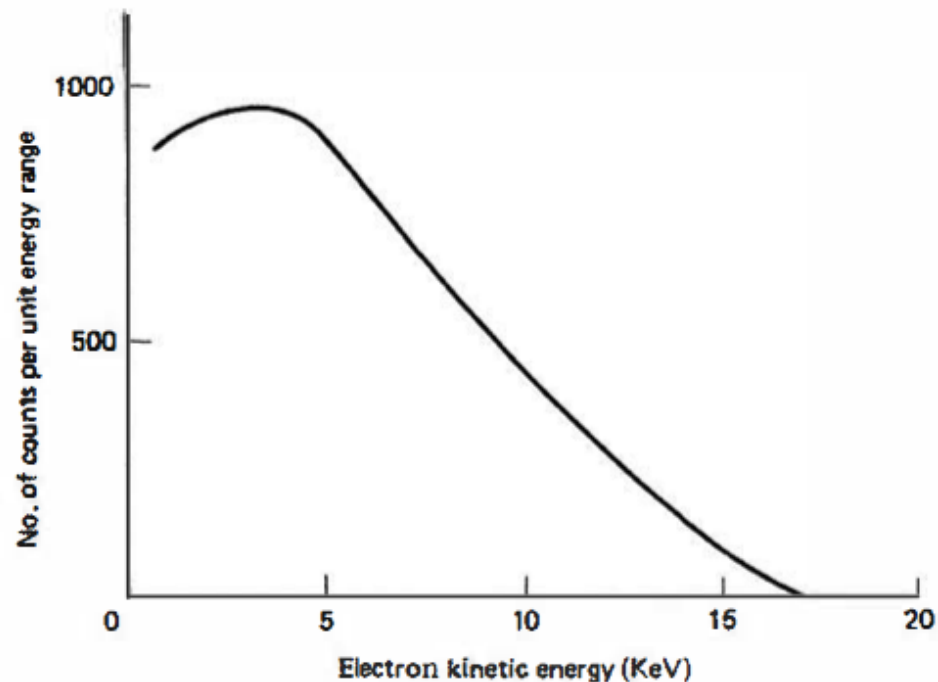


Fig. 1.5 The beta decay spectrum of tritium (${}^3_1\text{H} \rightarrow {}^3_2\text{He}$).
(Source: Lewis, G. M. (1970) *Neutrinos*, Wykeham, London, p. 30.)

“Little neutral one” to distinguish from the neutron. Physicists really cling to the idea of conservation of energy

From
Griffiths

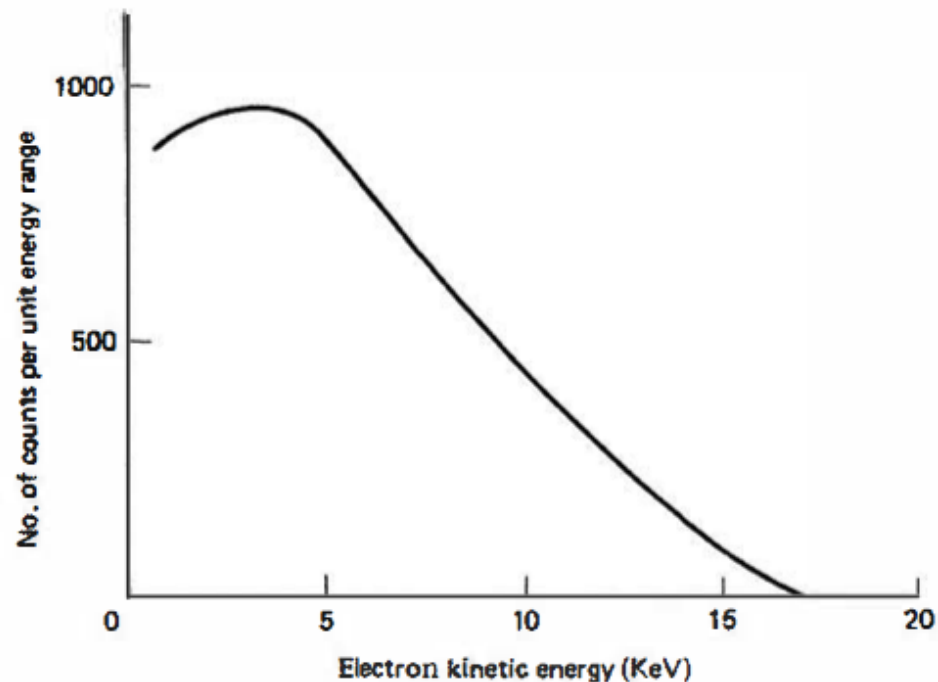
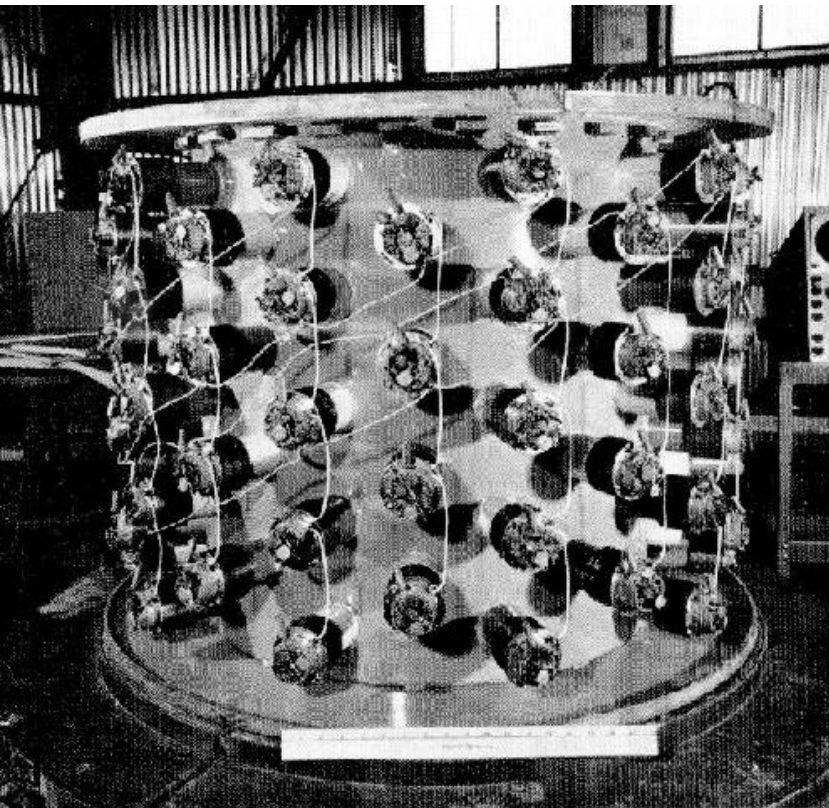
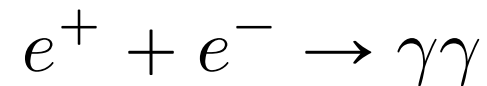
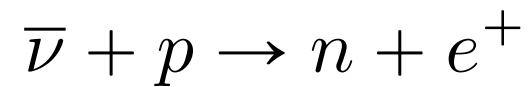


Fig. 1.5 The beta decay spectrum of tritium (${}^3_1\text{H} \rightarrow {}^3_2\text{He}$).
(Source: Lewis, G. M. (1970) *Neutrinos*, Wykeham, London, p. 30.)



Large tank of water
mixed with cadmium
chloride near a nuclear
reactor to look for



What about the neutron?
It gets captured by
cadmium, which then
emits pairs of photons
shortly thereafter

Tests with anti-neutrinos?

$$n + \nu \rightarrow p + e^{-}$$

$$n + \bar{\nu} \nrightarrow p + e^{-}$$

$$\gamma + \gamma \nrightarrow \mu^{+} + e^{-}$$

$$\mu^{-} \nrightarrow e^{-} + \gamma$$

Be careful
about what is
+1 and what
is -1!

Why not? Well, neutrinos and anti-neutrinos are not the same thing. But also... this violates a conservation law known as conservation of electron number.

Electrons and electron neutrinos carry electron number = +1, and anti-electrons and anti-electron neutrinos = -1

Define in the same way a
“muon number”. Muons
and muon neutrinos carry
muon number = +1, and
anti-muons and anti-
muon neutrinos = -1

And yet the same thing for
taus (which we haven't
seen quite yet but we will
soon)

Checks to make sure your neutrinos are in the right place

	Before			After	
	e	mu		e	mu
$\bar{\nu}_e + p \rightarrow n + e^+$	-1	0		-1	0
$\pi^+ \rightarrow \mu^+ + \nu_\mu$	0	0		0	1-1=0
$\pi^- \rightarrow \mu^- + \bar{\nu}_\mu$	0	0		0	1-1=0
$\mu^- \rightarrow e^- + \bar{\nu}_e + \nu_\mu$	0	1		1-1=0	1
$n \rightarrow p + e^- + \bar{\nu}_e$	0	0		1-1=0	0

Conservation of baryon number

Neutron decay

$$n \rightarrow e^{-} + \bar{\nu}_e + p$$

No proton decay

$$p \nrightarrow e^{+} + \nu_e$$

$$p \nrightarrow e^{+} + \nu_e + \gamma$$

Proton decay is not observed! Why not?

Propose conservation of baryon number

B = +1 for neutrons and protons, -1 for anti-neutrons and anti-protons

Proton is lightest baryon, so it cannot decay (well, not in the Standard Model!)

No “conservation of meson” number

Strange things

From Griffiths

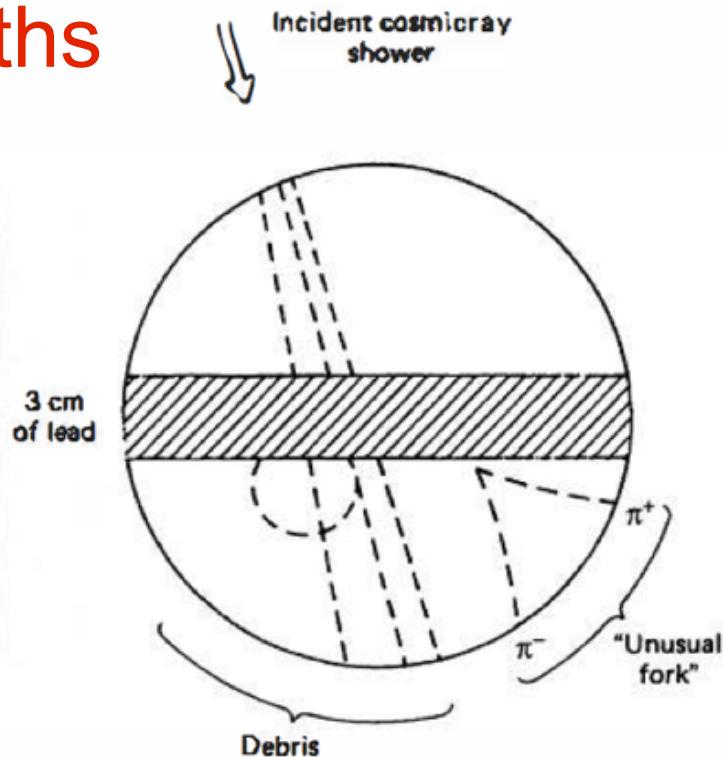
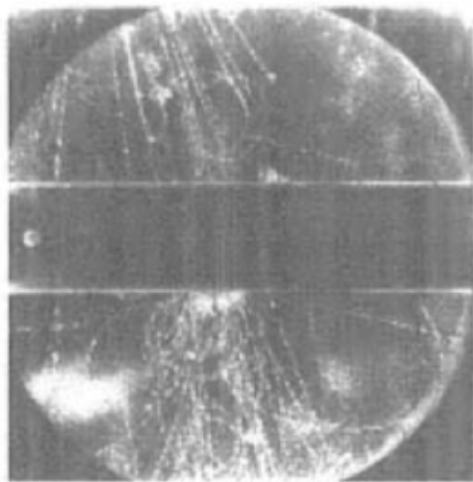


Fig. 1.7 The first strange particle. Cosmic rays strike a lead plate, producing a K^0 , which subsequently decays into a pair of charged pions. (Photo courtesy of Prof. Rochester, G. D. (© 1947). *Nature*, **160**, 855. Copyright Macmillan Journals Limited.)

$$K^0 \rightarrow \pi^+ + \pi^-$$

What is this neutral kaon?
Can produce them in accelerators, but they decay 13 orders of magnitude slower than expected!
Strange...

How to account for these strange particles?

What if kaons
are produced
by the strong
force, but
decay typically
via the weak
force?

Strangeness is
conserved in
strong
interactions but
not in weak
interactions

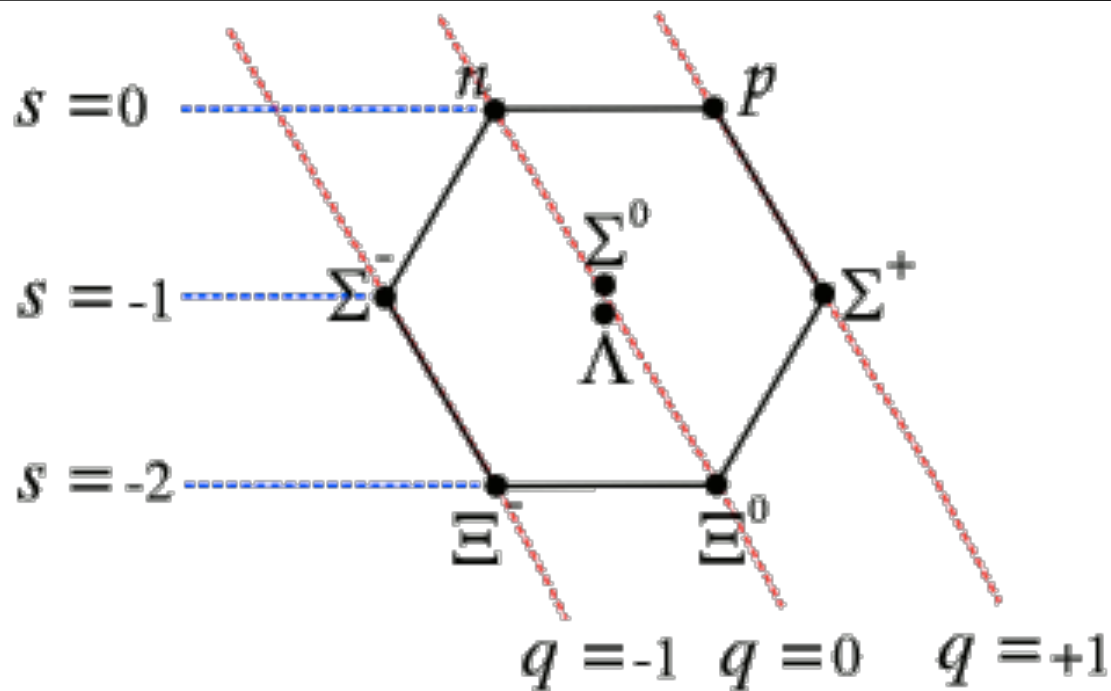
$$\pi^{-} + p \rightarrow K^{+} + \Sigma^{-}$$

$$\pi^{-} + p \rightarrow K^{0} + \Sigma^{0}$$

$$\pi^{-} + p \rightarrow K^{0} + \Lambda$$

Initially, have zero
strangeness. Assign $S=+1$
to K^{+} and K^{0} and $S=-1$ to Λ
and Σ , S remains 0. What
does this say about how
the above are produced?
Note: strangeness not
conserved in the decay.

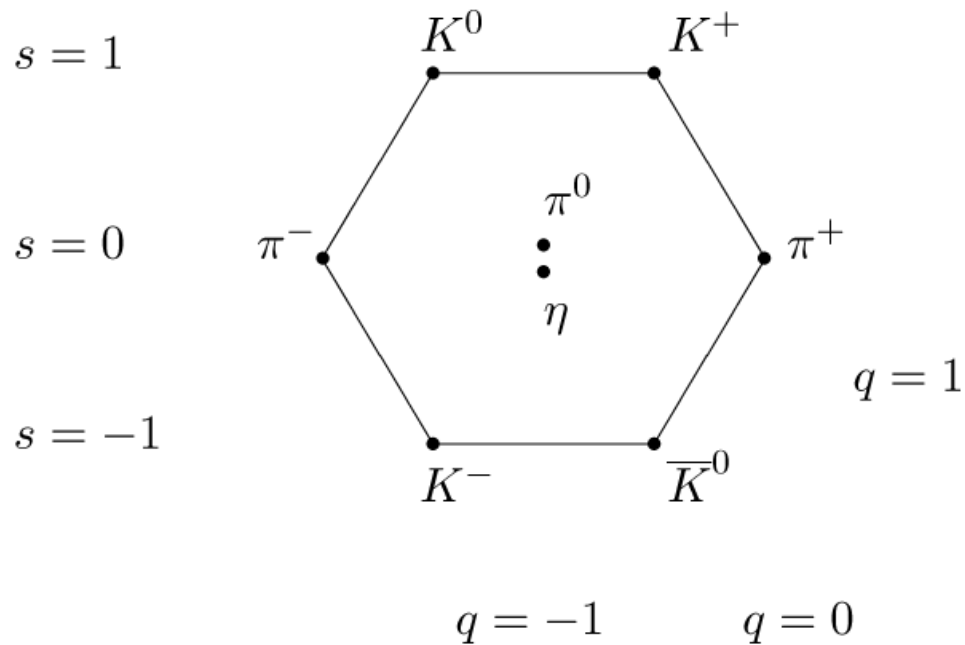
And how to start organizing all of this?



Murray Gell-Man proposed his “Eightfold way” (apparently a slight reference to the Noble Eightfold path of Buddhism)



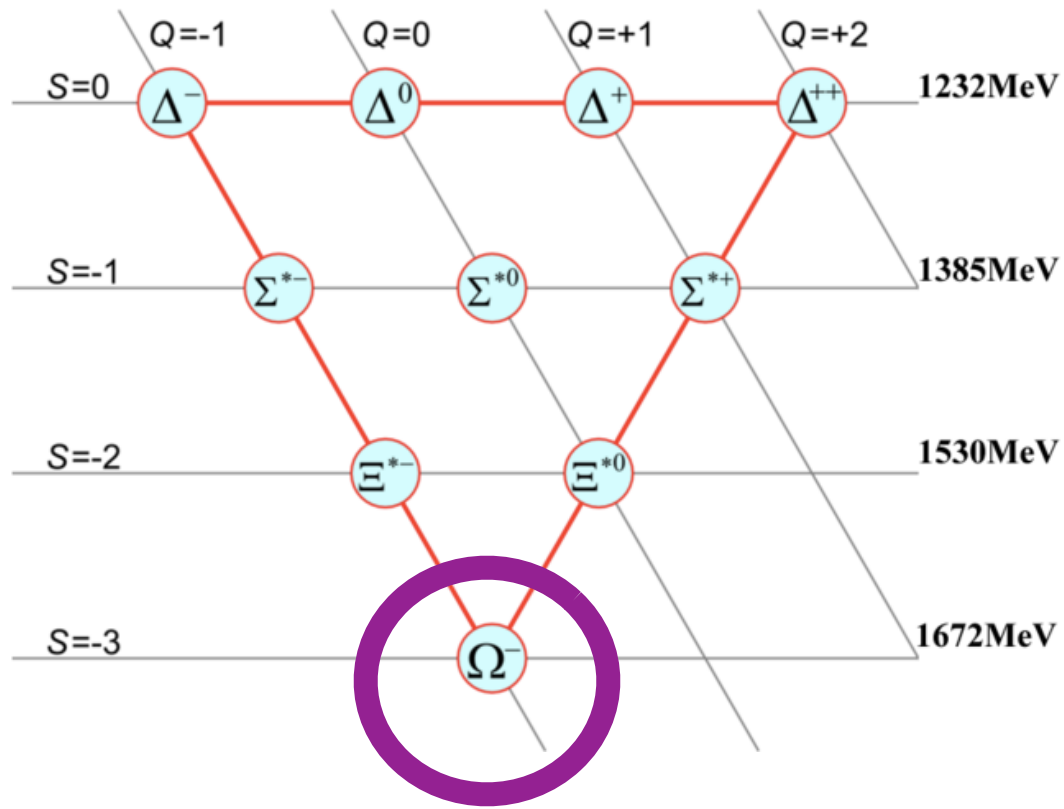
Moving from baryons to mesons



Similar periodic structure
(remind you of anything)?



How was this verified?



This was predicted (including its mass and lifetime!)



The particle ... zoo
was becoming a big
mess to keep track
of

Wolfgang Pauli: "Had I
foreseen that, I would
have gone into botany"



The particle ... zoo was becoming a big mess to keep track of (for some reason, physicists don't like botanists, apparently)

Fermi to Lederman:
“Young man, if I could remember the names of these particles, I would have been a botanist”



The quark model (Gell-Man and Zweig)

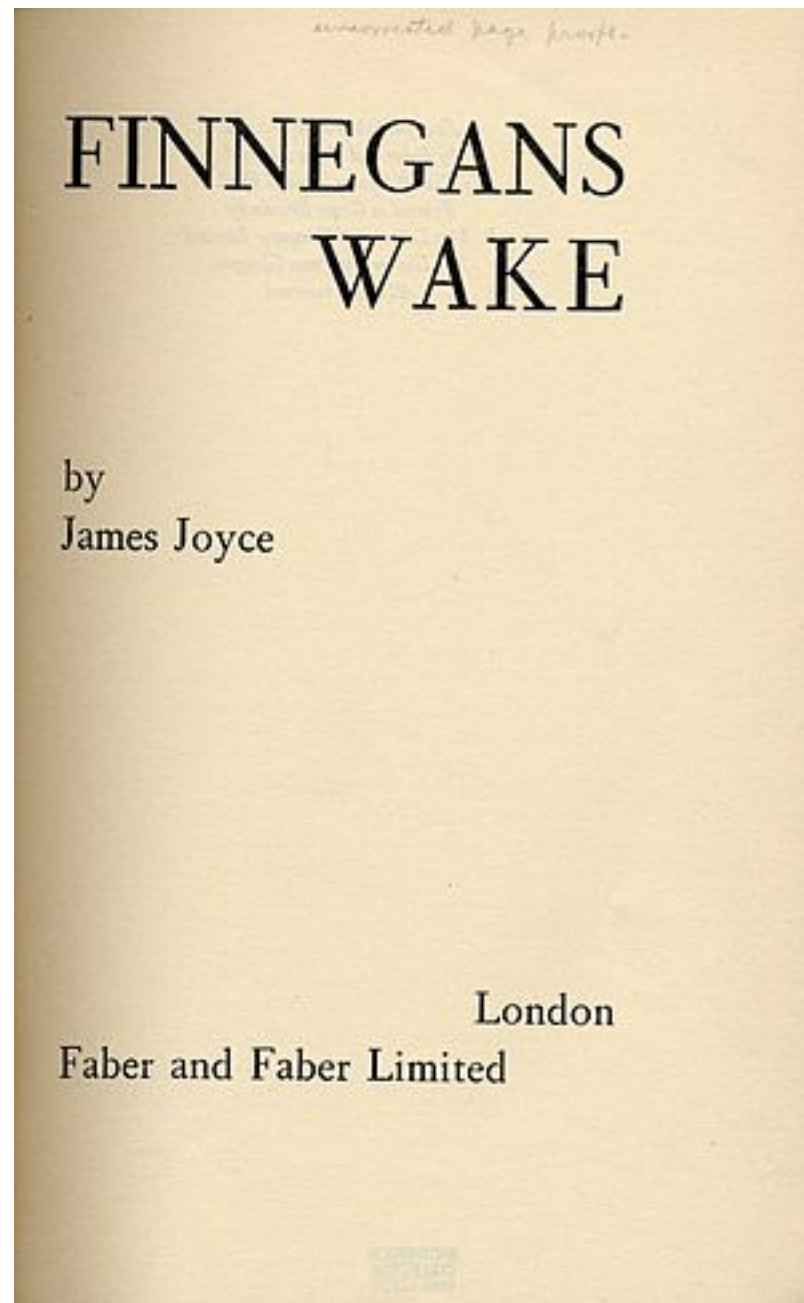
Three quarks for Muster Mark!

Sure he has not got much of a bark
And sure any he has it's all beside
the mark.

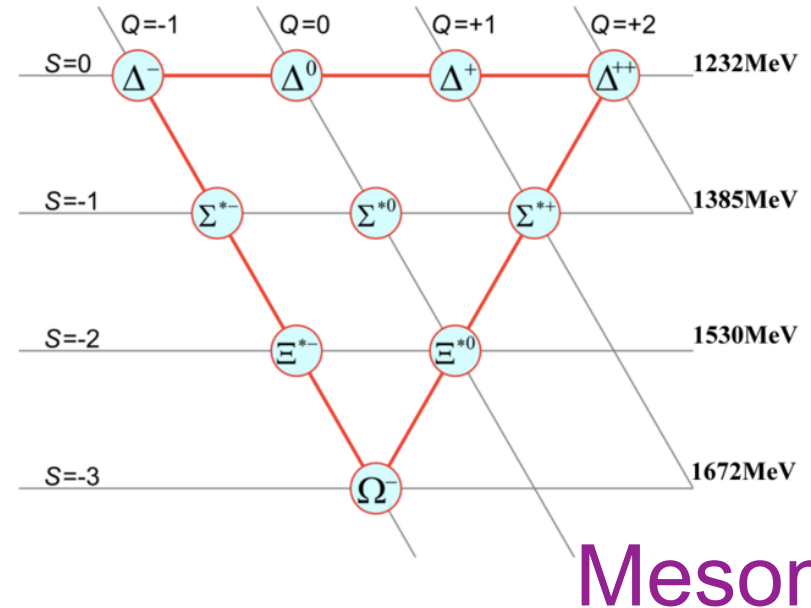
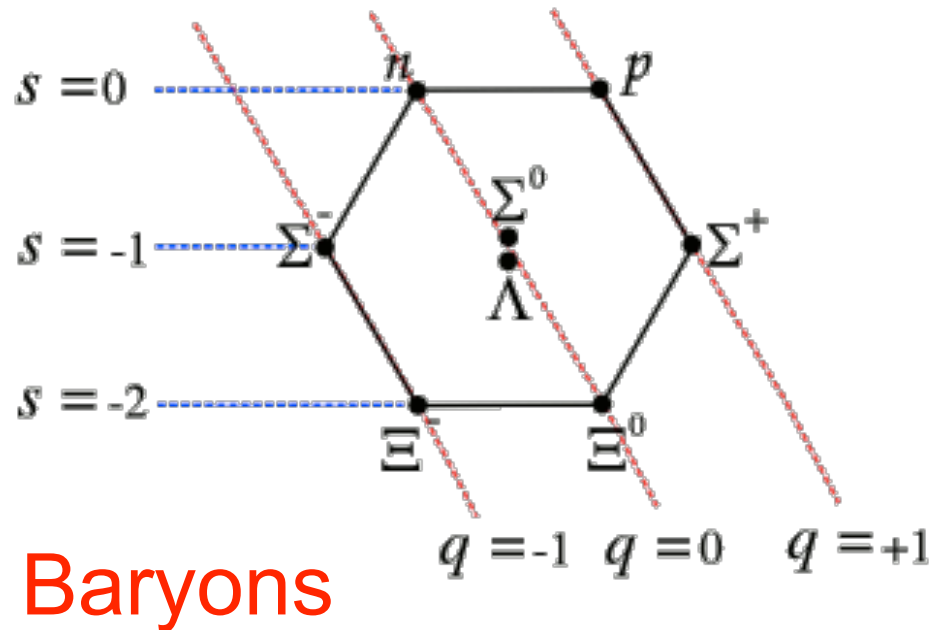
—James Joyce, *Finnegans Wake*

Quark and not
kwork!

Wikipedia: *Finnegans Wake* is a novel by Irish writer James Joyce. It is significant for its experimental style and reputation as one of the most difficult works of fiction in the English language.



Hadrons



All **hadrons** (**baryons** and **mesons**) are made themselves of smaller pieces called **quarks**

The quark model (so far in our course)

	Charge (units of e)	Strangeness
u	$+2/3$	0
d	$-1/3$	0
s	$-1/3$	1
ubar	$-2/3$	0
dbar	$+1/3$	0
sbar	$+1/3$	-1

Mesons = one quark and one anti-quark

Baryons = three quarks

Anti-baryons = three anti-quarks

Example of the baryon decuplet

	Q	S	Baryon	B number
uuu	2	0	Δ^{++}	1
uud	1	0	Δ^{+}	1
udd	0	0	Δ^0	1
ddd	-1	0	Δ^{-}	1
uus	1	-1	Σ^{*+}	1
uds	0	-1	Σ^{*0}	1
dds	-1	-1	Σ^{*-}	1
uss	0	-2	Ξ^{*0}	1
dss	-1	-2	Ξ^{*-}	1
sss	-1	-3	Ω^{-}	1

Note that this fills in nicely and makes predictions, but we have yet to account for different energy levels and spin

1

Meson Summary Table

See also the table of suggested $q\bar{q}$ quark-model assignments in the Quark Model section.

• Indicates particles that appear in the preceding Meson Summary Table. We do not regard the other entries as being established.

LIGHT UNFLAVORED ($S=C=B=0$)		STRANGE ($S=\pm 1, C=B=0$)		CHARMED, STRANGE ($C=S=\pm 1$)		$\bar{c}c$ $f_c(f_c)$	
	$f_c(f_c)$		$f_c(f_c)$		$f_c(f_c)$		
π^\pm	$1^-(0^-)$	$\phi(1680)$	$0^-(1^-)$	K^\pm	$1/2(0^-)$	D_s^\pm	$0^+(0^-)$
π^0	$1^-(0^-)$	$\rho_3(1690)$	$1^+(3^-)$	K^0	$1/2(0^-)$	D_s^\pm	$0^-(1^-)$
η	$0^+(0^-)$	$\phi(1700)$	$1^+(1^-)$	K_S^0	$1/2(0^-)$	$D_{s0}^*(2317)^\pm$	$0^+(1^+)$
$f_0(500)$	$0^+(0^-)$	$a_0(1700)$	$1^-(2^+)$	K_L^0	$1/2(0^-)$	$D_{s1}^*(2460)^\pm$	$0^+(1^+)$
$\rho(770)$	$1^+(1^-)$	$f_0(1710)$	$0^+(0^+)$	$K_2^*(800)$	$1/2(0^+)$	$D_{s1}^*(2536)^\pm$	$?^?(1^+)$
$\omega(782)$	$0^-(1^-)$	$\eta(1760)$	$0^+(0^-)$	$K^*(892)$	$1/2(1^-)$	$D_{s2}^*(2573)$	$0^+(2^+)$
$\eta'(958)$	$0^+(0^+)$	$\pi(1800)$	$1^-(0^-)$	$K_1^*(1270)$	$1/2(1^+)$	$D_{s1}^*(2700)^\pm$	$0^-(0^-)$
$f_0(980)$	$0^+(0^+)$	$f_2(1810)$	$0^+(2^+)$	$K_1^*(1400)$	$1/2(1^+)$	$D_{s1}^*(2860)^\pm$	$0^-(1^-)$
$a_0(980)$	$1^-(0^+)$	$X(1835)$	$?^?(?^-)$	$K^*(1410)$	$1/2(1^-)$	$D_{s1}^*(3040)^\pm$	$X(3823)$
$\omega(1020)$	$0^-(1^-)$	$X(1840)^\pm$	$?^?(?^\pm)$	$K_2^*(1430)$	$1/2(0^+)$		$X(3872)$
$f_1(1170)$	$0^-(1^+)$	$\phi_3(1850)$	$0^-(3^-)$	$K_2^*(1430)$	$1/2(2^+)$		$X(3900)^\pm$
$b_1(1235)$	$1^-(1^+)$	$\eta_2(1870)$	$0^+(2^+)$	$K(1460)$	$1/2(0^-)$		$X(3900)^\pm$
$a_1(1260)$	$1^-(1^+)$	$\pi_2(1880)$	$1^-(2^+)$	$K(1580)$	$1/2(2^-)$		$\lambda_{c0}(2P)$
$f_2(1270)$	$0^+(2^+)$	$\mu(1900)$	$1^+(1^-)$	$K_1^*(1580)$	$1/2(2^-)$		$\chi_{c2}(2P)$
$f_1(1285)$	$0^+(1^+)$	$f_2(1910)$	$0^+(2^+)$	$K(1630)$	$1/2(2^-)$		$X(3940)$
$\eta(1295)$	$0^+(0^-)$	$f_2(1910)$	$0^+(2^+)$	$K_1^*(1650)$	$1/2(1^+)$		$X(4020)^\pm$
$\omega(1300)$	$1^-(0^+)$	$f_2(1950)$	$0^+(2^+)$	$K^*(1680)$	$1/2(1^-)$		$\psi(4040)$
$a_2(1320)$	$1^-(2^+)$	$\rho_3(1990)$	$1^+(3^-)$	$K_2^*(1770)$	$1/2(2^-)$		$X(4050)^\pm$
$f_0(1370)$	$0^+(0^+)$	$f_2(2010)$	$0^+(2^+)$	$K_2^*(1780)$	$1/2(3^-)$		$X(4140)$
$h_1(1380)$	$?^-(1^+)$	$f_0(2020)$	$0^+(0^+)$	$K_2^*(1820)$	$1/2(2^-)$		$\psi(4160)$
$\pi_1(1400)$	$1^-(1^+)$	$a_4(2040)$	$1^-(4^+)$	$K(1830)$	$1/2(0^-)$		$X(4160)^\pm$
$\eta(1405)$	$0^+(0^+)$	$f_4(2050)$	$0^+(4^+)$	$K_2^*(1950)$	$1/2(0^+)$		$X(4250)^\pm$
$f_1(1420)$	$0^+(1^+)$	$\pi_2(2100)$	$1^-(2^+)$	$K_2^*(1980)$	$1/2(2^+)$		$X(4260)$
$\omega(1420)$	$0^-(1^-)$	$f_0(2100)$	$0^+(0^+)$	$K_2^*(2045)$	$1/2(4^+)$		$X(4350)$
$f_2(1430)$	$0^+(2^+)$	$f_2(2150)$	$0^+(2^+)$	$K_2(2250)$	$1/2(3^-)$		$X(4360)$
$a_0(1450)$	$1^-(0^+)$	$\mu(2150)$	$1^+(1^-)$	$K_2(2320)$	$1/2(3^+)$		$\psi(4415)$
$\phi(1450)$	$1^-(1^+)$	$\phi(2170)$	$0^-(1^-)$	$K_2(2380)$	$1/2(5^-)$		$X(4430)^\pm$
$\eta(1475)$	$0^+(0^+)$	$f_0(2200)$	$0^+(0^+)$	$K_4(2500)$	$1/2(4^-)$		$X(4660)$
$f_0(1500)$	$0^+(0^+)$	$f_2(2220)$	$0^+(2^+)$	$K(3100)$	$1/2(2^?)$		
$f_1(1510)$	$0^+(1^+)$	$\alpha(4^-)$	$0^-(0^-)$				
$f_2(1525)$	$0^+(2^+)$	$\eta(2225)$	$0^+(0^-)$				
$f_2(1565)$	$0^+(2^+)$	$\rho_3(2230)$	$1^+(3^-)$				
$\mu(1570)$	$1^+(1^-)$	$f_2(2300)$	$0^+(2^+)$				
$h_1(1595)$	$0^-(1^+)$	$f_1(2300)$	$0^+(4^+)$				
$\pi_1(1600)$	$1^-(1^+)$	$f_0(2330)$	$0^+(0^+)$				
$a_1(1640)$	$1^-(1^+)$	$f_2(2340)$	$0^+(2^+)$				
$f_2(1640)$	$0^+(2^+)$	$\rho_5(2350)$	$1^+(5^-)$				
$\eta_2(1645)$	$0^+(2^+)$	$a_6(2450)$	$1^-(6^+)$				
$\omega(1650)$	$0^-(1^-)$	$f_6(2510)$	$0^+(6^+)$				
$\omega_3(1670)$	$0^-(3^-)$						
$\pi_2(1670)$	$1^-(2^-)$						

1
Baryon Summary Table

This short table gives the name, the quantum numbers (where known), and the status of baryons in the Review. Only the baryons with 3- or 4-star status are included in the Baryon Summary Table. Due to insufficient data or uncertain interpretation, the other entries in the table are not established baryons. The names with masses are of baryons that decay strongly. The spin-parity J^P (when known) is given with each particle. For the strongly decaying particles, the J^P values are considered to be part of the names.

ρ	$1/2^+$	****	$\Delta(1232)$	$3/2^+$	****	Σ^+	$1/2^+$	****	Ξ^0	$1/2^+$	****	Λ_c^+	$1/2^+$	****
n	$1/2^+$	****	$\Delta(1600)$	$3/2^+$	***	Σ^0	$1/2^+$	****	Ξ^-	$1/2^+$	****	$\Lambda_c(2595)^+$	$1/2^-$	***
$N(1440)$	$1/2^+$	****	$\Delta(1620)$	$1/2^-$	****	Σ^-	$1/2^+$	****	$\Xi(1530)$	$3/2^+$	****	$\Lambda_c(2625)^+$	$3/2^-$	***
$N(1520)$	$3/2^-$	****	$\Delta(1700)$	$3/2^-$	****	$\Sigma(1385)$	$3/2^+$	****	$\Xi(1620)$	*		$\Lambda_c(2765)^+$	*	
$N(1535)$	$1/2^-$	****	$\Delta(1750)$	$1/2^+$	*	$\Sigma(1480)$	*		$\Xi(1690)$	*		$\Lambda_c(2880)^+$	$5/2^+$	***
$N(1650)$	$1/2^-$	****	$\Delta(1900)$	$1/2^-$	**	$\Sigma(1560)$	*		$\Xi(1820)$	$3/2^-$	***	$\Lambda_c(2940)^+$	*	
$N(1675)$	$5/2^-$	****	$\Delta(1905)$	$5/2^+$	****	$\Sigma(1580)$	$3/2^-$	*	$\Xi(1950)$	*		$\Sigma_c(2455)$	$1/2^+$	****
$N(1680)$	$5/2^+$	****	$\Delta(1910)$	$1/2^+$	****	$\Sigma(1620)$	$1/2^-$	*	$\Xi(2030)$	$\geq \frac{5}{2}^?$	***	$\Sigma_c(2520)$	$3/2^-$	****
$N(1685)$	*		$\Delta(1920)$	$3/2^+$	***	$\Sigma(1660)$	$1/2^+$	***	$\Xi(2120)$	*		$\Sigma_c(2800)$	***	
$N(1700)$	$3/2^-$	***	$\Delta(1930)$	$5/2^+$	***	$\Sigma(1670)$	$3/2^-$	****	$\Xi(2250)$	**		Ξ_c^+	$1/2^+$	***
$N(1710)$	$1/2^+$	***	$\Delta(1940)$	$3/2^-$	**	$\Sigma(1690)$	**		$\Xi(2370)$	**		Ξ_c^0	$1/2^+$	***
$N(1720)$	$3/2^+$	****	$\Delta(1950)$	$7/2^+$	****	$\Sigma(1730)$	$3/2^+$	*	$\Xi(2500)$	*		Ξ_c^0	$1/2^+$	***
$N(1860)$	$5/2^+$	**	$\Delta(2000)$	$5/2^+$	**	$\Sigma(1750)$	$1/2^-$	***				Ξ_c^0	$1/2^+$	***
$N(1875)$	$3/2^-$	***	$\Delta(2150)$	$1/2^-$	*	$\Sigma(1770)$	$1/2^+$	*	Ω^-	$3/2^+$	***	$\Xi_c(2645)$	$3/2^-$	***
$N(1880)$	$1/2^+$	**	$\Delta(2200)$	$7/2^-$	*	$\Sigma(1775)$	$5/2^-$	****	$\Omega(2250)^-$	***		$\Xi_c(2790)$	$1/2^-$	***
$N(1895)$	$1/2^-$	**	$\Delta(2300)$	$9/2^+$	**	$\Sigma(1840)$	$3/2^+$	*	$\Omega(2380)^-$	**		$\Xi_c(2815)$	$3/2^-$	***
$N(1900)$	$3/2^+$	***	$\Delta(2350)$	$5/2^-$	*	$\Sigma(1880)$	$1/2^+$	**	$\Omega(2470)$	**		$\Xi_c(2930)$	*	
$N(1990)$	$7/2^+$	**	$\Delta(2390)$	$7/2^+$	*	$\Sigma(1900)$	$1/2^-$	*				$\Xi_c(2980)$	***	
$N(2000)$	$5/2^+$	**	$\Delta(2400)$	$9/2^-$	**	$\Sigma(1915)$	$5/2^+$	****				$\Xi_c(3055)$	***	
$N(2040)$	$3/2^+$	*	$\Delta(2420)$	$11/2^+$	****	$\Sigma(1940)$	$3/2^+$	*				$\Xi_c(3080)$	***	
$N(2060)$	$5/2^-$	**	$\Delta(2750)$	$13/2^-$	**	$\Sigma(1940)$	$3/2^-$	***				$\Xi_c(3123)$	***	
$N(2100)$	$1/2^+$	*	$\Delta(2950)$	$15/2^+$	**	$\Sigma(2000)$	$1/2^-$	*				Ω_c^0	$1/2^+$	***
$N(2120)$	$3/2^-$	***				$\Sigma(2030)$	$7/2^+$	****				$\Omega_c(2770)^0$	$3/2^+$	***
$N(2190)$	$7/2^-$	****	Λ	$1/2^+$	****	$\Sigma(2070)$	$5/2^+$	***				Ξ_{cc}^+	*	
$N(2220)$	$9/2^+$	****	$\Lambda(1405)$	$1/2^-$	****	$\Sigma(2080)$	$3/2^+$	**						
$N(2250)$	$9/2^-$	****	$\Lambda(1520)$	$3/2^-$	****	$\Sigma(2100)$	$7/2^-$	*						
$N(2300)$	$1/2^+$	**	$\Lambda(1600)$	$1/2^+$	***	$\Sigma(2250)$	***							
$N(2570)$	$5/2^-$	**	$\Lambda(1670)$	$1/2^-$	****	$\Sigma(2455)$	***					Λ_b^0	$1/2^+$	***
$N(2600)$	$11/2^-$	***	$\Lambda(1690)$	$3/2^-$	****	$\Sigma(2620)$	**					$\Lambda_b(5912)^0$	$1/2^-$	***
$N(2700)$	$13/2^+$	**	$\Lambda(1710)$	$1/2^+$	*	$\Sigma(3000)$	*					$\Lambda_b(5920)^0$	$3/2^-$	***
			$\Lambda(1800)$	$1/2^-$	***	$\Sigma(3170)$	*					Σ_b	$1/2^+$	***
			$\Lambda(1810)$	$1/2^+$	***							Σ_b^-	$3/2^+$	***
			$\Lambda(1820)$	$5/2^+$	****							Ξ_b^0, Ξ_b^-	$1/2^+$	***
			$\Lambda(1830)$	$5/2^-$	****							$\Xi_b(5945)^0$	$3/2^+$	***
			$\Lambda(1890)$	$3/2^+$	****							Ω_b^-	$1/2^+$	***
			$\Lambda(2000)$	*										
			$\Lambda(2020)$	$7/2^+$	*									
			$\Lambda(2050)$	$3/2^-$	*									
			$\Lambda(2100)$	$7/2^-$	****									
			$\Lambda(2110)$	$5/2^+$	**									
			$\Lambda(2325)$	$3/2^-$	*									
			$\Lambda(2350)$	$9/2^+$	***									
			$\Lambda(2585)$	**										

**** Existence is certain, and properties are at least fairly well explored.

*** Existence ranges from very likely to certain, but further confirmation is desirable and/or quantum numbers, branching fractions, etc. are not well determined.

** Evidence of existence is only fair.

* Evidence of existence is poor.

Let's pause and discuss the PDG a bit here. Who knows anything about the PDG?

Quarks are **confined** to hadrons, and cannot be observed as bare objects. In other words, they are **social beasts**, and don't like to exist on their own. We'll discuss them more later on

What about Pauli exclusion principle?

sss hadron (Ω^-)
 should violate Pauli
 exclusion principle
 (multiple times!)
 There needs to be
 some fundamental
 difference between
 the quarks for this to
 be allowed: QCD
 color charge (beware
 comparisons to real
 “color”)

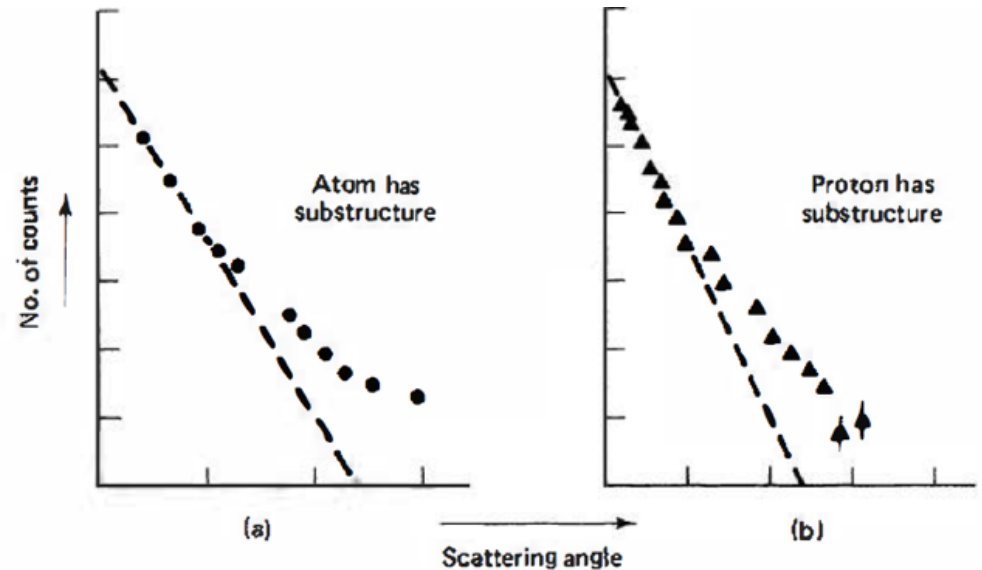


Fig. 1.11 (a) In Rutherford scattering, the number of particles deflected through large angles indicates that the atom has internal structure (a nucleus). (b) In deep inelastic scattering, the number of particles deflected through large angles indicates that the proton has internal structure (quarks). The dashed lines show what you would expect

if the positive charge were uniformly distributed over the volume of (a) the atom, (b) the proton. (Source: Halzen, F. and Martin, A. D. (1984) *Quarks and Leptons*, John Wiley & Sons, New York, p. 17. Copyright © John Wiley & Sons, Inc. Reprinted by permission.)

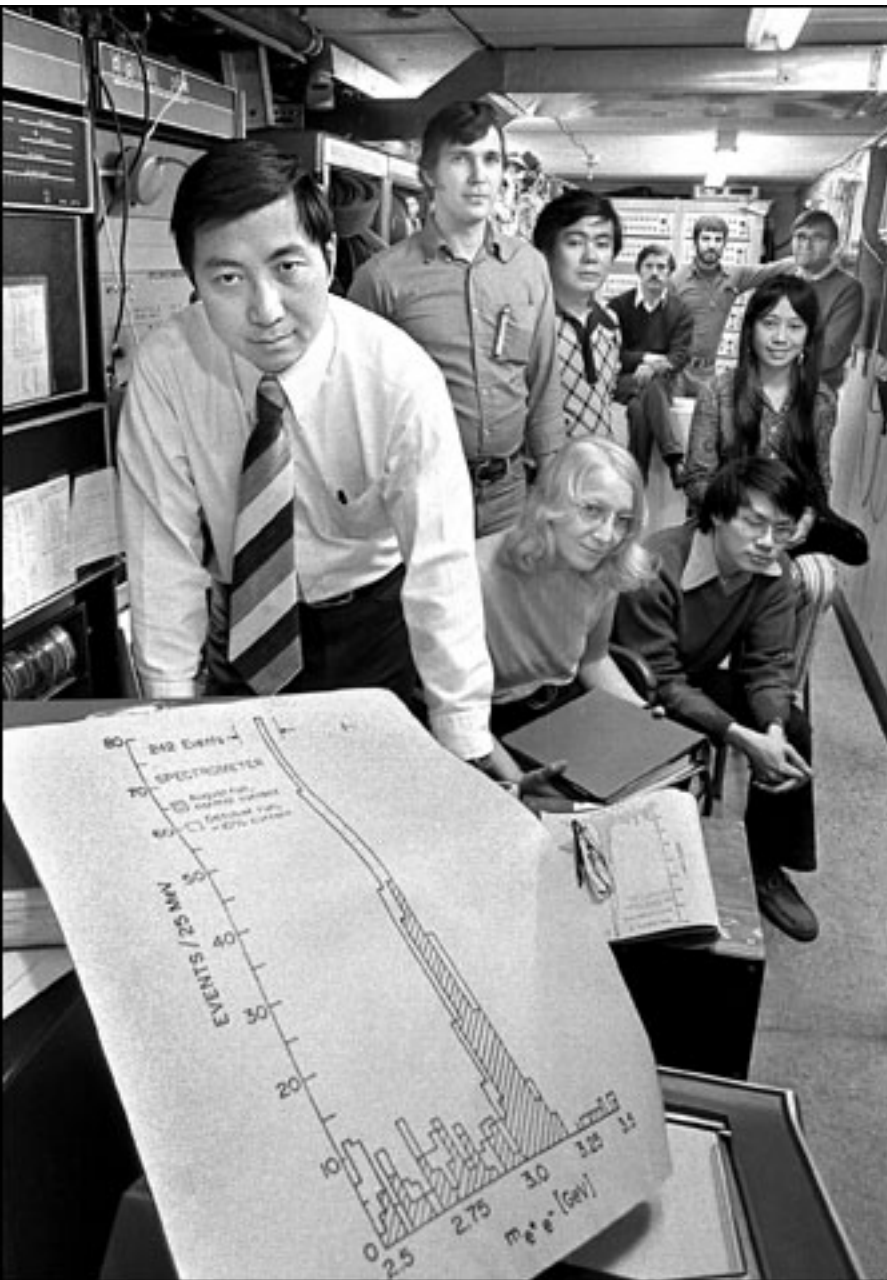
Colorless objects only:
 Explains why we don't
 have qq (or q) final states

November 1974, ψ meson discovered at SLAC, J meson at Brookhaven. Hence the name J/ψ , a new, electrically neutral particle with a long lifetime. Began the “November revolution”



¡Viva la Revolución!

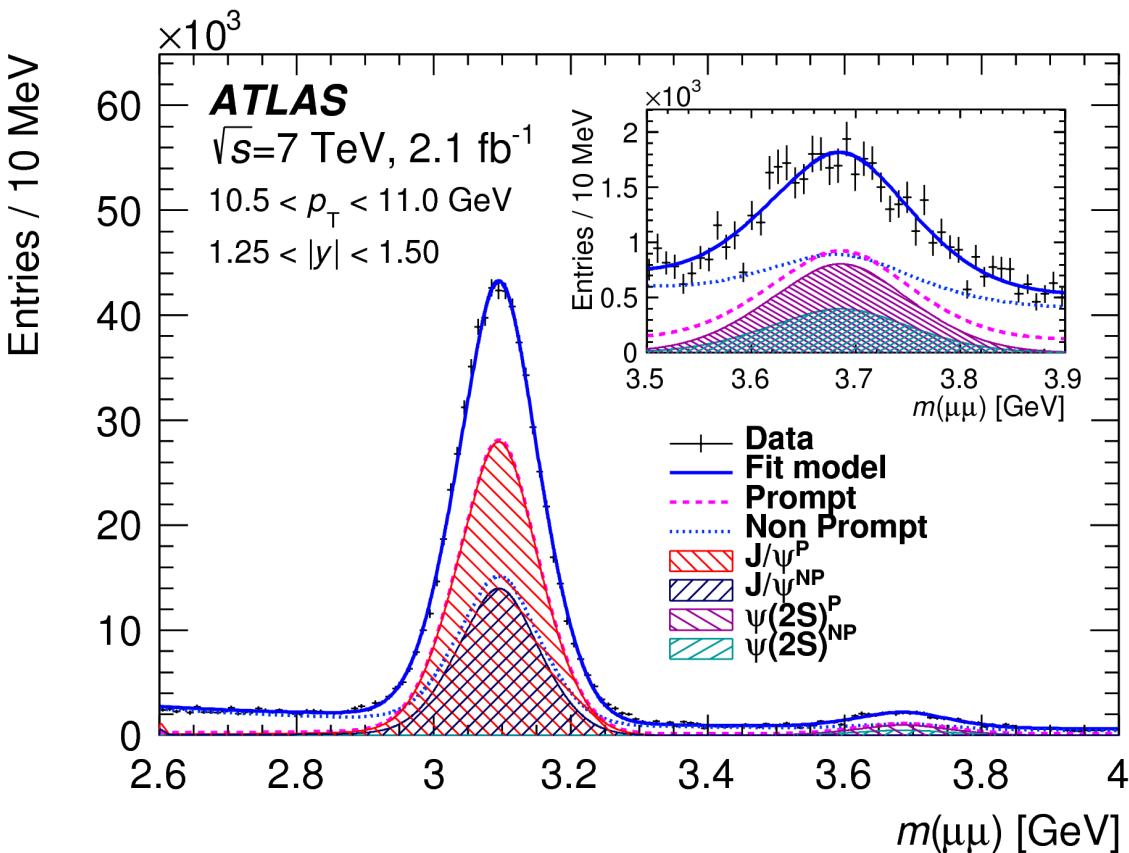
How was it discovered?



https://www.bnl.gov/bnlweb/history/nobel/nobel_76.asp

Sam Ting and his team, showing a plot of mass of e^+e^- pairs. As we will see shortly, the mass of objects is an invariant even after decay, so we see a bump at 3.1 GeV = J/ψ mass

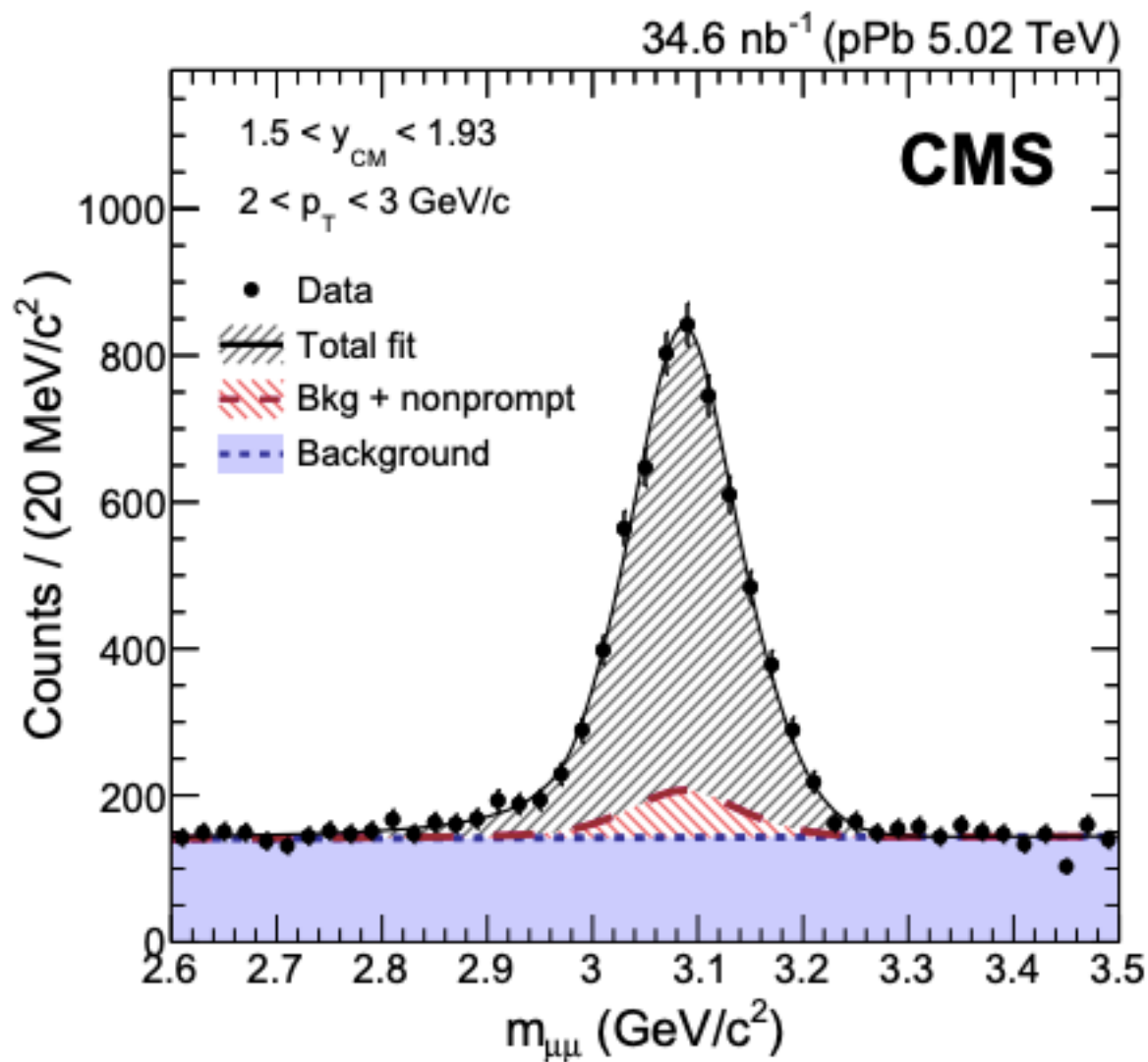
And these days



We know that
the J/ψ is a
charm-
anticharm
bound state
with spin = 1

This is a tiny fraction of the
data available to ATLAS and CMS, and
a large fraction of the J/ψ that we
produced are not even recorded

arXiv: 1612.02950



Proton-lead
collisions!

arXiv: 1702.01462

Add in the third generation

Table I. From Perl (1975). A table of 2-charged-particle events collected at 4.8 GeV in the Mark I detector. The table, containing 24 $e\mu$ events with zero total charge and no photons, was the strongest evidence at that time for the τ . The caption read:

“Distribution of 513, 4.8 GeV, 2-prong, events which meet the criteria:
 $p_e > 0.65 \text{ GeV}/c$, $p_\mu > 0.65 \text{ GeV}/c$, $\theta_{copl} > 20^\circ$.”

Number photons =	Total Charge = 0			Total Charge = ± 2		
	0	1	> 1	0	1	> 1
cc	40	111	55	0	1	0
$e\mu$	24	8	8	0	0	3
$\mu\mu$	16	15	6	0	0	0
eh	18	23	32	2	3	3
μh	15	16	31	4	0	5
hh	13	11	30	10	4	6
Sum	126	184	162	16	8	17

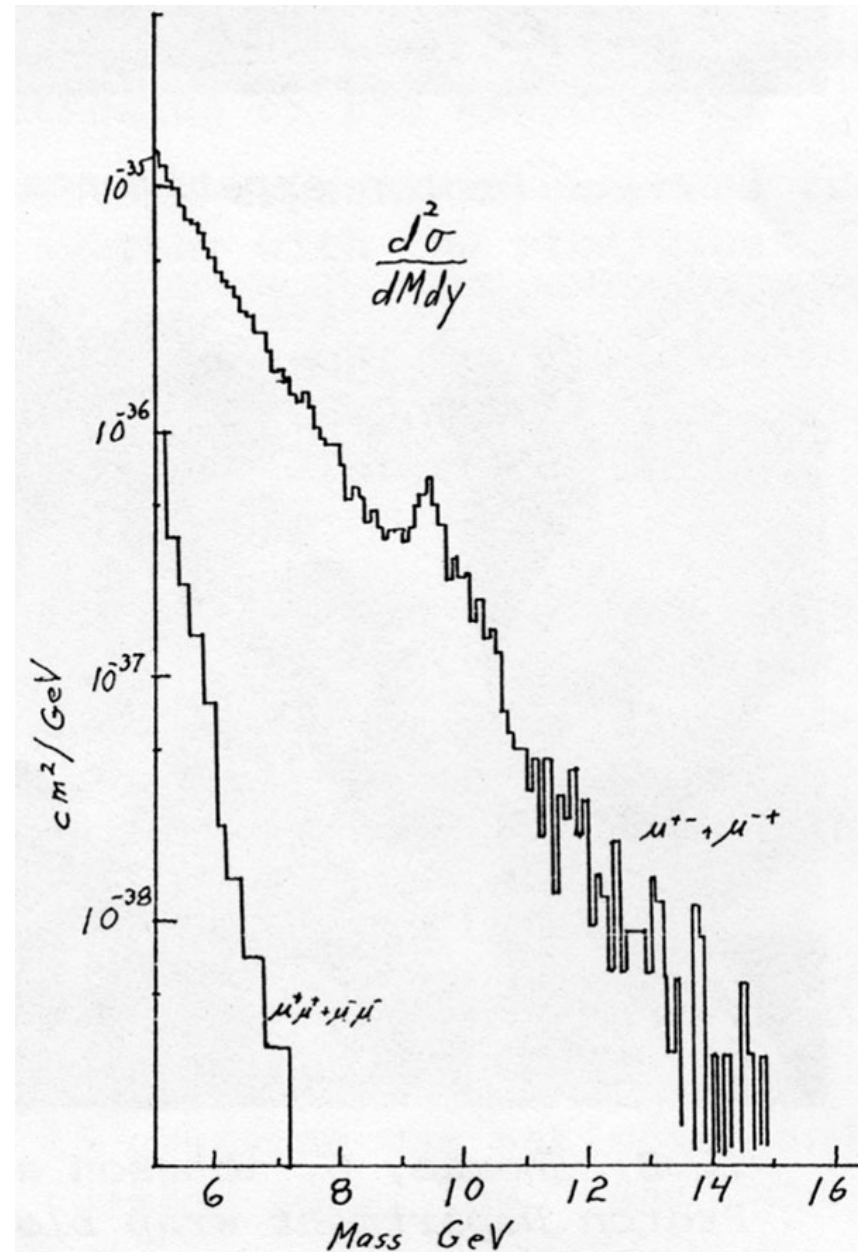


Martin Perl (1975) discovery of
 tau lepton (tau neutrino not until 2000!)

Add in the third generation

Lederman and E288
collaborators - discovery of
the bottom quark at nearby
Fermilab:

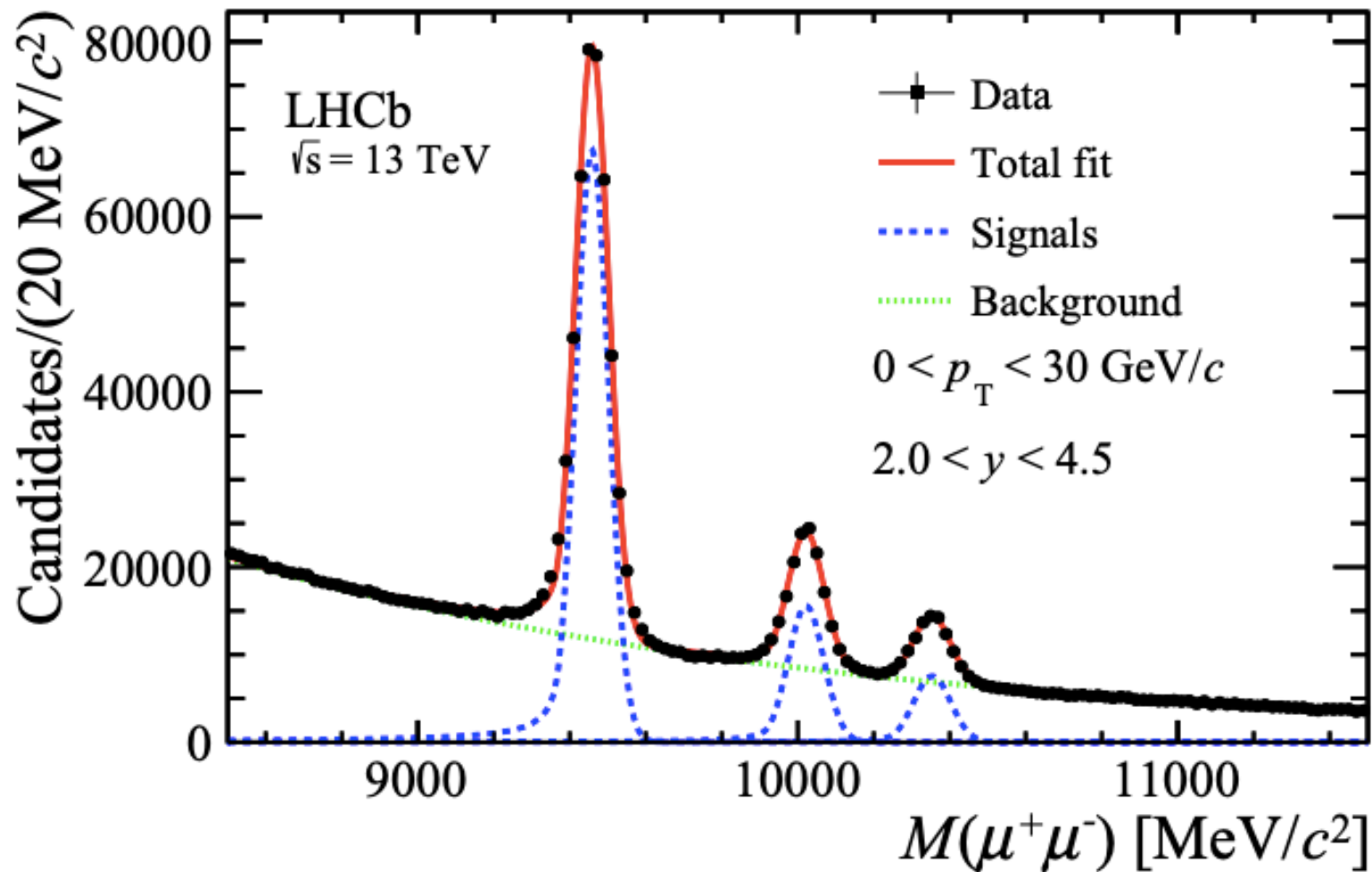
$$\Upsilon = b\bar{b}$$



Lots of upsilons everywhere, too

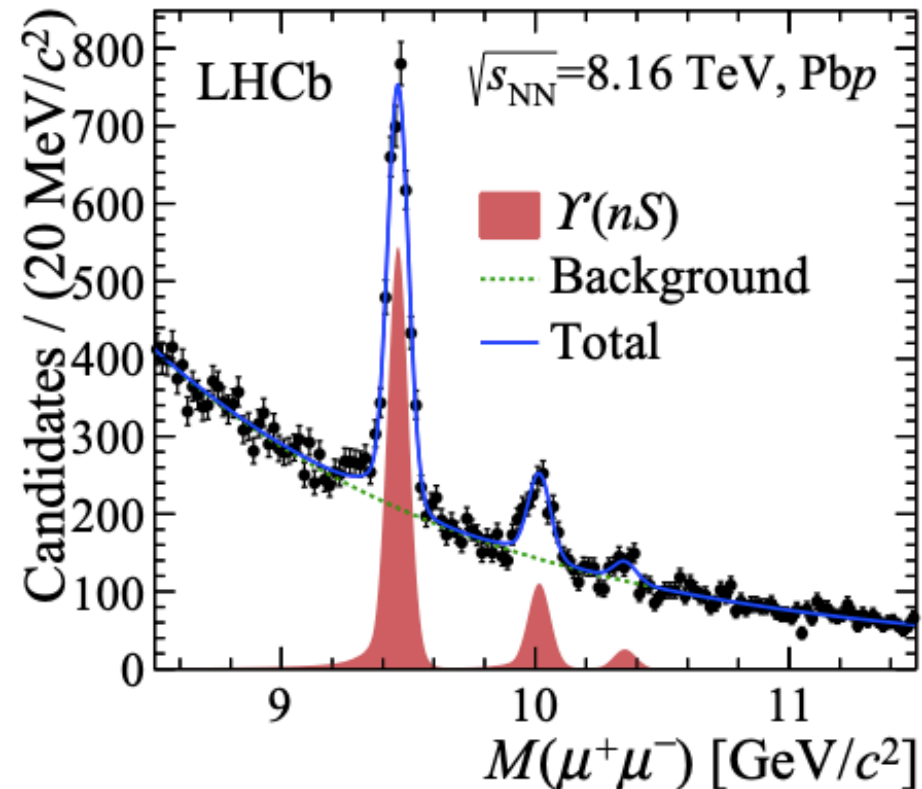
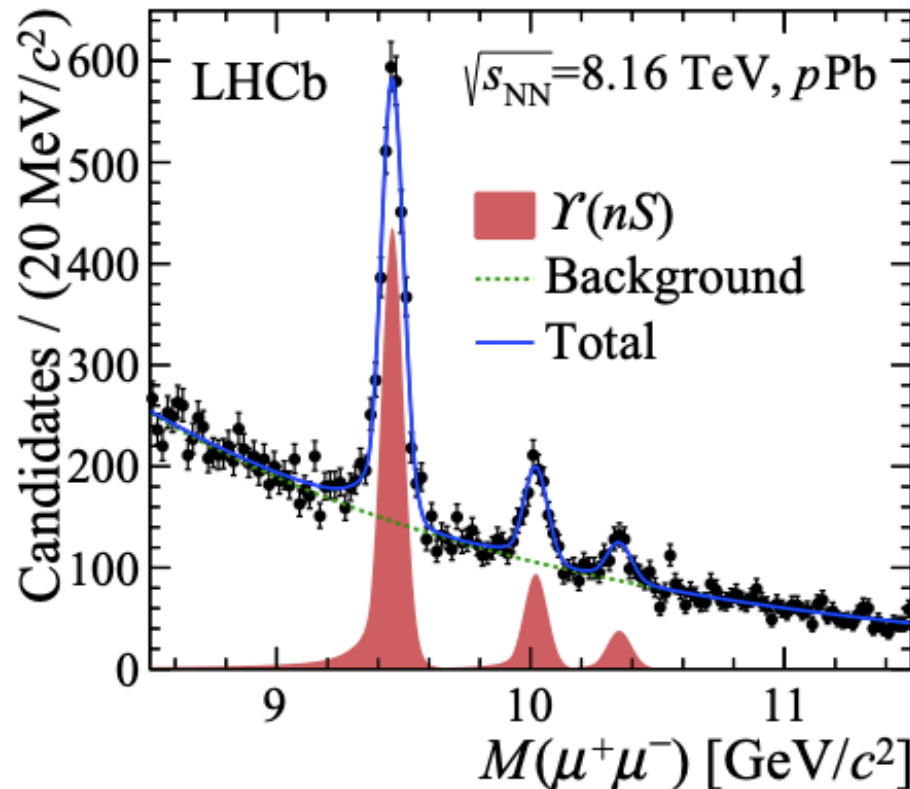
arXiv: 1804.09214

We'll talk about the 3 signal peaks
in a few chapters!

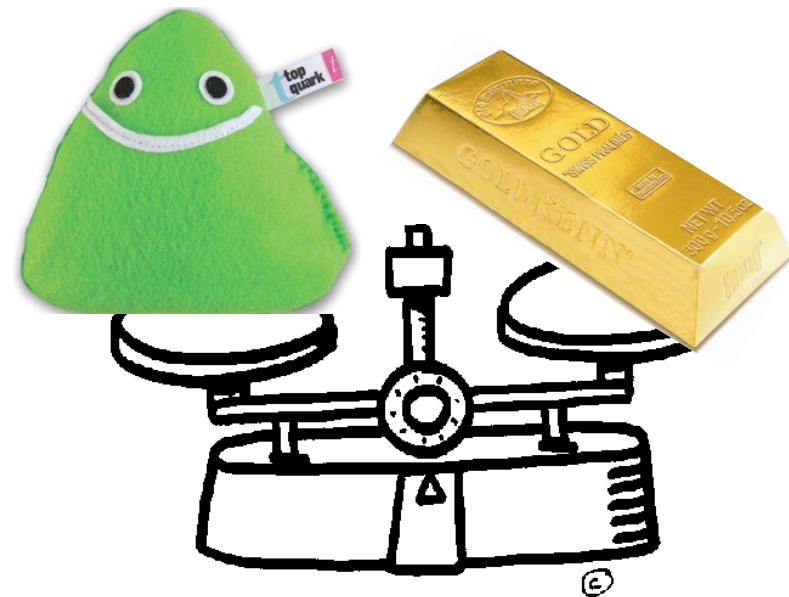


LHCb-PAPER-2018-035

LHCb is an asymmetric detector (any guesses why?). Difference between the two is which beams moves toward the detector at the interaction region



Announced jointly
1994-1995 by DZero and
CDF (at Fermilab) in
proton-antiproton collisions,
but top quarks decay so
quickly that they do not
form stable/metastable
bound states. Mass of top
quark ~ 173 GeV!

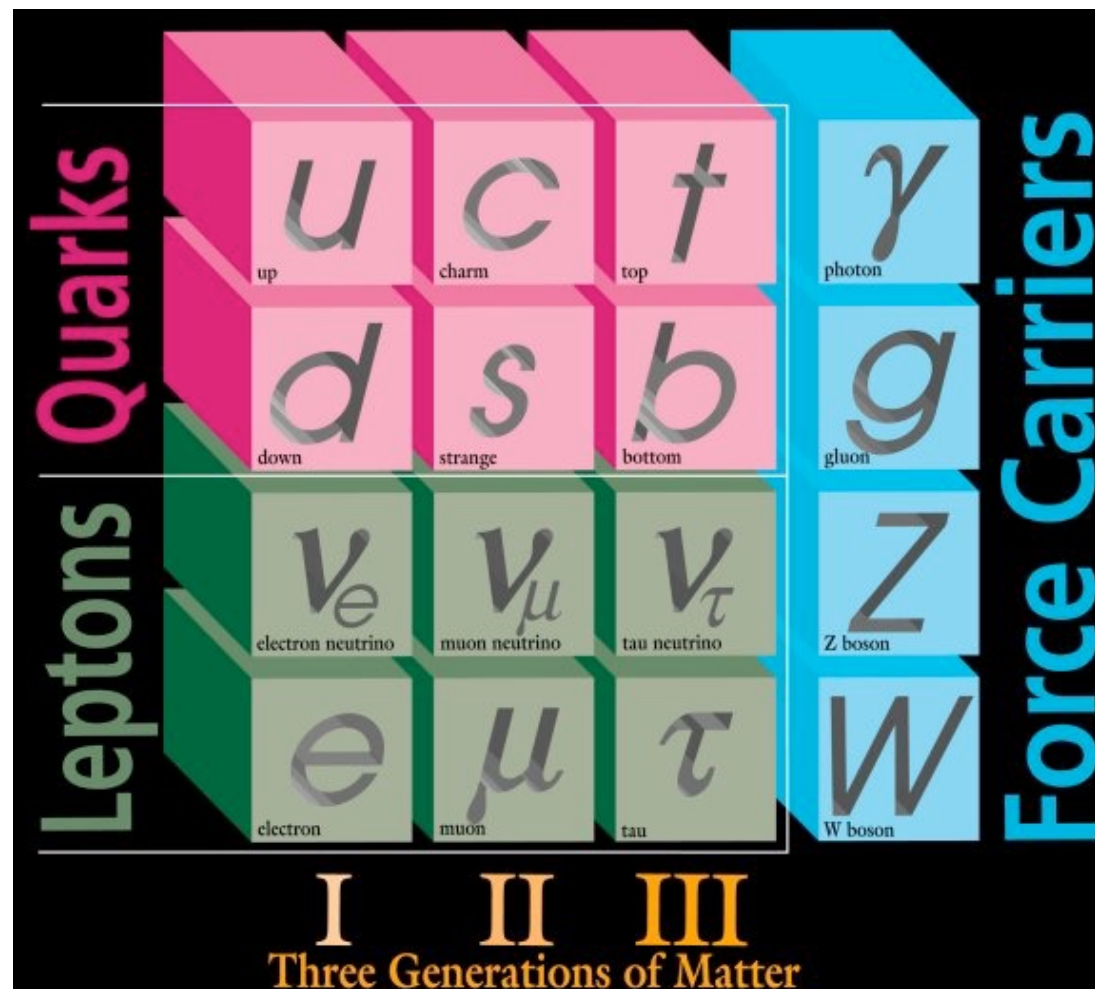


Fun aside: UA1 at
CERN made a
“discovery” of the
top quark in 1984
with a mass of
 40 ± 10 GeV

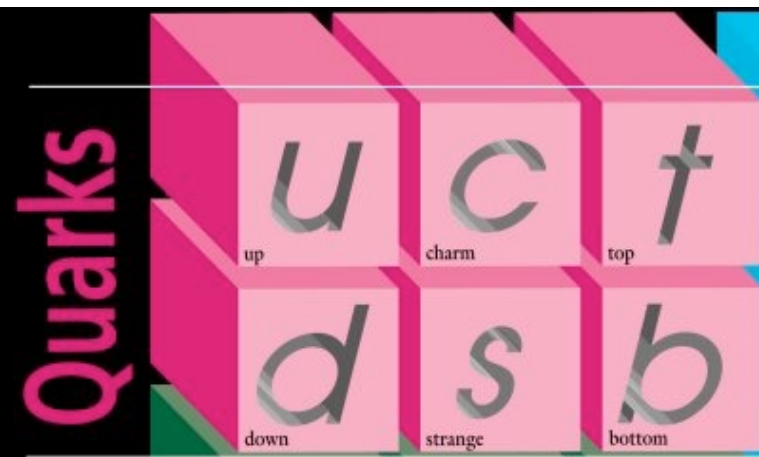
Putting it all together, aka the Standard Model (SM)

Fermions

Bosons



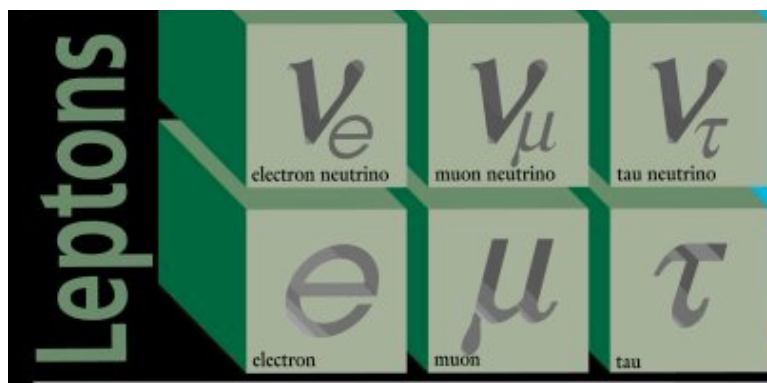
This is really the full Standard Model (modulo the Higgs boson, h), though it of course ... hides some details



Three generations of quarks, with each generation getting more massive. Each quark carries electric charge ($+2/3, -1/3$), and also QCD color (**rgb**). Quarks are confined, and do not exist alone in nature, but rather only in **hadrons**: **baryons** and **mesons**. Quarks also contain “**flavor**” (strangeness, topness, etc) that is conserved in QCD, but not in weak interactions. **Anti-quarks** not shown

Are there additional generations of quarks? We've been looking for them

The leptons

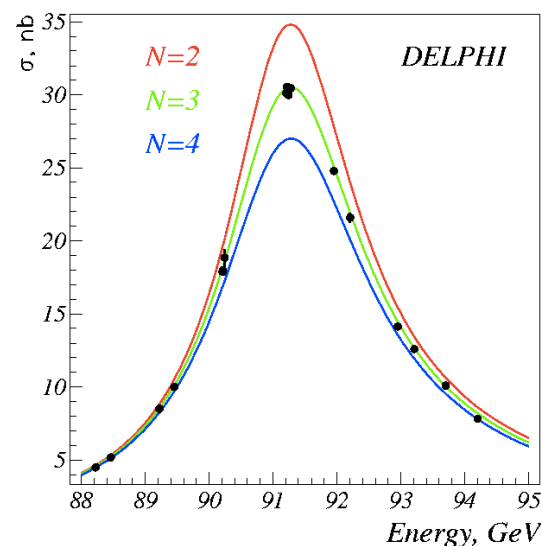


Are there additional leptons? We've been looking for them, though, though extra neutrinos have to be very massive or rarely interact. Masses of observed neutrinos unknown, but are very small

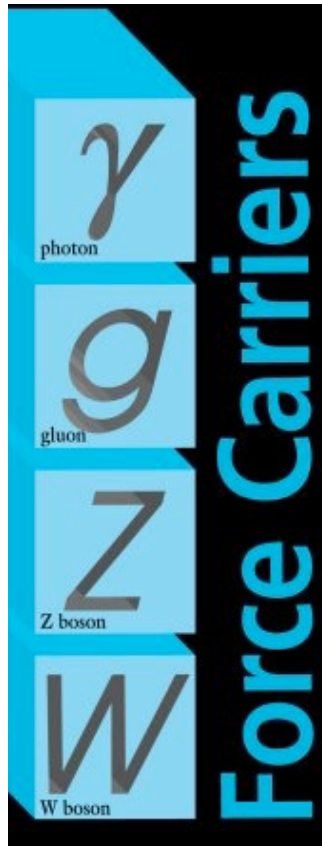
Three generations of **leptons**, with each generation (at least of charged leptons) getting more massive. Charged leptons carry electric charge, neutrinos do not. All leptons carry electron, muon and tau number, which is conserved.

Anti-particles not shown

Study number of light neutrinos with Z production at e^+e^- machines

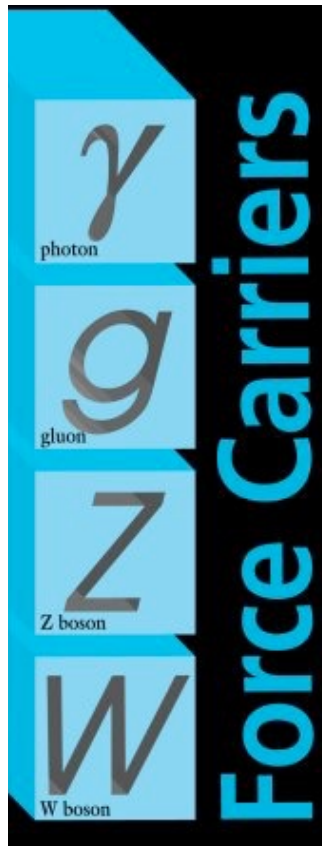


Photon never changes matter flavor

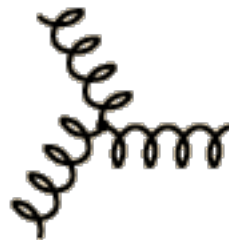


Force carriers are bosons with integer spin. The **photon** is the force carrier from E&M, and has spin-1 (it's a vector boson) and zero mass. Interacts only with electrically charged particles

Gluon never changes matter flavor



The **gluon** is the force carrier of QCD, and has spin 1 (it's a vector boson) and zero mass. It has no electric charge, but it carries **QCD color charge** (there are 8 types of gluons). Hence, it couples not only to quarks, but also to itself and other gluons (but not leptons)



The bosons



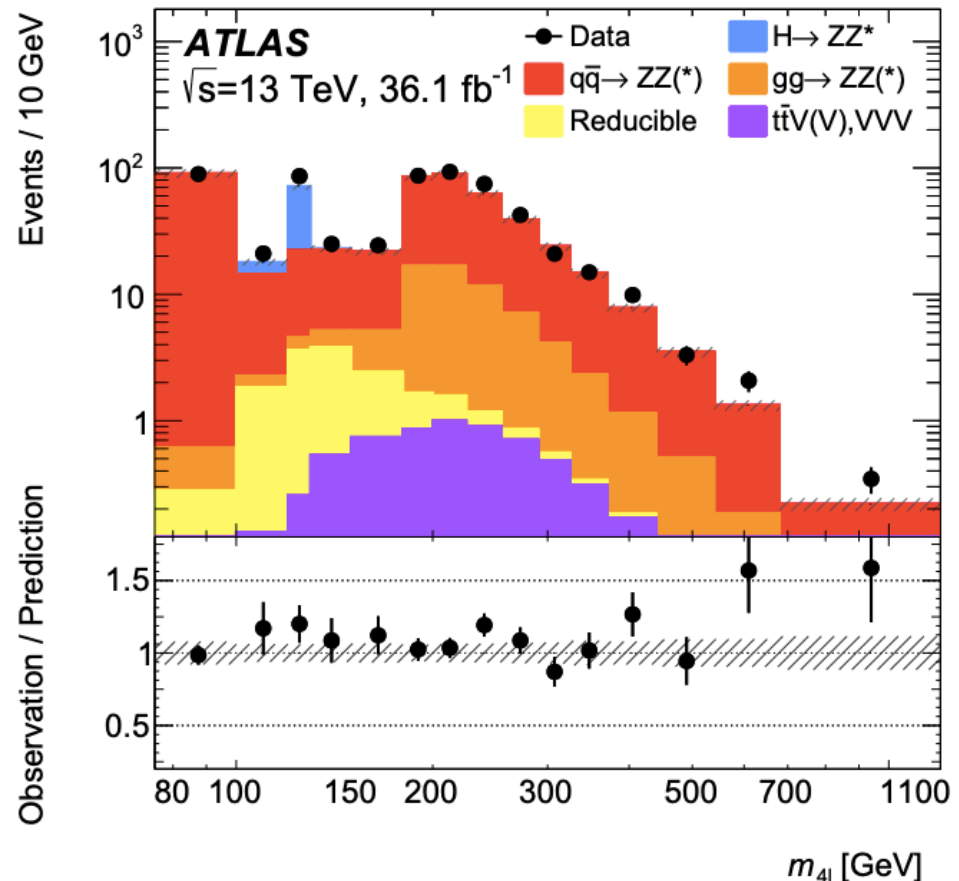
W bosons
always change
matter flavor,
Z bosons do not

The W^\pm and Z^0 bosons are the **weak force carriers**, with spin-1 (vector bosons) and both having large, non-zero mass ($W \sim 80$ GeV, $Z \sim 91$ GeV). The weak force is called exactly that due to their large mass. Weak force carriers are special - they are the only way to change one quark generation into another (see JPsi lifetime!), and have other special properties that we'll get to. Responsible for **nuclear β -decay and fusion**

The Higgs boson

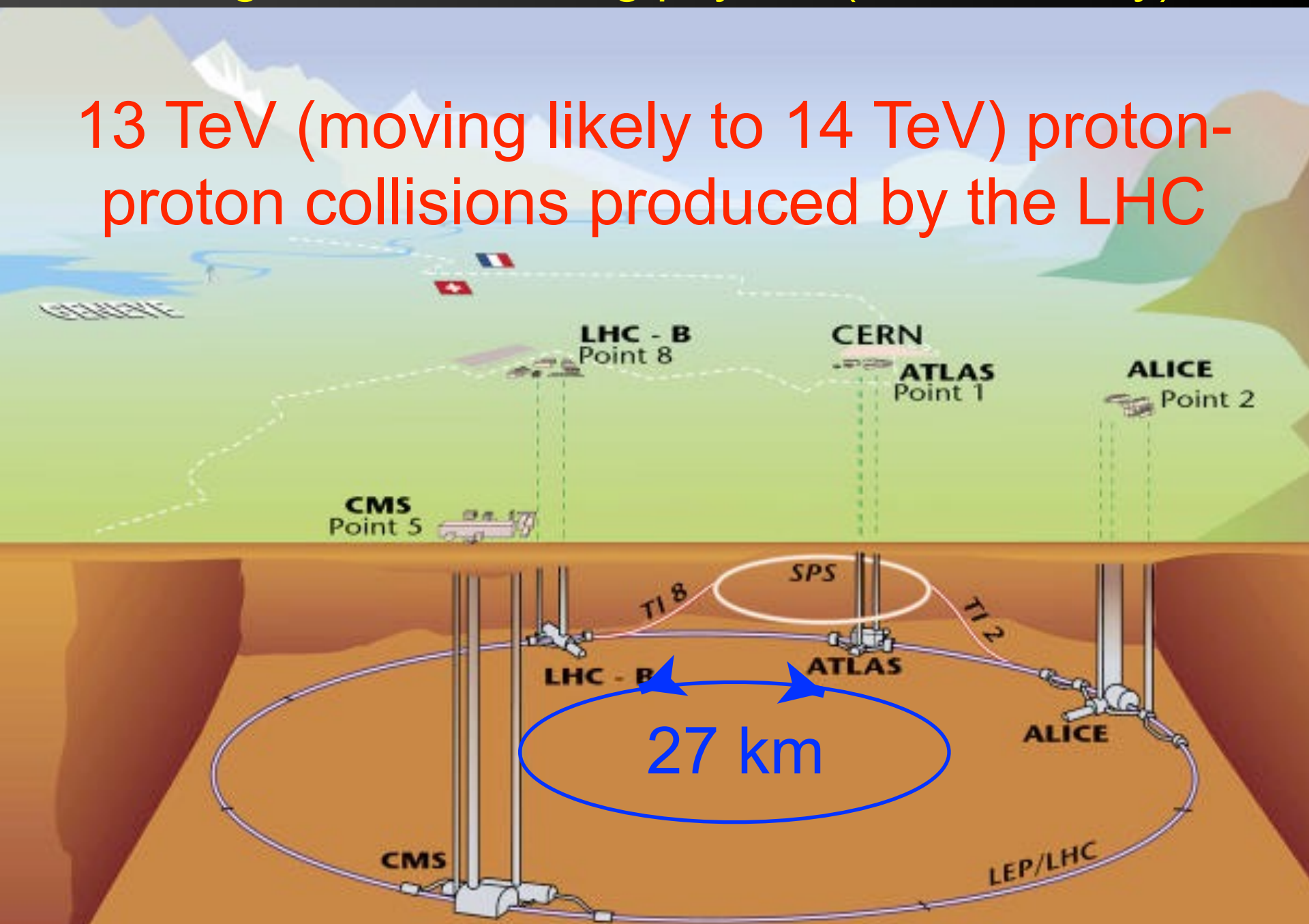
The Higgs boson (h) was hypothesized in 1960s, but was not discovered until July 2012. Long timeline! We'll see later in the course how the **Higgs mechanism** explains why the weak force carriers are so weak/massive, and why the fermions have mass

$m_H \sim 125 \text{ GeV}$

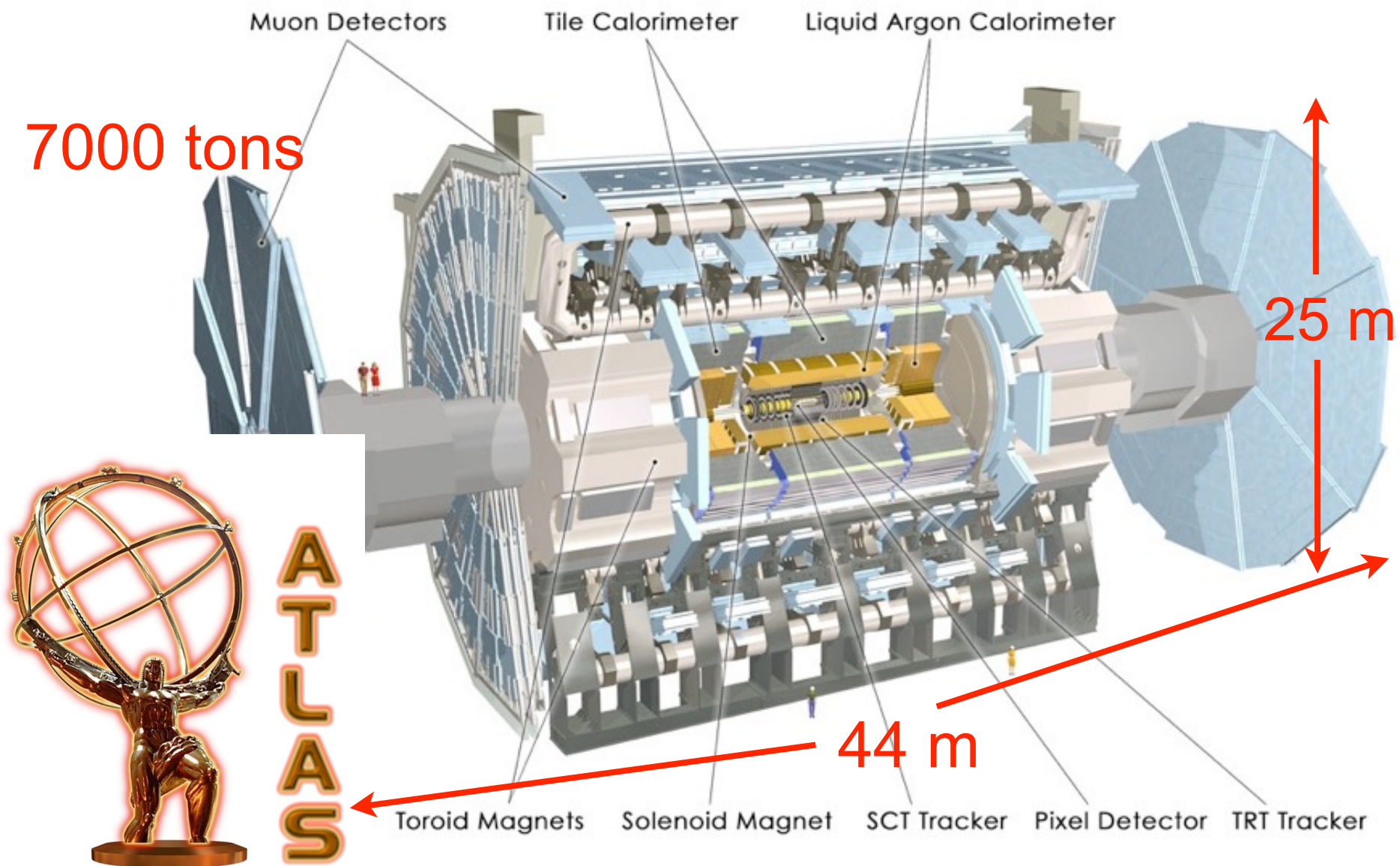


arXiv: 1902.05892

13 TeV (moving likely to 14 TeV) proton-proton collisions produced by the LHC



ATLAS (I can talk about my experiment for.. awhile)

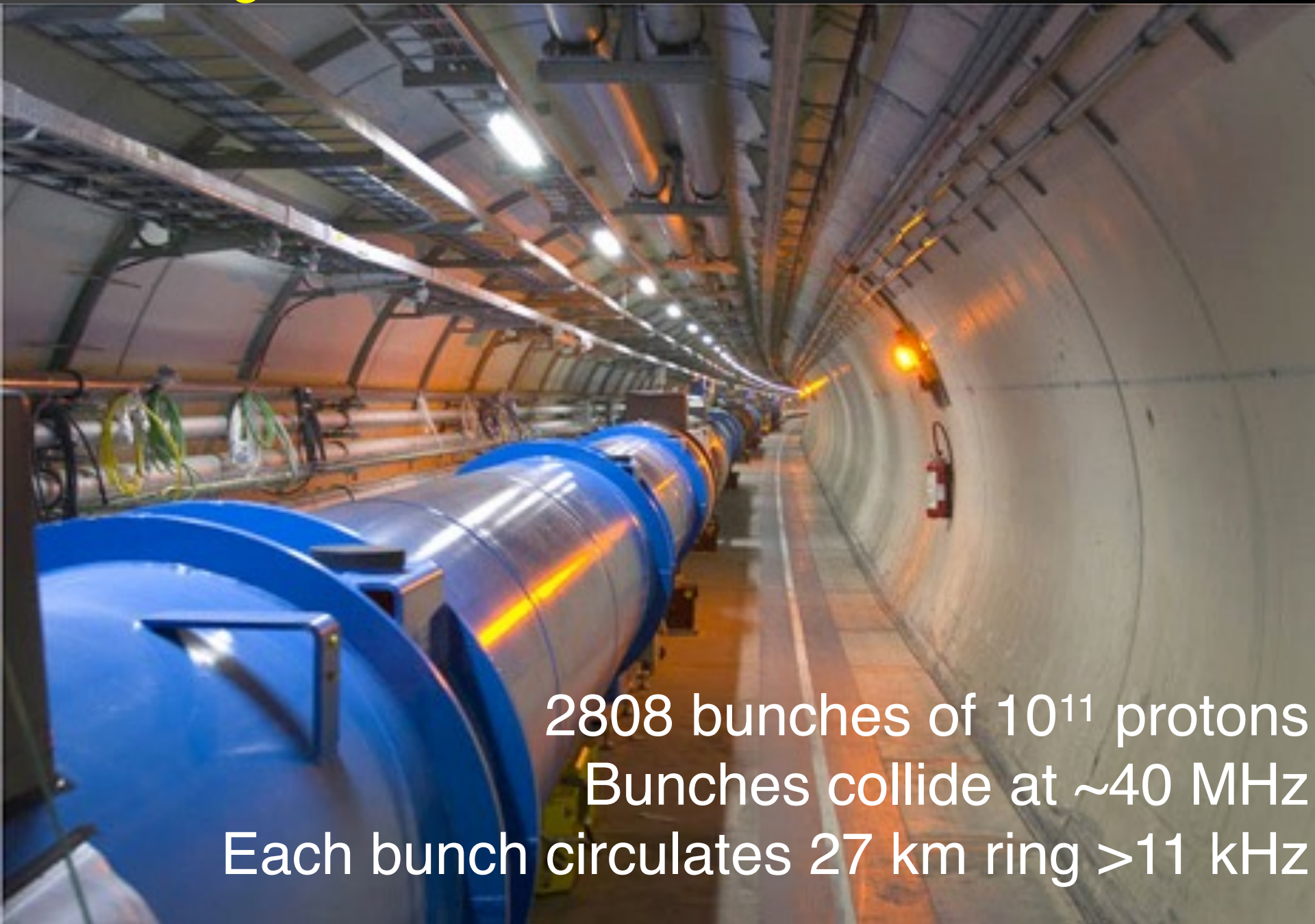




Trigger system: 40 MHz
reduced to ~ 1 kHz

1 GB of data recorded
every ~ 2 seconds





2808 bunches of 10^{11} protons
Bunches collide at ~ 40 MHz
Each bunch circulates 27 km ring > 11 kHz

Other sorts of modern experiments

g-2
mu2e
neutrino experiments (nuclear, solar, accelerator)
nuclear physics
astroparticle physics
dark matter searches
dark energy surveys
...

Not to mention all the accelerator physics
that goes along with much of the above

How do modern particle detectors work?

Want to see the effect of a particle, usually in the form of radiation or energy transfer that we can observe. **Goal is to infer as much about the original particle/object as possible.**

Problem is of course that we cannot just put things inside of a microscope for careful, lengthy study: **typically traveling close to speed of light**, **often very short-lived**, **occasionally produced with many other nearby objects**, **sometimes have no electric charge** and **can look like other, similar particles**

What can we take advantage of?

Charged particles bend in a magnetic field (can measure electric charge and momentum)

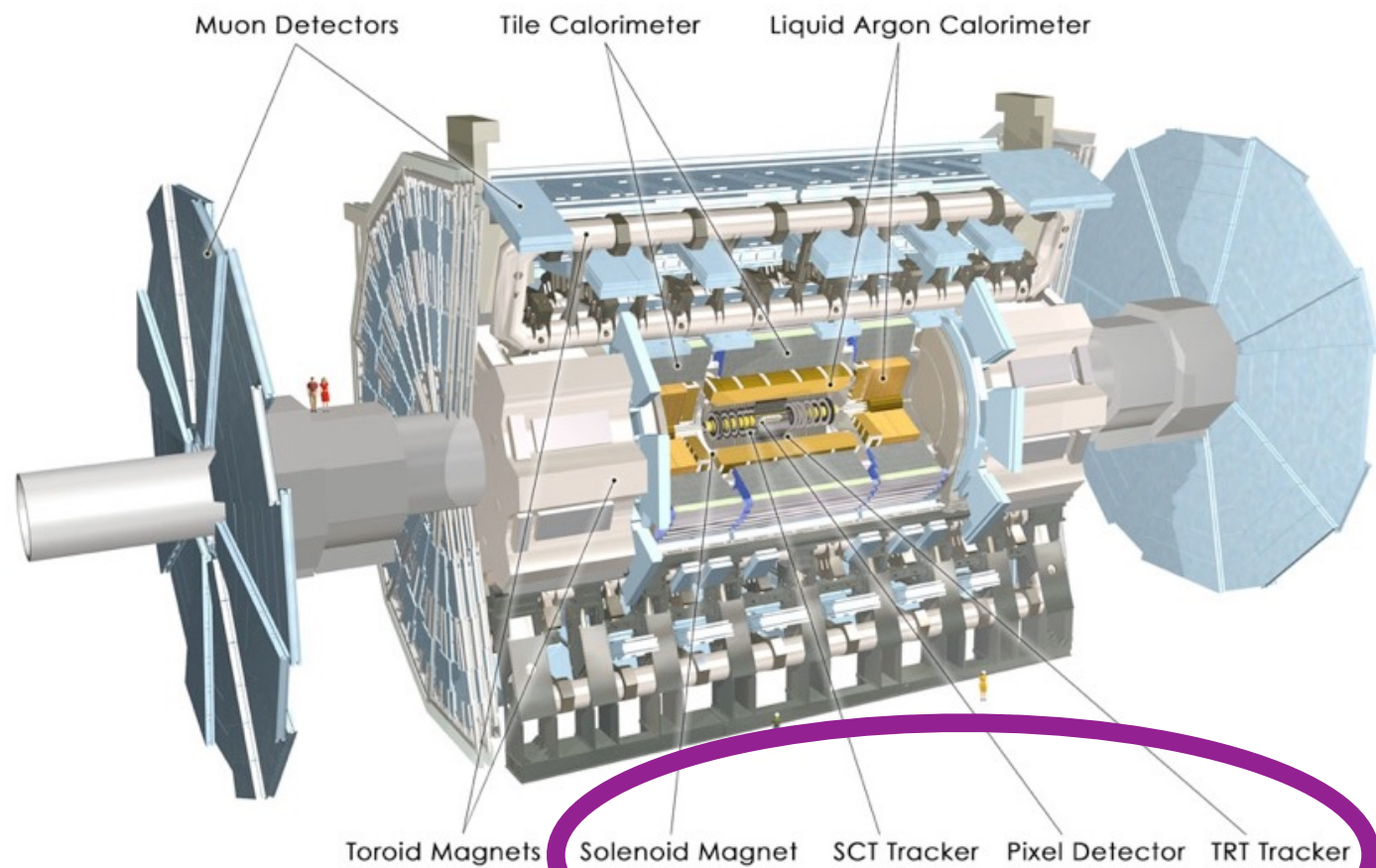
Careful timing measurements can give us particle velocity and other information (useful not only for the original particle, but also secondary particles it produce)

Calorimeter measurements give particle energy (different types of particles deposit energy electromagnetically vs via strong force, and at different rates)

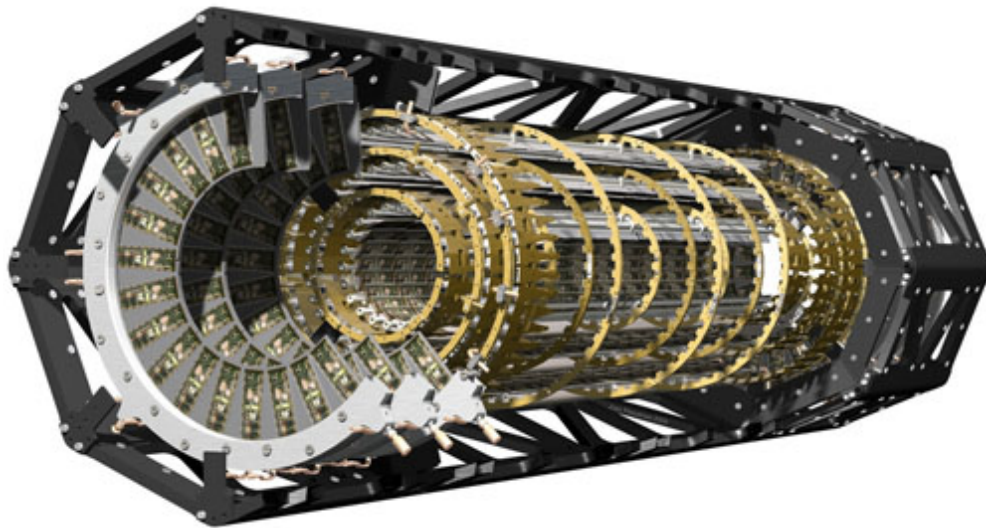
Neutrinos escape ~undetected, leading to imbalance of momentum in detector

Muons are highly penetrating and minimally ionizing

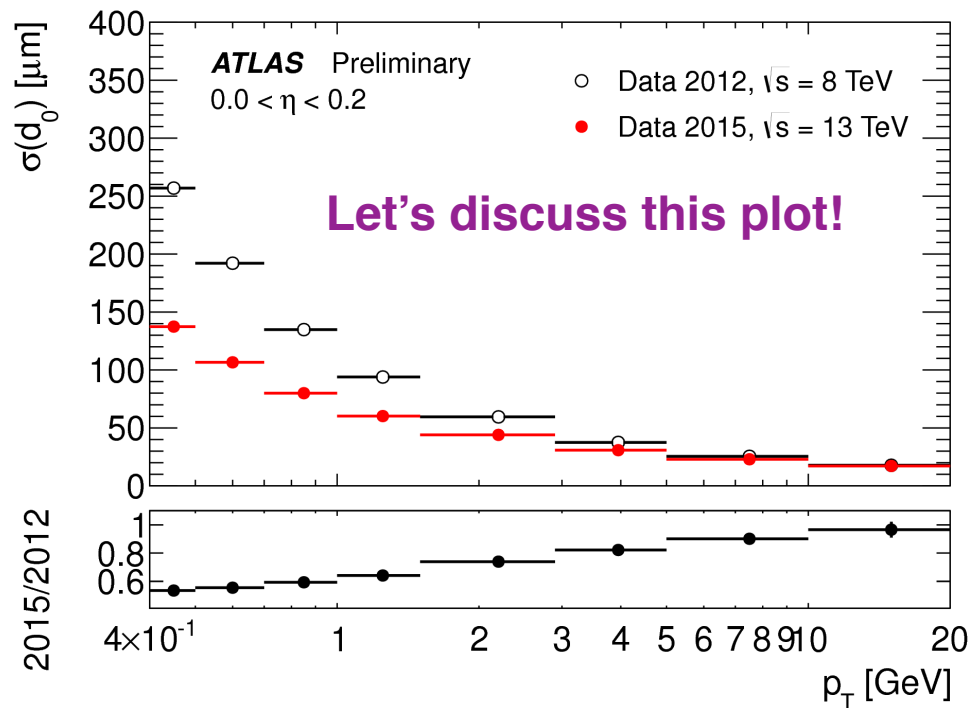
Other tricks like Cherenkov radiation, measurements of dE/dx , looking for transition radiation at material boundaries, ...



Inner tracking system nearest collision point immersed in 2T solenoid magnetic field: measure p and q



100 million readout channels (upgraded between the two data-taking years on the plot for an extra layer) to measure precise location of charged particle trajectory

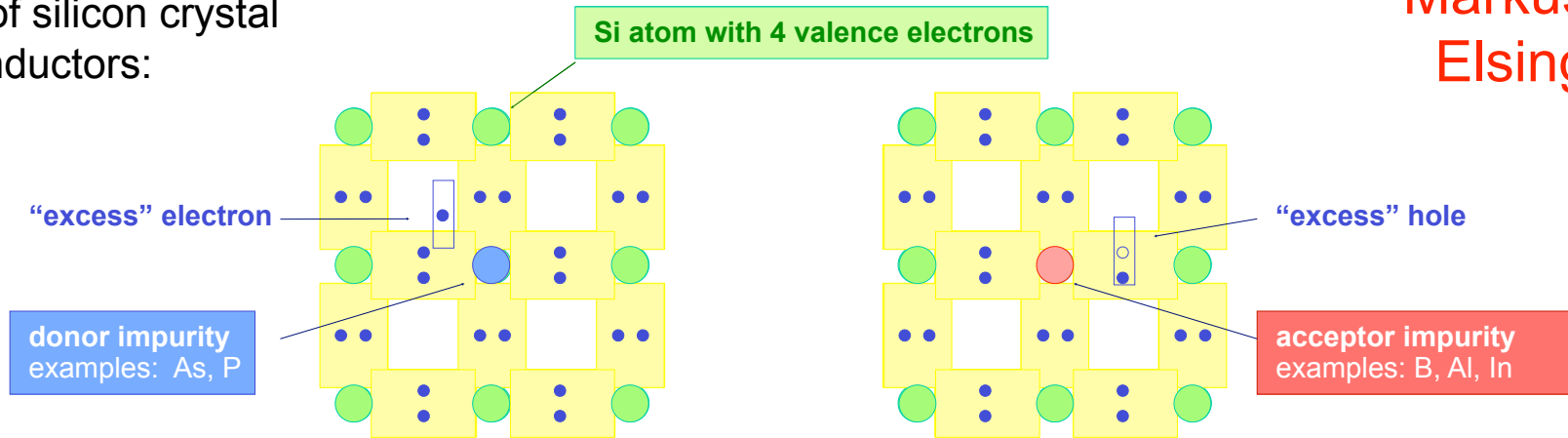


<https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/PLOTS/IDTR-2015-007/>

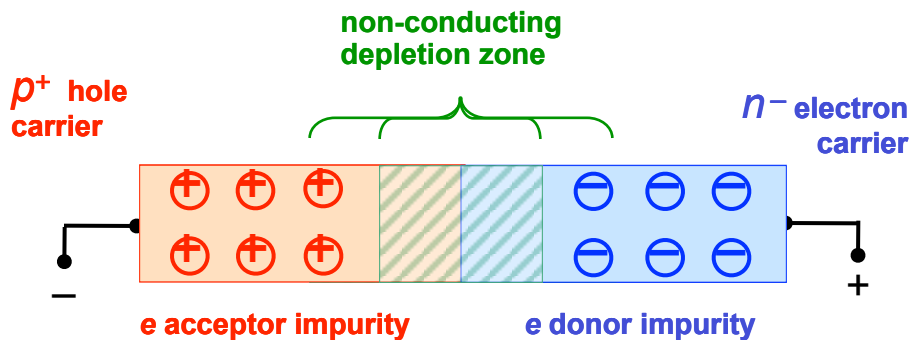
Semiconductors

Slide
from
Markus
Elsing

- doping of silicon crystal semiconductors:



p - n junction p - n junction

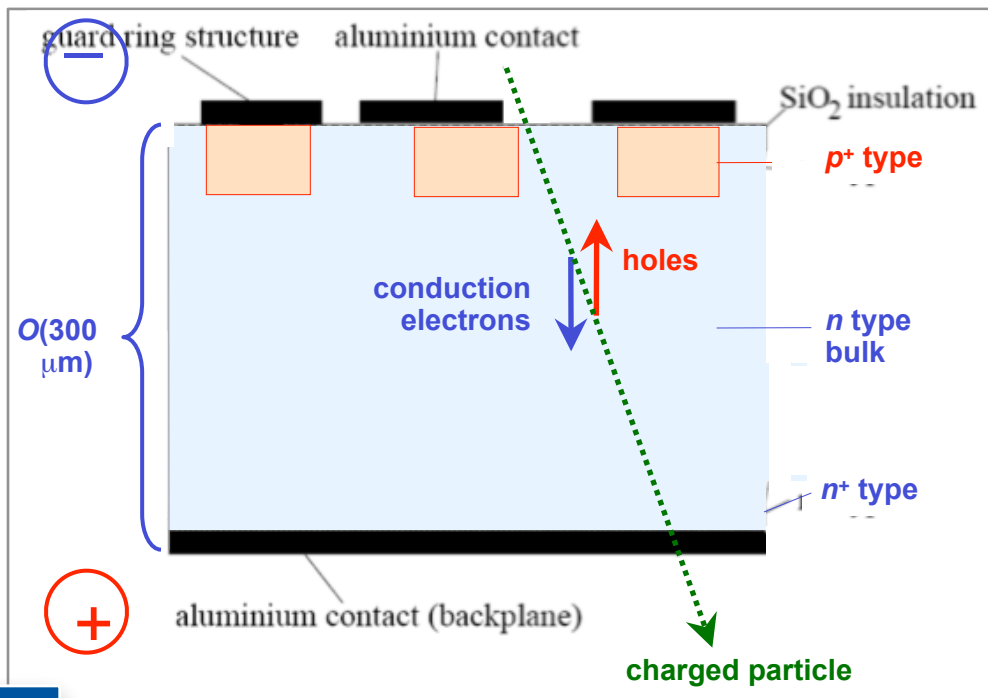


- the depletion zone, depletion zone, the potential barrier in the depletion zone, enhancing its resistance
- the potential barrier in the junction
- counter-weights the opposing potential

The p - n Junction as a Tracking Detector

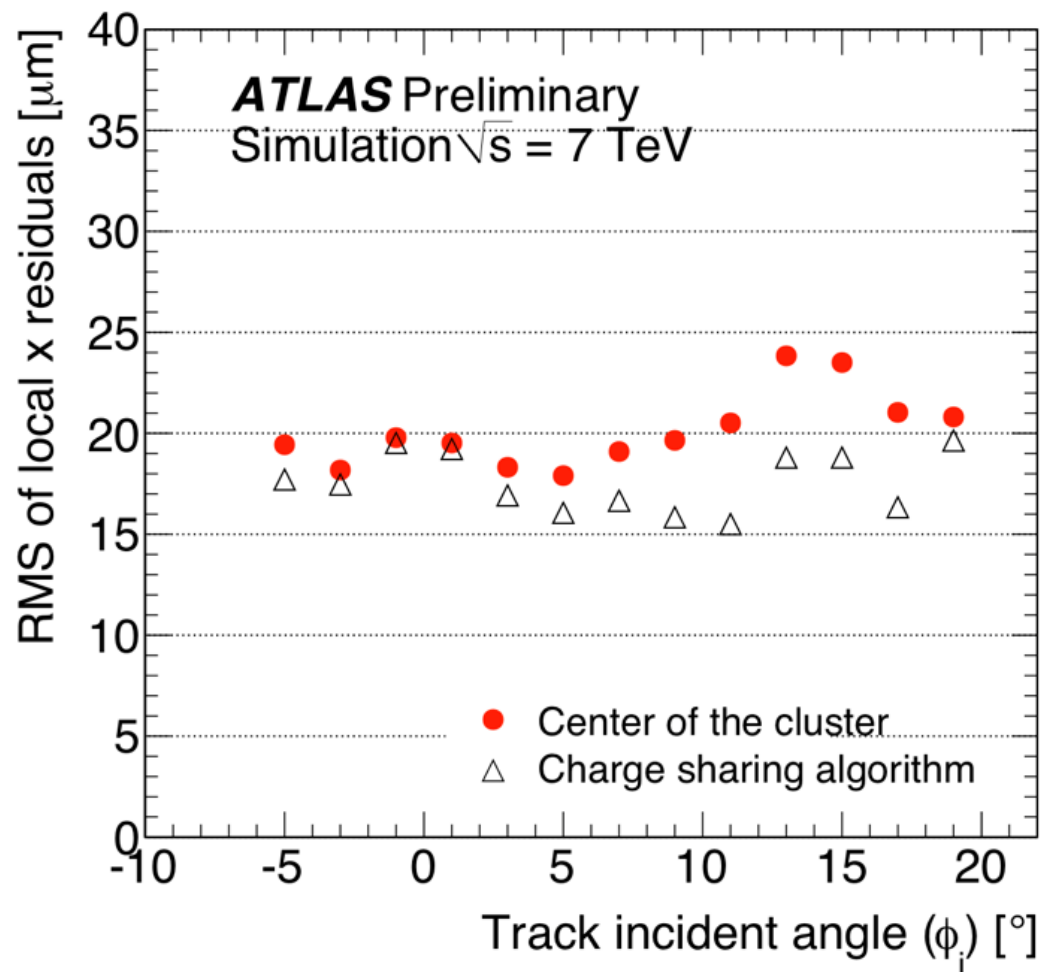
- thin ($\sim \mu\text{m}$), highly doped p^+ ($\sim 10^{19} \text{ cm}^{-3}$) layer on lightly doped n ($\sim 10^{12} \text{ cm}^{-3}$) substrate
- high mobility of charge carriers in Si allows fast charge collection ($\sim 5 \text{ ns}$ for electron)
- high Si density & low electron-hole creation potential (3.6 eV compared to $\sim 36 \text{ eV}$ for gaseous ionization) allows use of very thin detectors with reasonable signal

Slide
from
Markus
Elsing



schema of silicon microstrip sensor

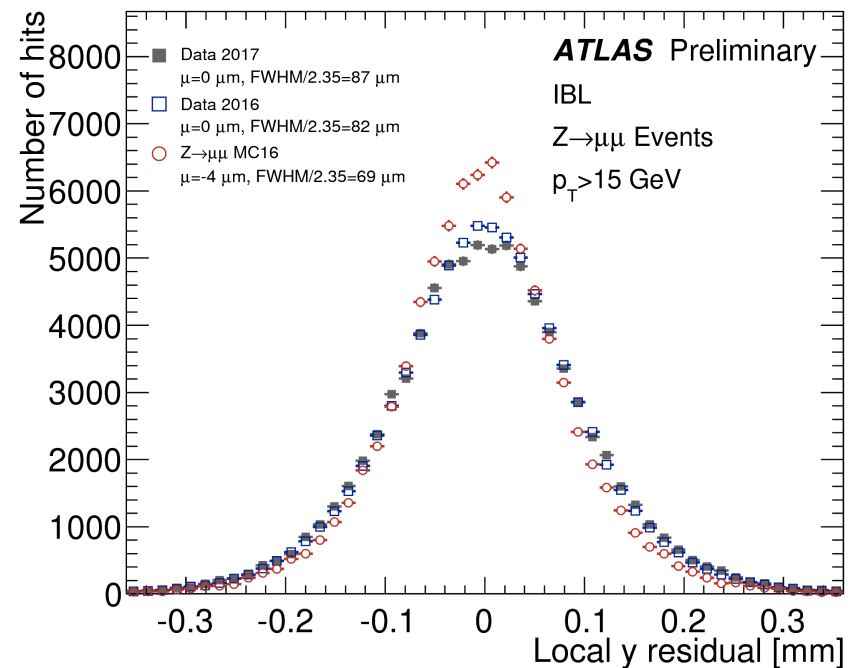
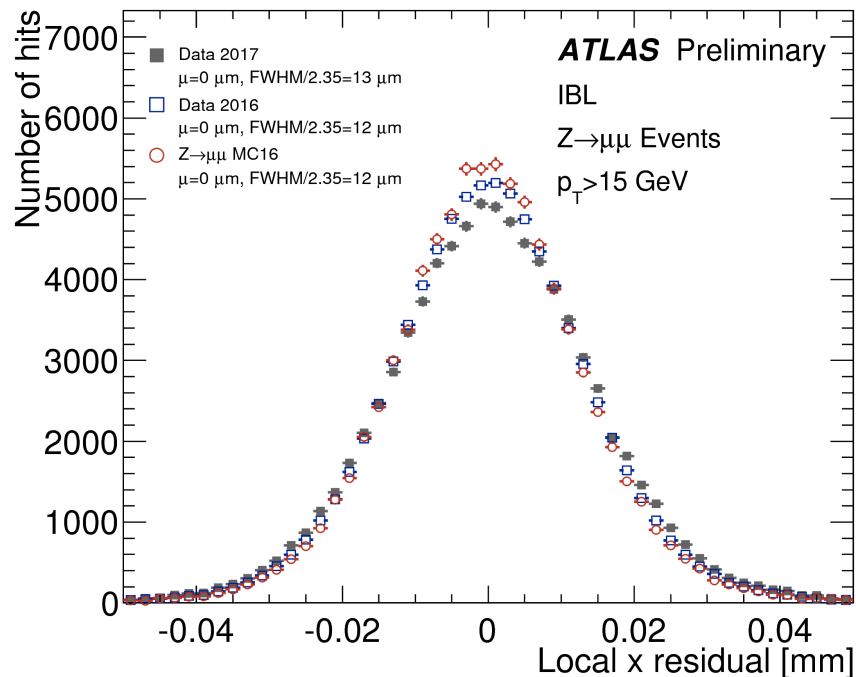
- reverse bias: backplane set to positive voltage ($< 500 \text{ V}$)
- a traversing charged particle ionizes silicon, creating conduction electrons and holes that induce a measurable current by drifting to electrodes
- metal-semiconductor transition forms charge (Schottky) barrier similar to p - n junction. Highly doped n^+ layer reduces width of potential barrier and hence resistance



Tens of micron resolution from single hits! The alignment for all the modules gets quite ... tricky

ATLAS IBL pixel system

<https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/PLOTS/IDTR-2017-004/>

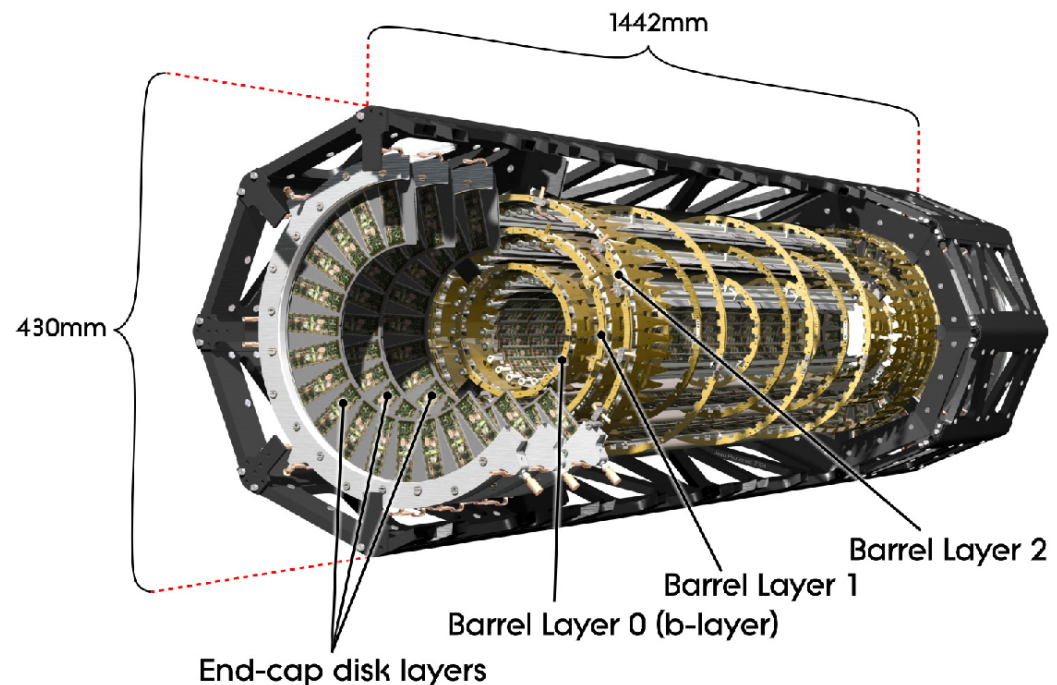


Let's look very carefully at
these plots together

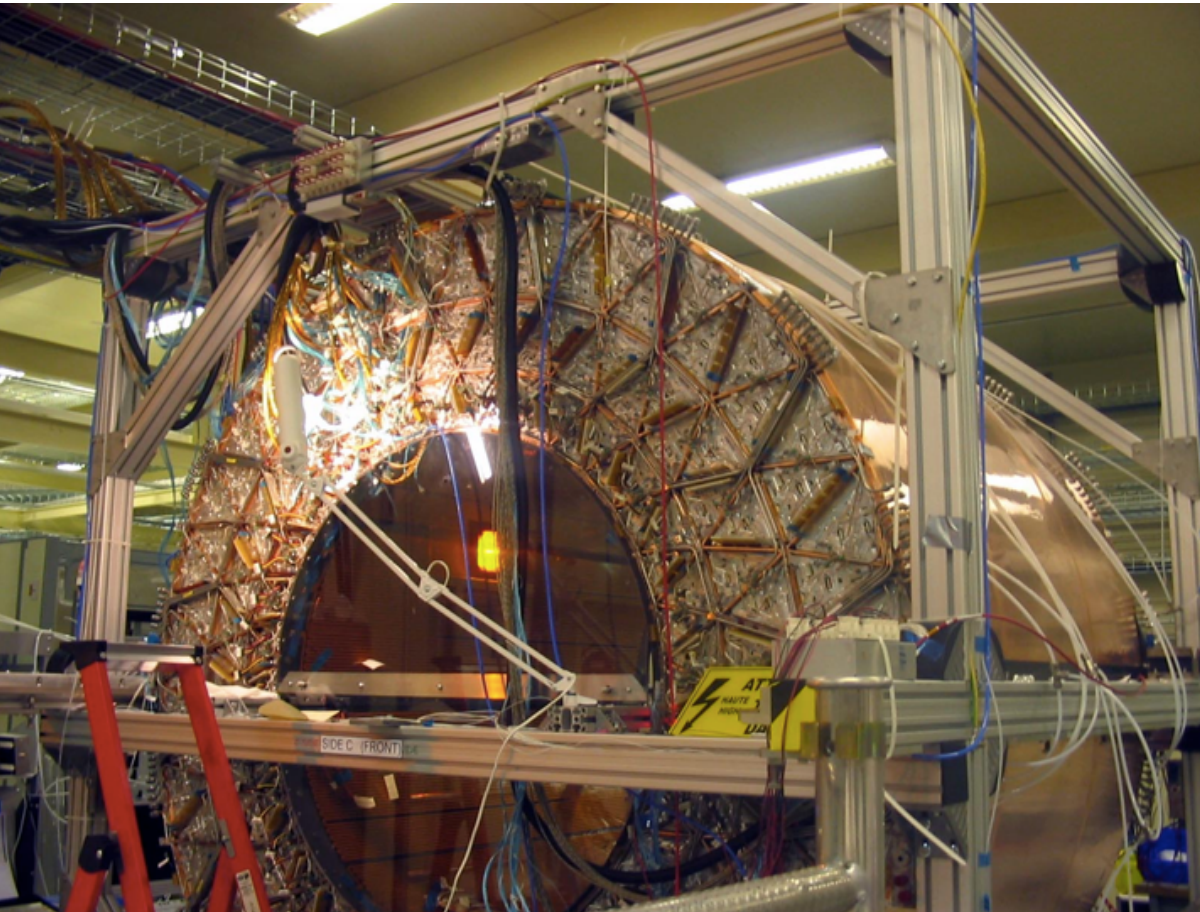
Challenges for silicon systems at the LHC

Just like your digital camera - except more directional, ie pointing in different directions (why?)... and we have to read out data a lot faster!

Not to mention dealing with intense radiation environments. Why might this be a problem? How can we mitigate the problem?



ATLAS TRT (Transition Radiation Tracker)

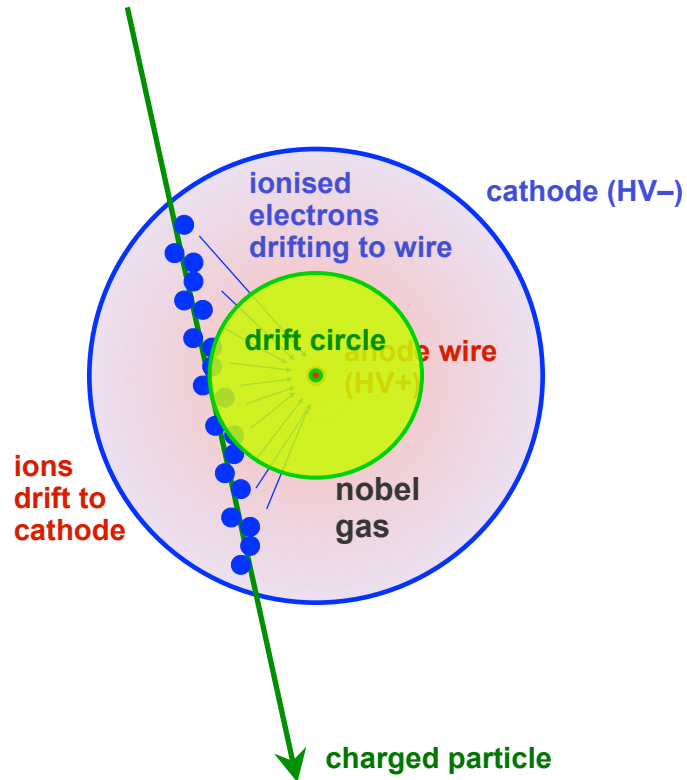


300,000 straws
(4 mm in
diameter) at
larger track
radius, ~ 35
measurements
per track. Also
helps with
particle
identification

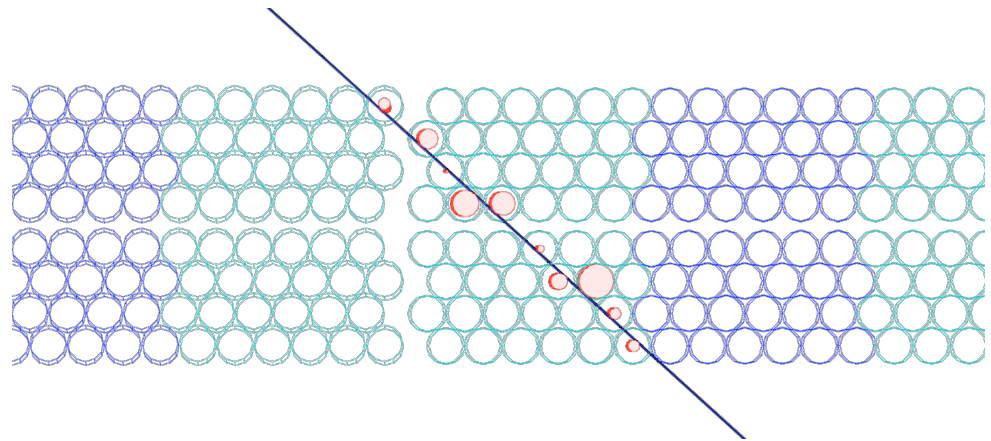
This is being removed for future LHC operations with larger numbers of collisions. Any guesses why?

Drift Tubes in ATLAS: Inner Detector and Muon Spectrometer

- classical detection technique for charged particles based on gas ionization and drift time measurement



example: segment in muon drift tubes reconstruction from measured drift circles (left-right ambiguity)

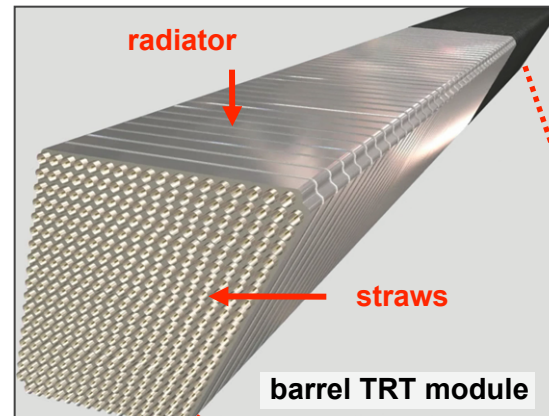
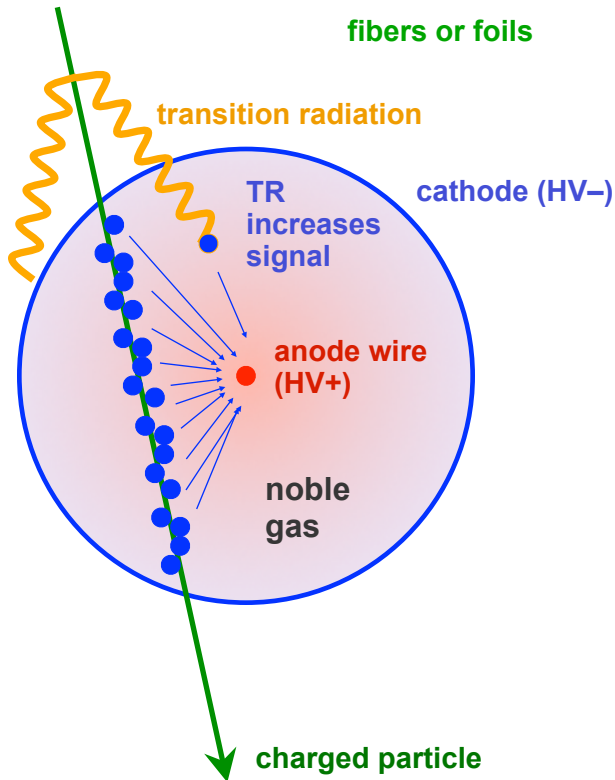


TRT: Kapton tubes, $\varnothing = 4 \text{ mm}$
MDT: Aluminium tubes, $\varnothing = 30 \text{ mm}$

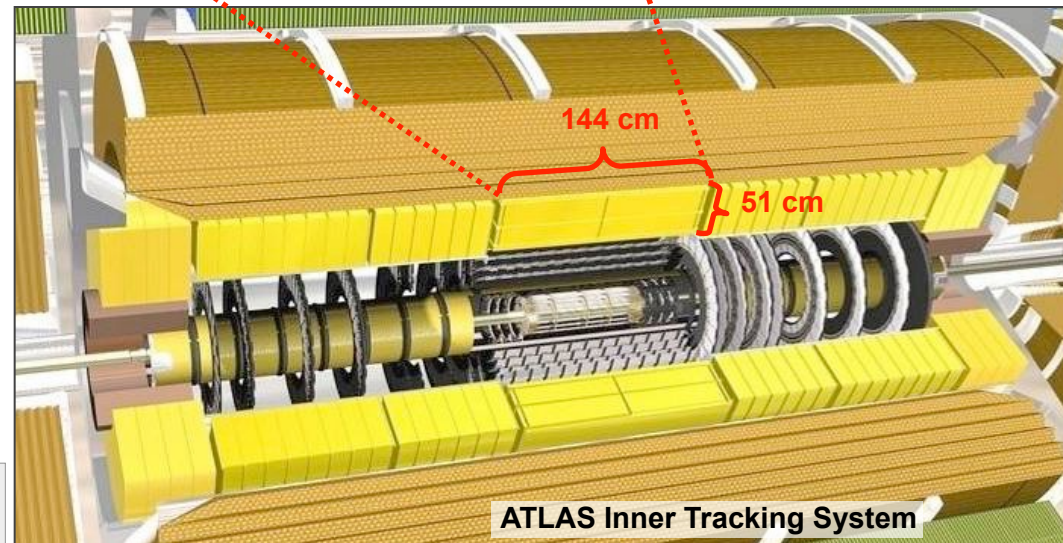
Slide from
Markus Elsing

Combining Tracking with PID: the ATLAS TRT

- e/π separation via transition radiation: polymer (PP) fibers/foils interleaved with drift tubes

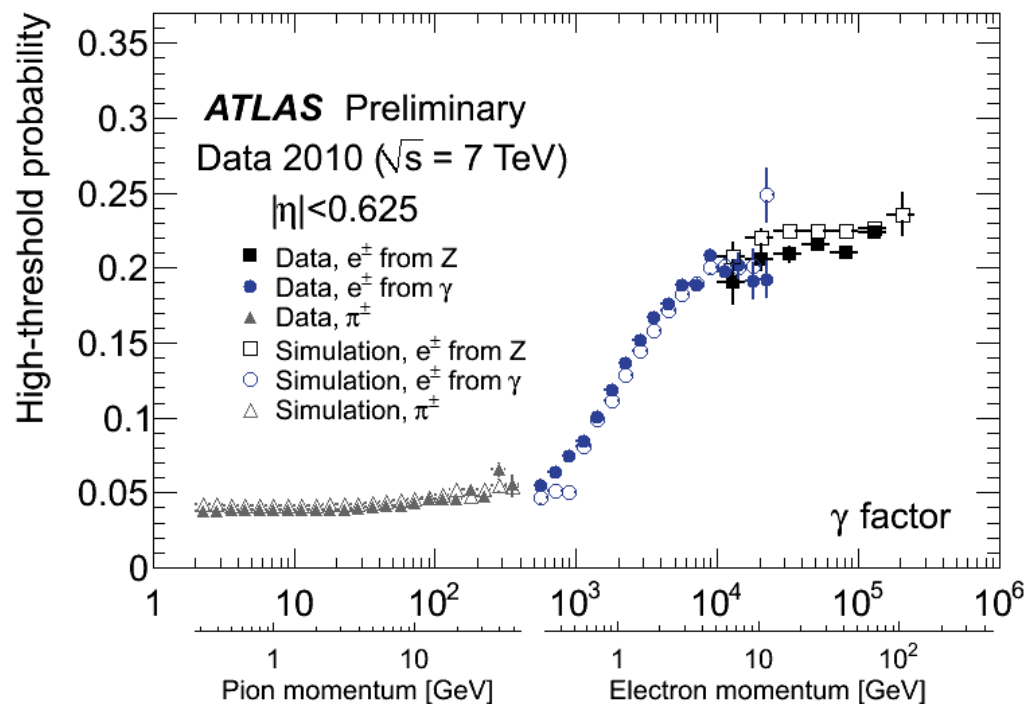


total: 370k straws
barrel ($|\eta| < 0.7$):
36 $r-\phi$ measurements / track
resolution $\sim 130 \mu\text{m}$ / straw
14 end-cap wheels ($|\eta| < 2.1$):
40 or less $z-\phi$ points



electrons radiate \rightarrow higher signal
PID info by counting
high-threshold hits

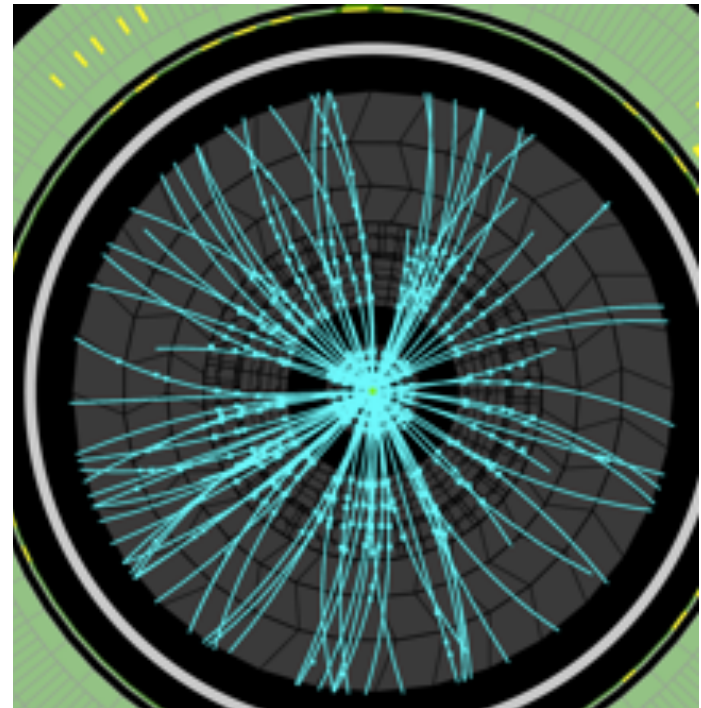
ATLAS-CONF-2011-128



Given ~ 30 hits per track, small difference in probability to measure hits with a higher threshold can give significant particle identification/background rejection for electron ID

$$p \propto B \cdot R$$

For precise measurement of p , want precise measurement of radius of curvature. 100 GeV object at ATLAS has $R = 166\text{m}$! A 1 TeV pion will have R close to 1 km... need precision in silicon systems of order ~ 10 microns per measurement



Particle travels $\sim c\tau$ before decaying in its own rest frame but in lab frame, $\sim \gamma c\tau$. Typically interested in objects with substantial Lorentz gamma factors, so muons, neutrons and charged pions and kaons travel and decay in the detector

Bethe-Bloch equation

When a relativistic charged particle passes through some material with atomic number Z and electron density n , it ionizes the atoms and thus loses energy. I is the mean excitation energy in the material $\sim 10 Z$ [eV]

$$-\frac{dE}{dx} = \frac{4\pi}{m_e c^2} \cdot \frac{n z^2}{\beta^2} \cdot \left(\frac{e^2}{4\pi\epsilon_0} \right)^2 \cdot \left[\ln \left(\frac{2m_e c^2 \beta^2}{I \cdot (1 - \beta^2)} \right) - \beta^2 \right]$$

Not very intuitive :)

Bethe-Bloche equation

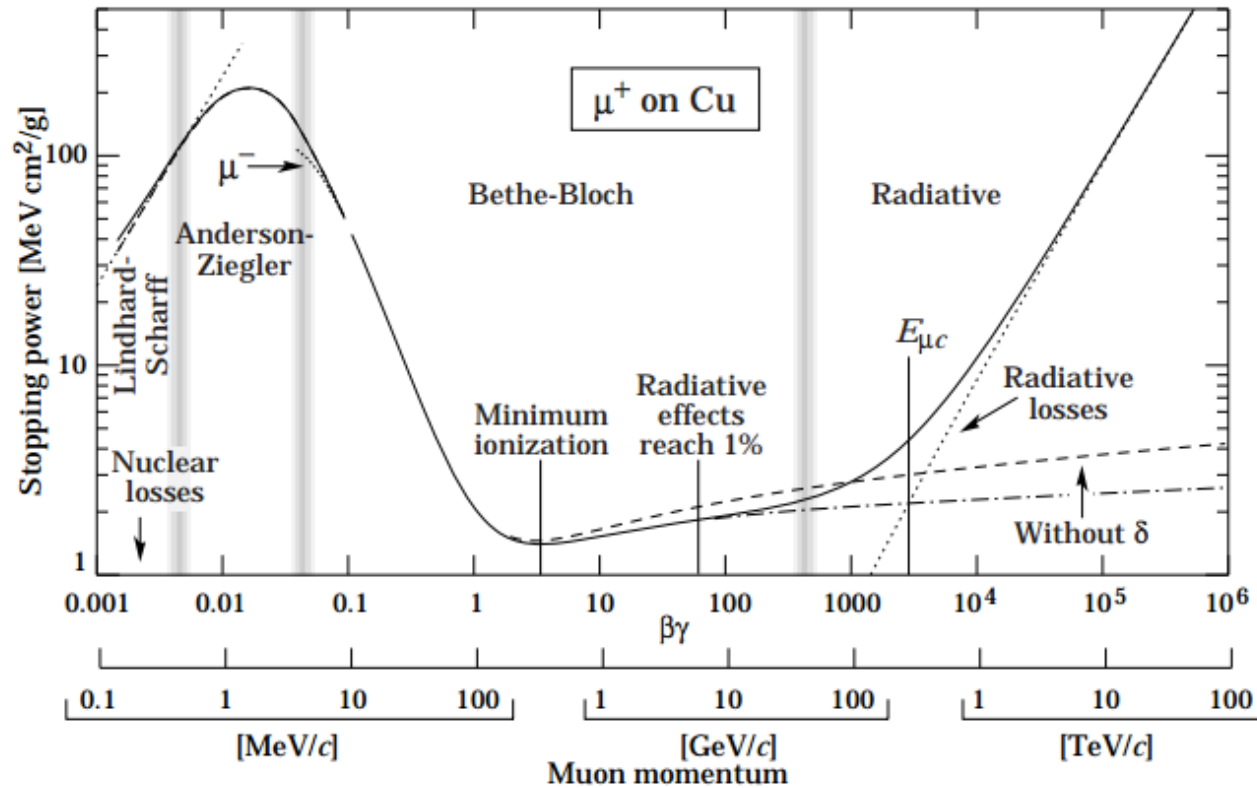
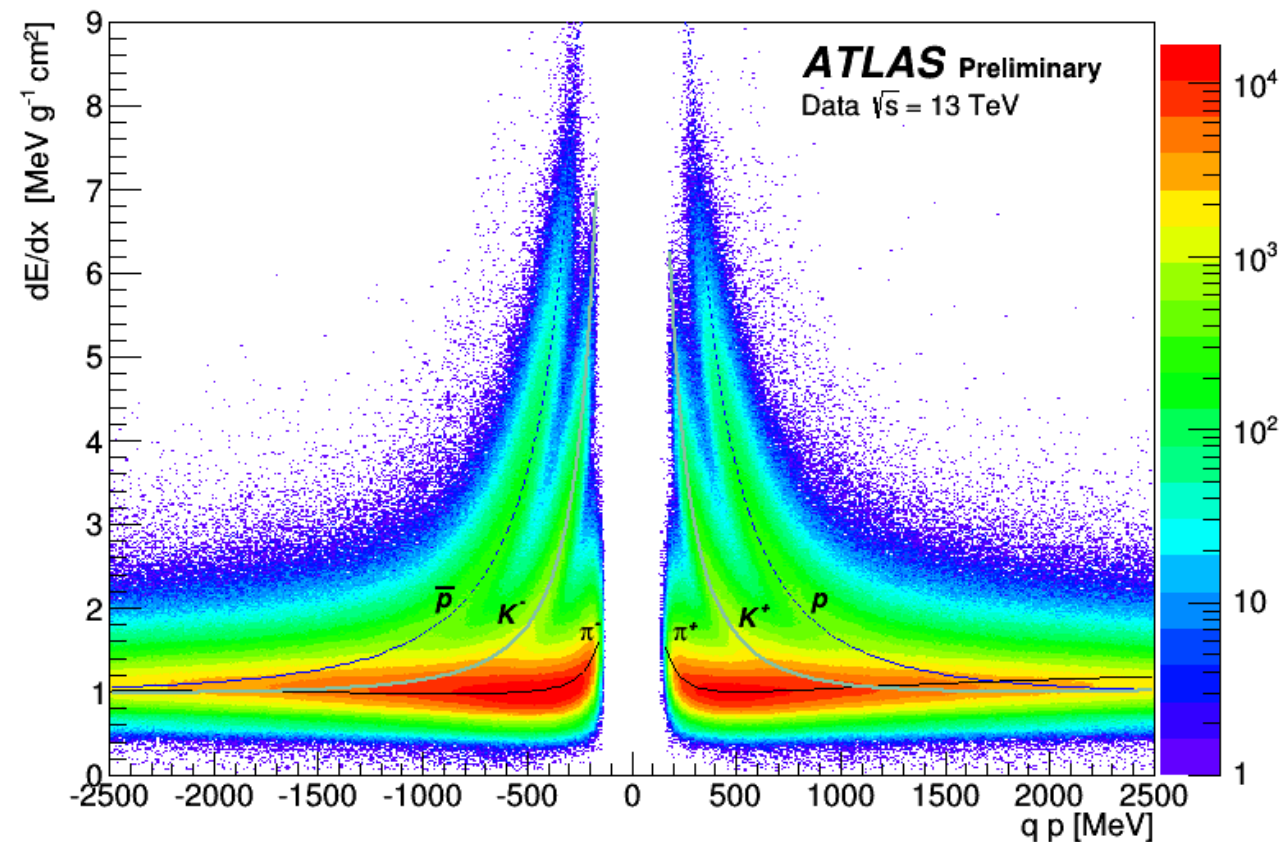


Fig. 27.1: Stopping power ($= \langle -dE/dx \rangle$) for positive muons in copper as a function of $\beta\gamma = p/Mc$ over nine orders of magnitude in momentum (12 orders of magnitude in kinetic energy). Solid curves indicate the total stopping power. Data below the break at $\beta\gamma \approx 0.1$ are taken from ICRU 49 [4], and data at higher energies are from Ref. 5. Vertical bands indicate boundaries between different approximations discussed in the text. The short dotted lines labeled " μ^- " illustrate the "Barkas effect," the dependence of stopping power on projectile charge at very low energies [6].

From PDG.
 Particles with $\beta\gamma \sim 3$ lose the least amount of energy as they travel, and are referred to as "minimum ionizing" particles

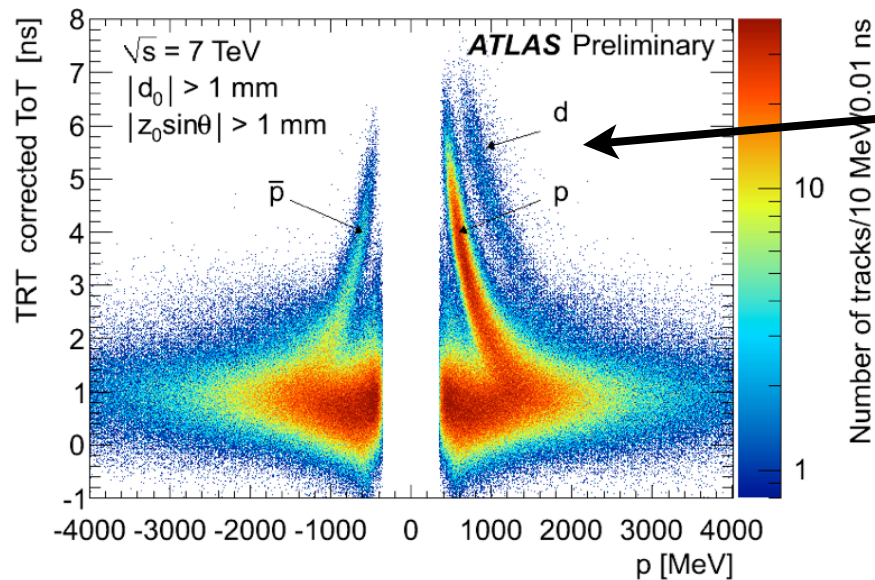
Using dE/dx in the pixel system of ATLAS



Can see
pions, kaons
and protons!

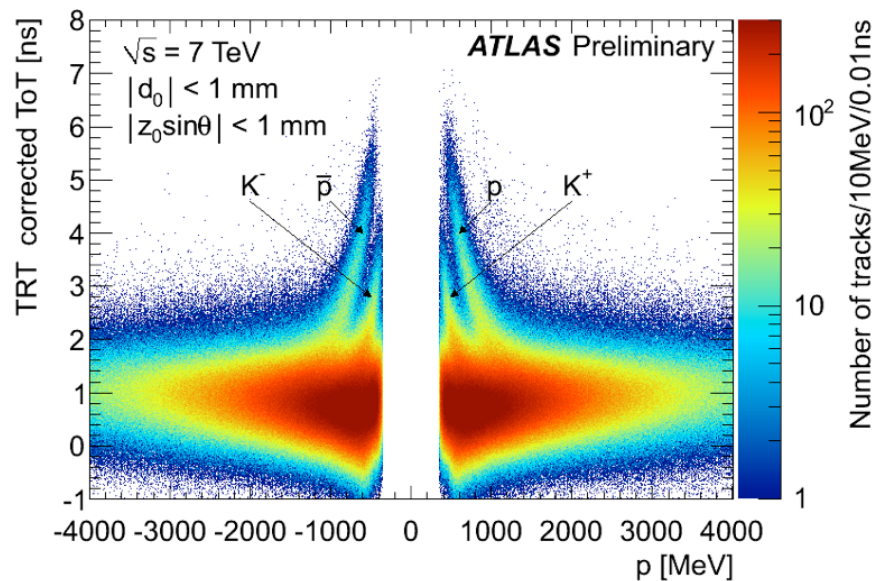
<https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/PLOTS/PIX-2015-002/>

Using dE/dx in the TRT system of ATLAS



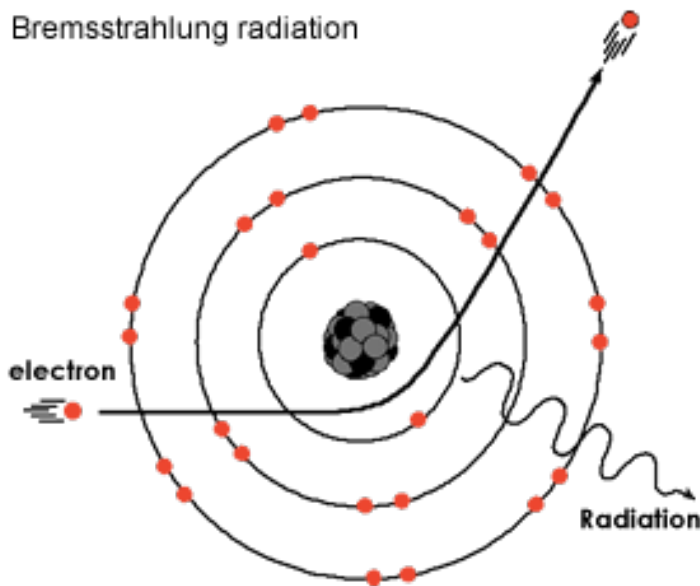
Asymmetry! Why?

Using “time over threshold”, we can also do particle identification with straw detectors

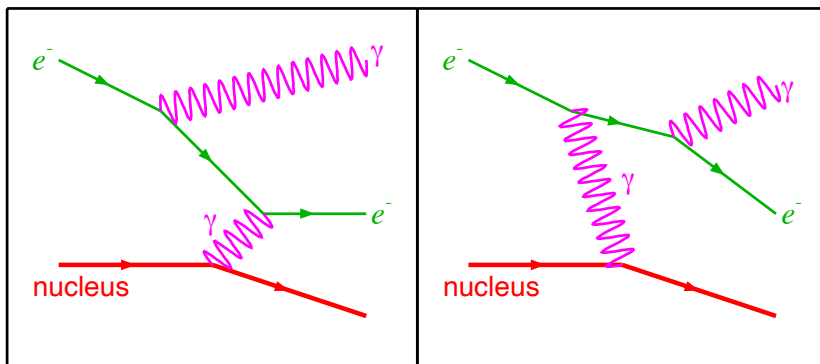


Bremsstrahlung

Bremsstrahlung radiation



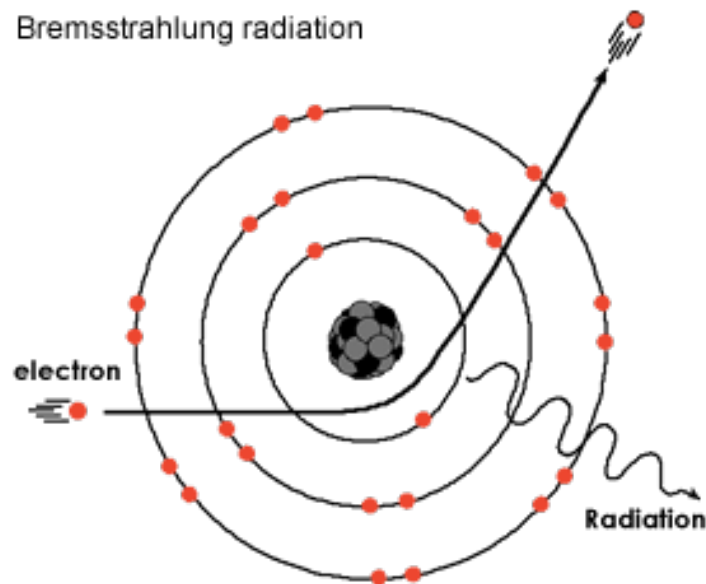
Bremsstrahlung



Literally “braking radiation” in German, **bremsstrahlung** is the main way that electrons of interest at ATLAS lose energy. In EM you might have seen that the amount of energy radiated away goes as $1/\text{mass}^2$, which is why one reason why ee accelerators need to be so big, and why muons don't lose much energy in the detector

Radiation length for high-energy electrons/photons

Bremsstrahlung radiation

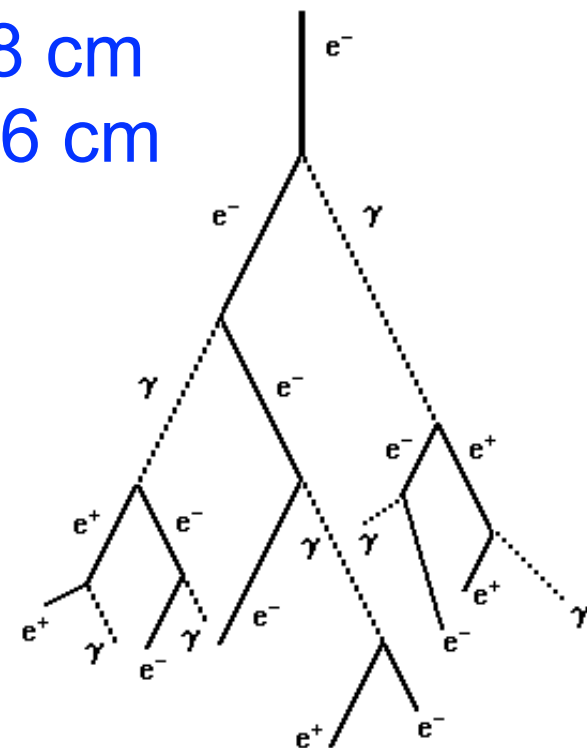
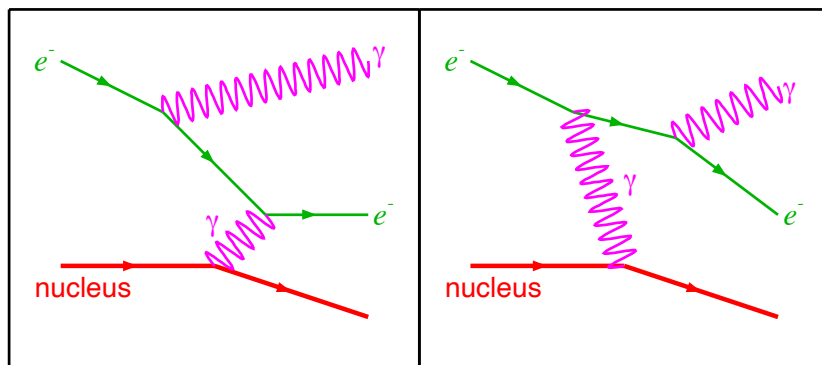


Radiation length X_0 is the average distance over which the energy of an electron is reduced by $1/e$ (characteristic distance scale for material effects)

$X_0(\text{iron}) = 1.8 \text{ cm}$

$X_0(\text{lead}) = 0.6 \text{ cm}$

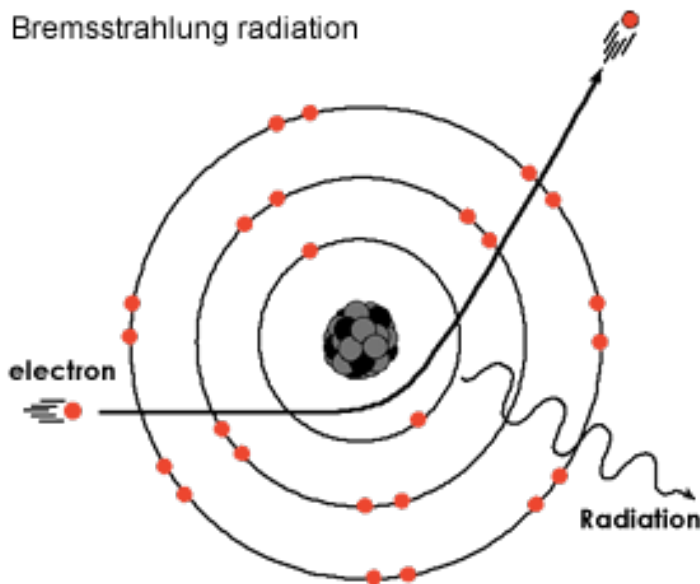
Bremsstrahlung



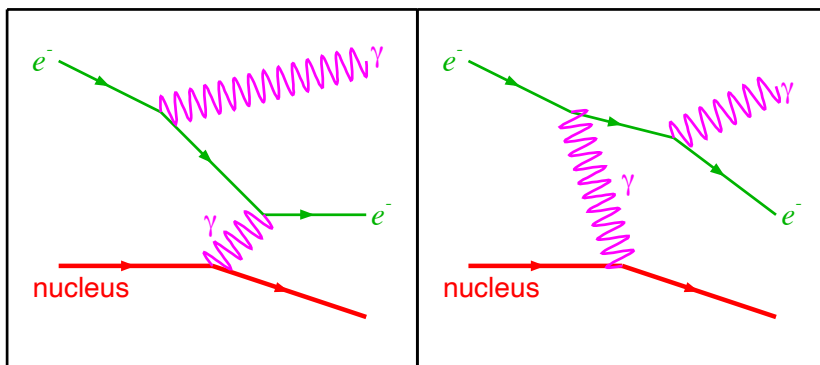
Very similar for photons

Radiation length for high-energy electrons/photons

Bremsstrahlung radiation



Bremsstrahlung



After 1 X_0 we have roughly twice as many particles, with half the original energy

After 2 X_0 , we have $\sim 4x$ as many particles, with $1/4$ the original energy

After n X_0 , we have $\sim 2^n$ as many particles, and the energy of each is $\sim 2^{-n}$ of the original value

At some critical energy E_c , the Brem process stops

$$\langle E \rangle_n = \frac{E}{2^n} = E_c$$

$$\ln E - \ln 2^n = \ln E_c$$

$$\ln E - n \ln 2 = \ln E_c$$

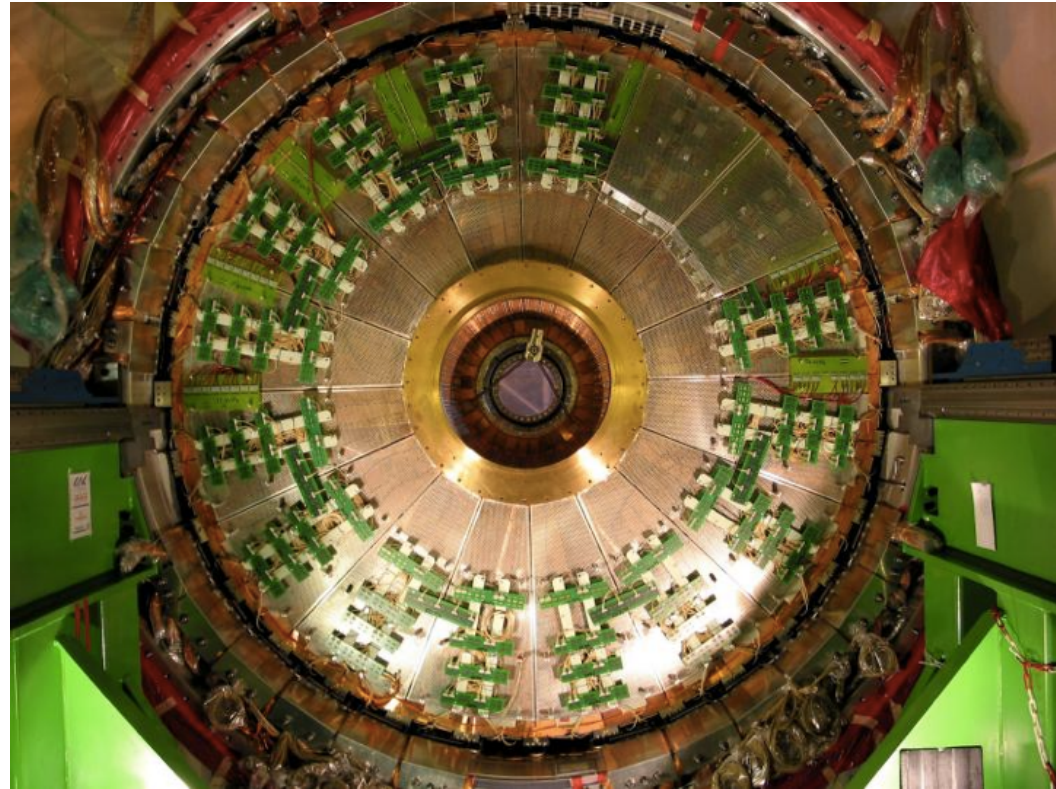
$$n \ln 2 = \ln(E/E_c)$$

$$n = \frac{\ln(E/E_c)}{\ln 2}$$

Here n is the number of radiation lengths where the maximum number of particles is observed, aka where Brem stops (for lead, 100 GeV electron gives 13 X_0 , which is just a few cm)

Need some dense material to absorb energy, and some active material to notice this and produce an output signal. Can be the same material, often is not. ATLAS EM calorimeter is lead-liquid argon

A view inside the ATLAS LAr calorimeter



Hadronic calorimeters

Trickier, as hadrons can be electrically neutral but even then the constituents (quarks) have electric charge.

And many hadrons have an overall electric charge

Defined by the nuclear interaction length (λ_I), which is the mean distance between hadronic interactions.

$\lambda_I(\text{lead}) = 17 \text{ cm}$ (compare with $X_0(\text{lead}) = 0.6 \text{ cm}$)

Also tricky because neutral pions decay 99% of the time to a pair of photons

Intersperse steel absorber with plastic scintillator tiles, plastic doped with organic material. When charged secondary particles emerge from the steel, they excite the doped material, and emit UV light that can be re-emitted as one color by a dye

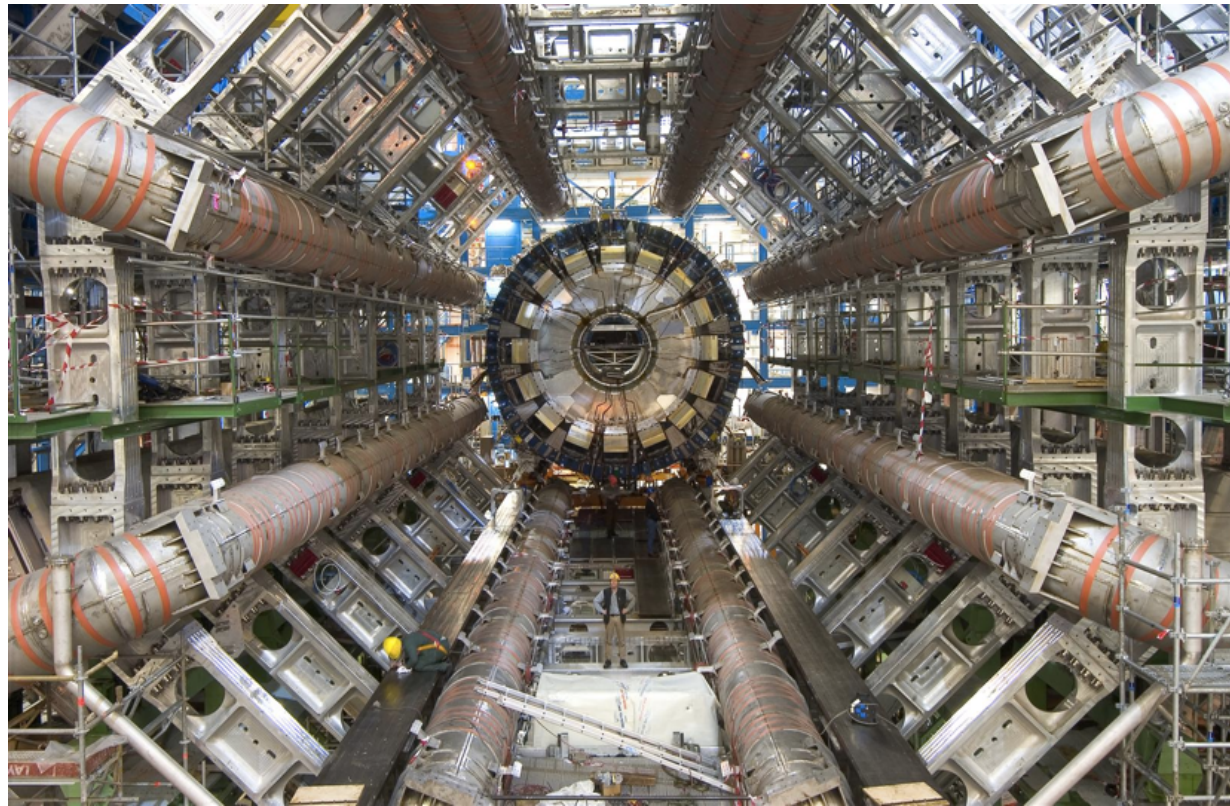
The ATLAS tile calorimeter



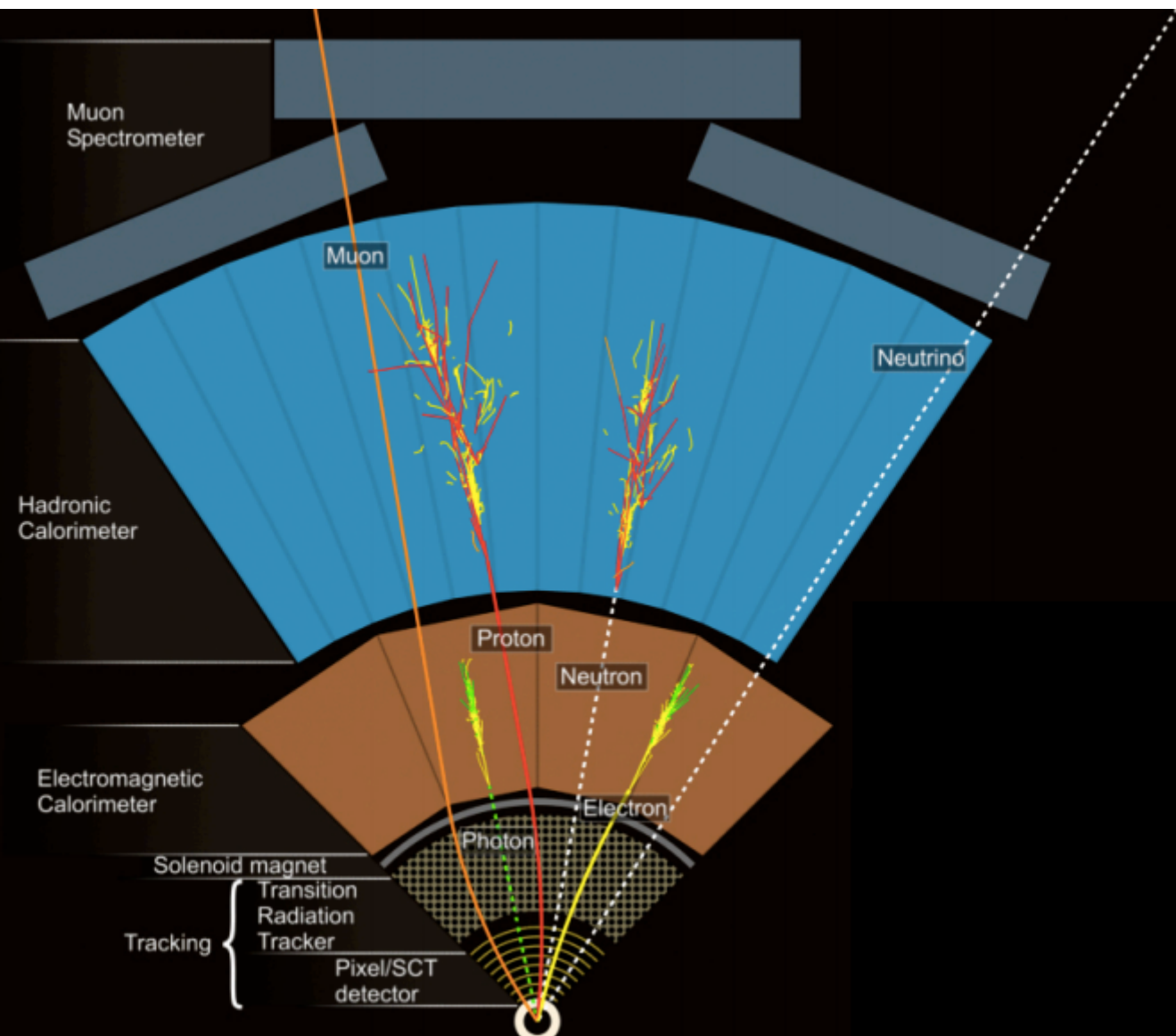
What emerges from the calorimeters?

Neutrinos... we “detect” them (indirectly) by applying momentum conservation in the plane perpendicular to the beam

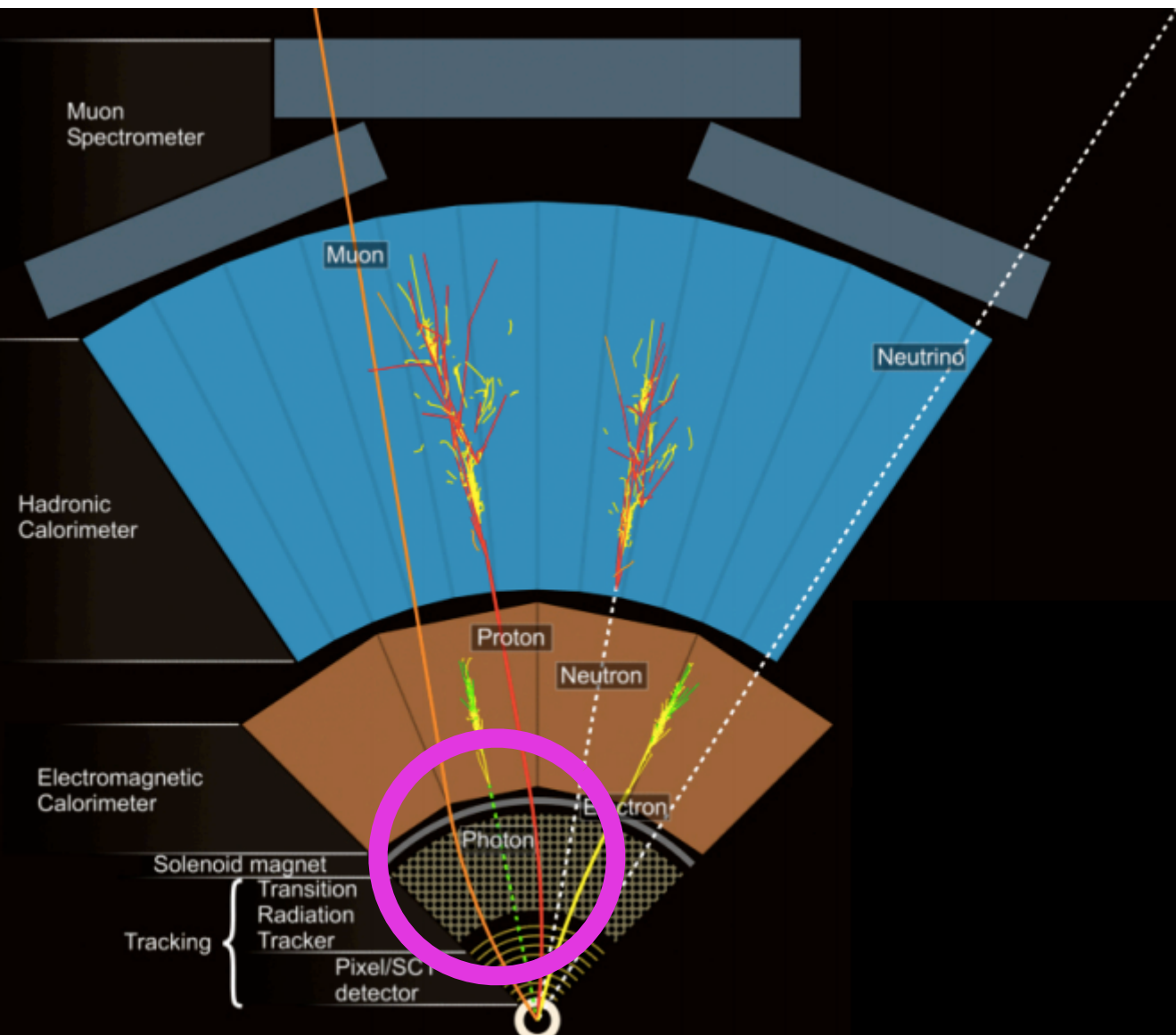
And muons! Have a set of toroidal magnets (giving ATLAS its shape and name) and more muon systems on outside of detector



Highly non-trivial B field. Need to monitor not just alignment but also field itself



Putting it all together

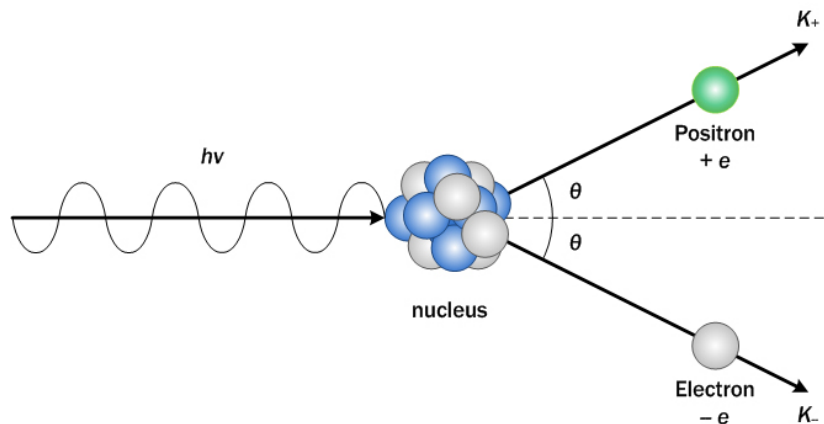
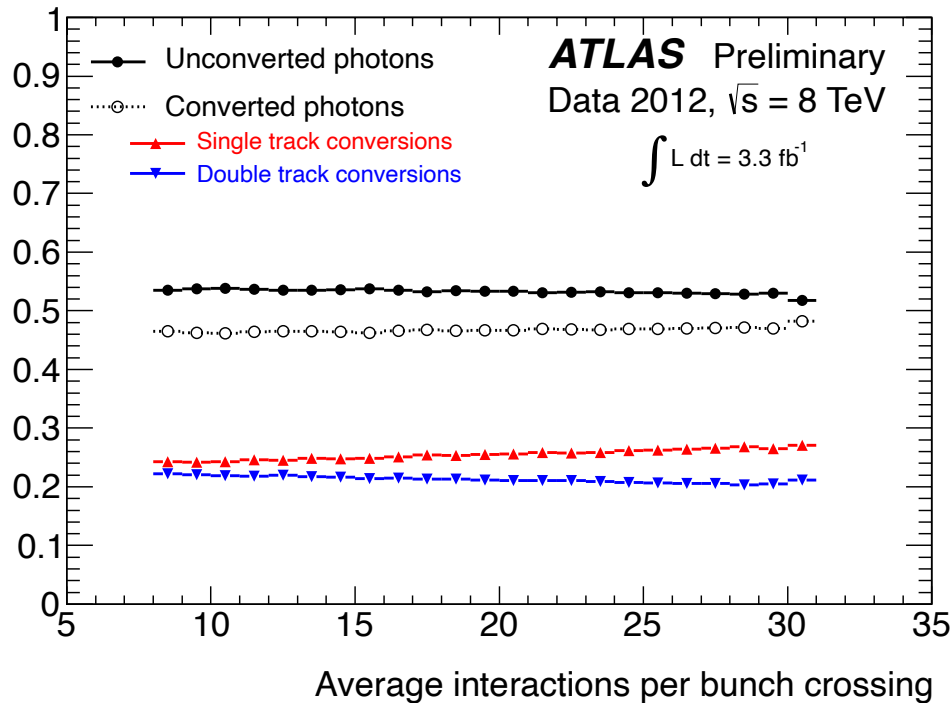


Photon can appear as isolated cluster in the EM calorimeter with nothing in hadronic calorimeter behind it and nothing else nearby. NO charged track pointing at calorimeter. Careful: lots of neutral pions!

Putting it all together

<https://twiki.cern.ch/twiki/bin/view/AtlasPublic/ElectronGammaPublicCollisionResults>

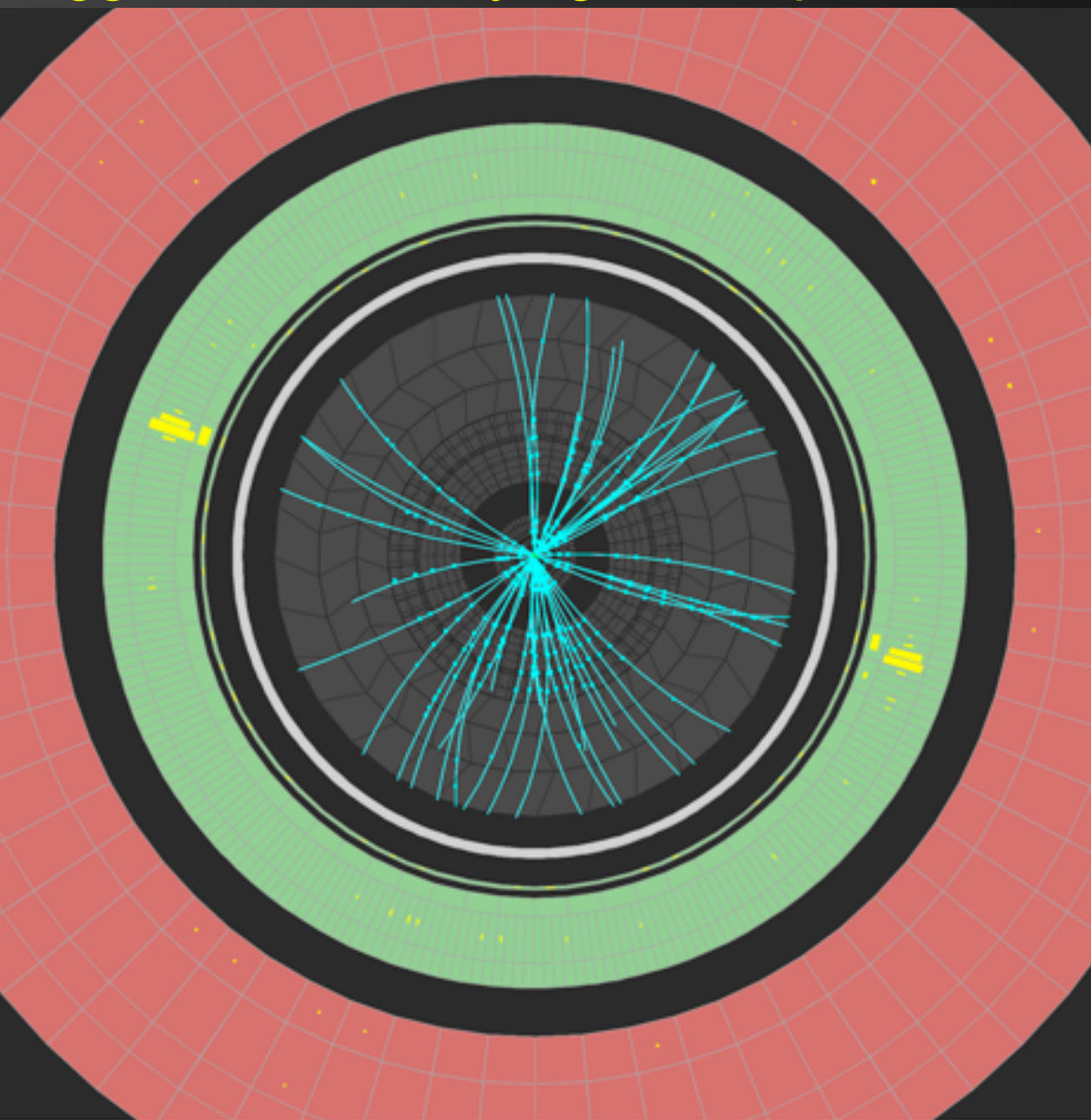
Fraction of photon candidates



Need to be careful because almost half of the photons at ATLAS interact with material in the detector before reaching the calorimeter! These photons look similar, except there are one or two clusters of energy with charged tracks not coming from the original interaction. How can there be only one track? Other one can be very **soft** (low momentum)

Higgs boson decaying to two photons

III

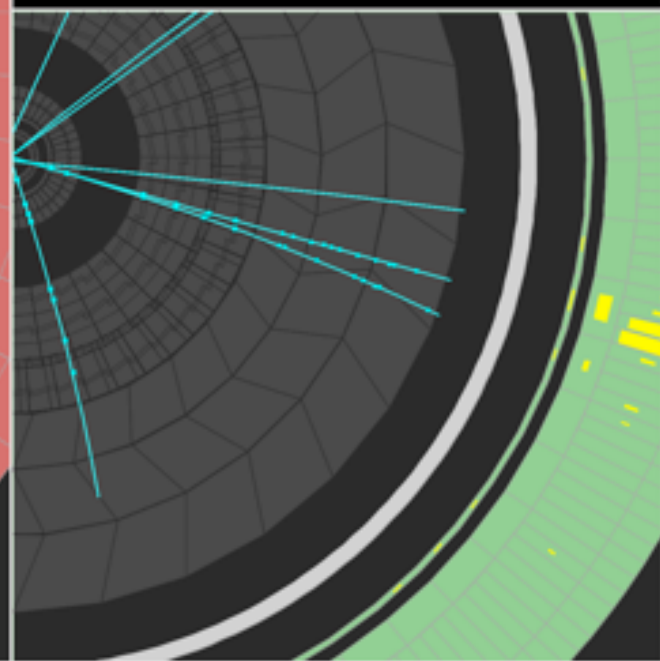


ATLAS
EXPERIMENT

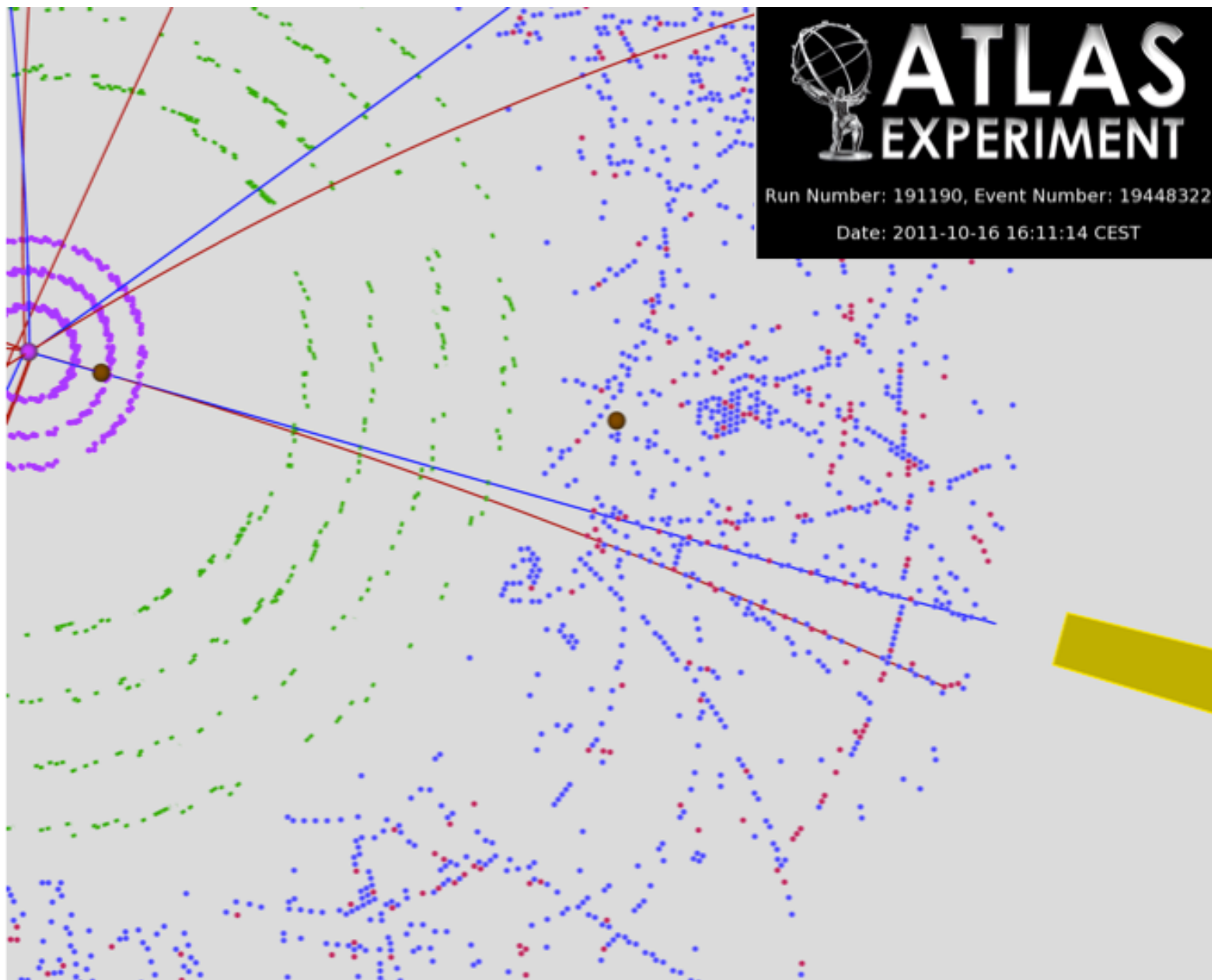
Run Number: 191190, Event Number: 19448322

Date: 2011-10-16 16:11:14 CEST

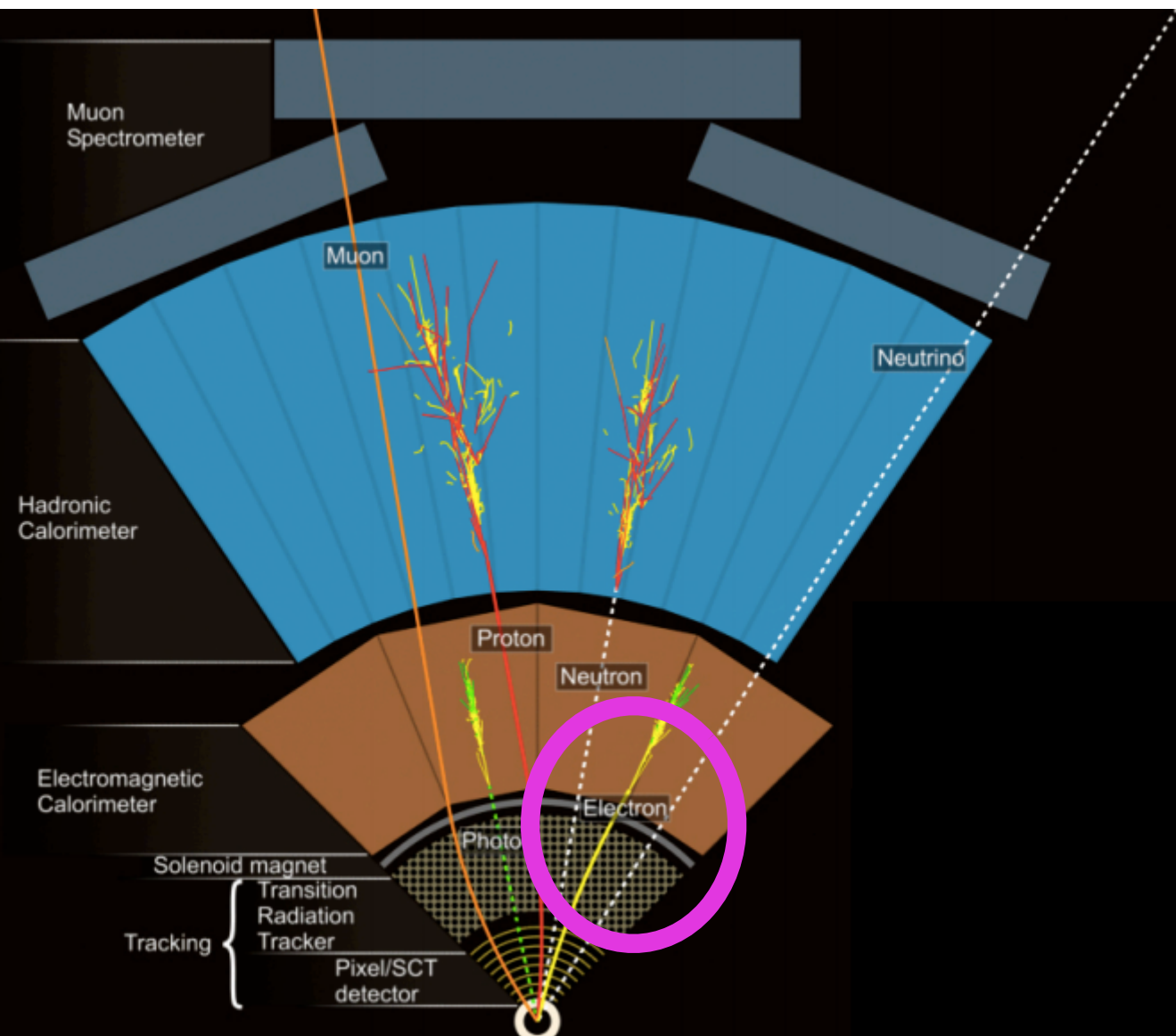
$$m_{\gamma\gamma} = 125.8 \text{ GeV}$$



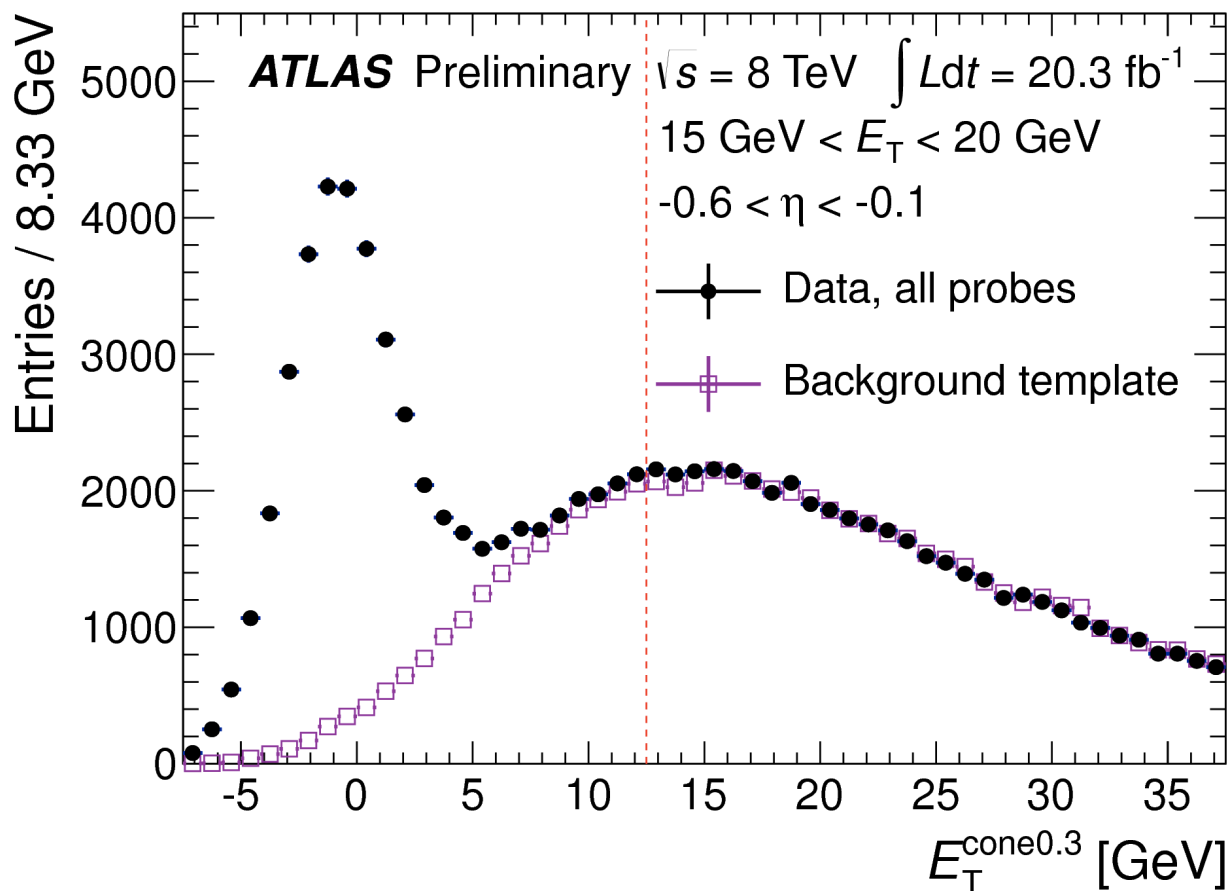
Zooming in on a converted photon



Putting it all together

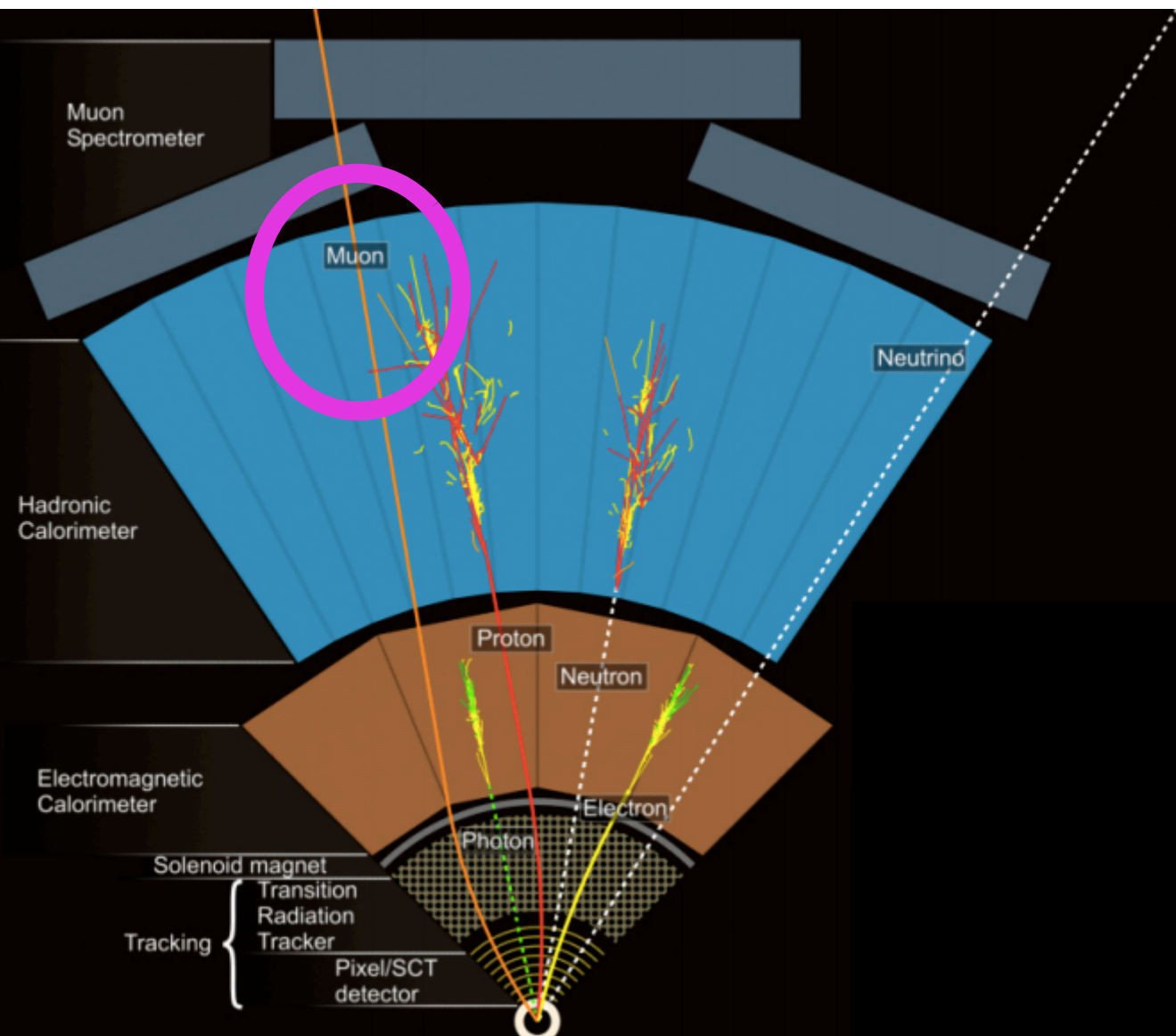


Electron appears as isolated cluster in the EM calorimeter with nothing in hadronic calorimeter behind it and a charged track. Photons and charged hadrons look like this too!



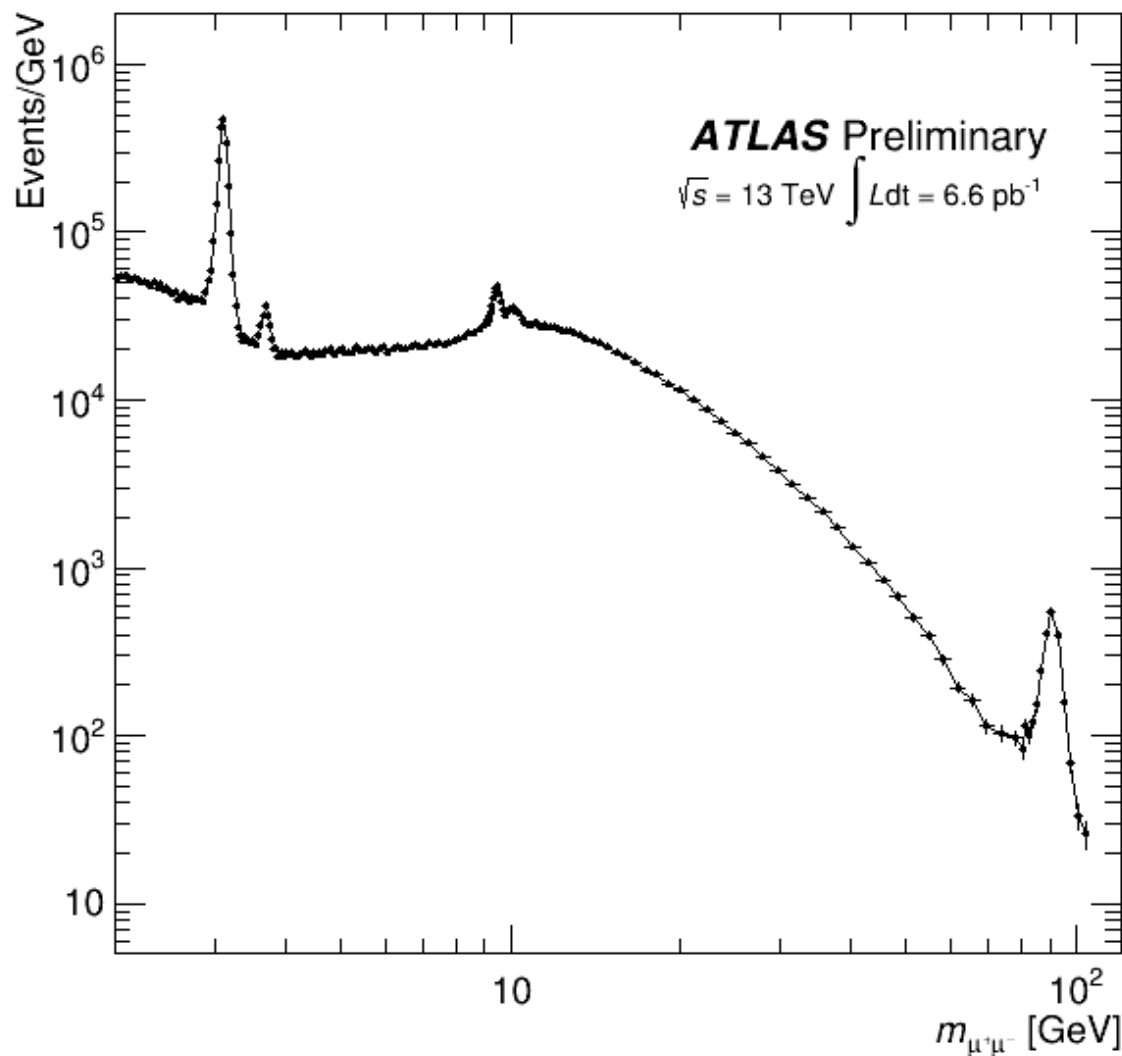
“Isolation” of nearby activity (in calorimeters and also tracking system) can help us to distinguish real electrons from fake electrons

Putting it all together

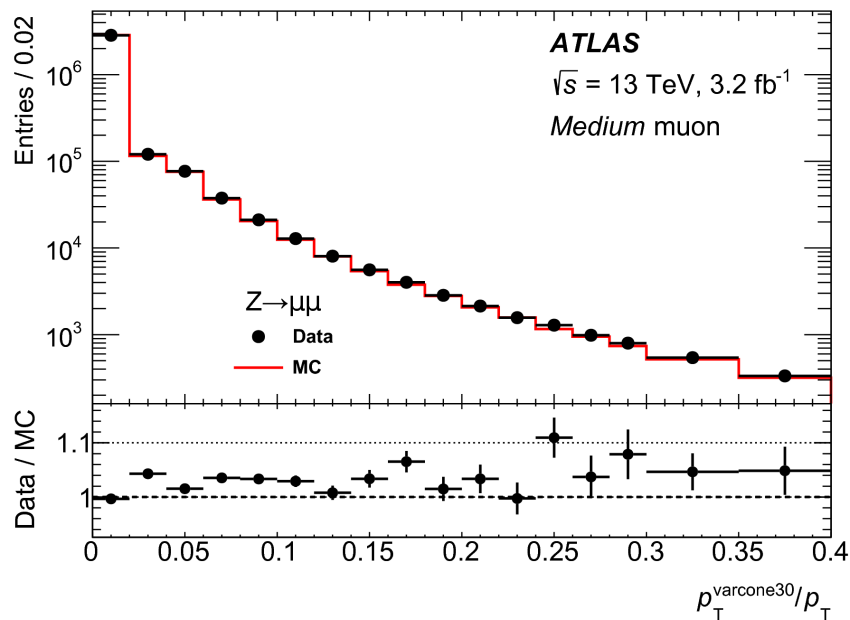


Muons appear as isolated, minimally ionizing particles in the calorimeter, with charged tracks in both the inner detector and also the muon spectrometer. Typically not so many fake muons, but can have **non-prompt** muons from hadron decays

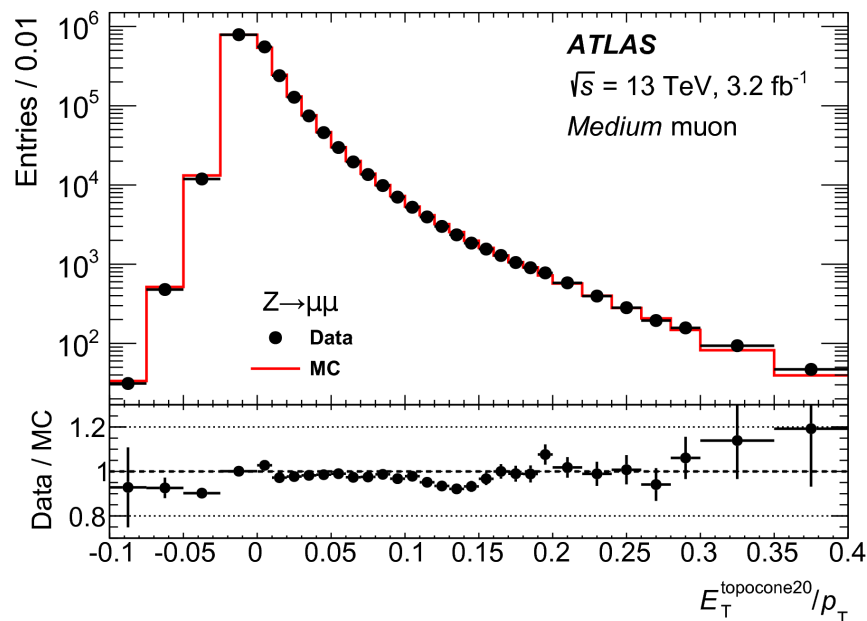
<https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/PLOTS/MUON-2015-001/index.html>



Beautiful
invariant mass
plot with early
Run 2 ATLAS
data

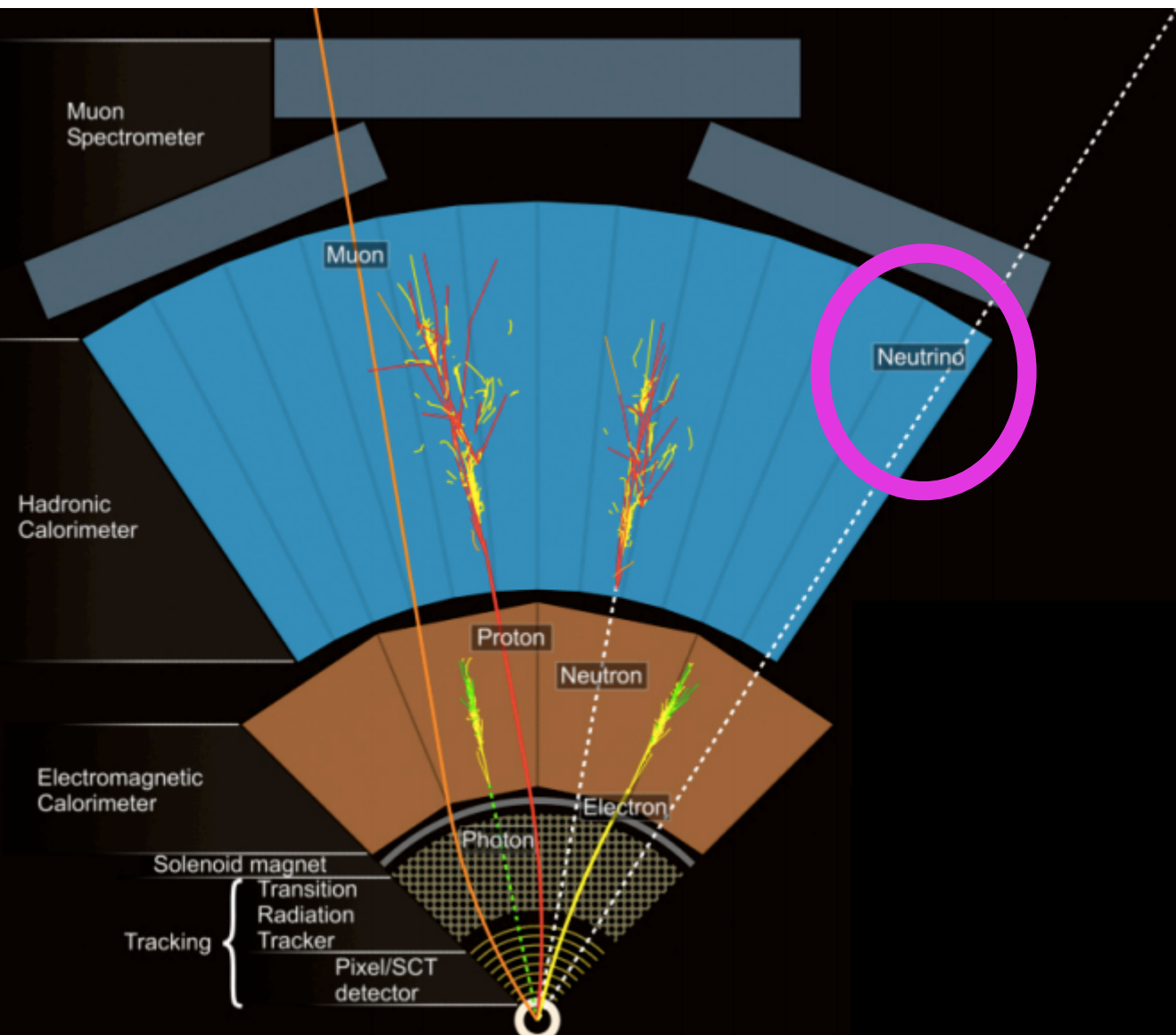


Let's look at these two isolation plots (from muons inside the Z boson mass window)

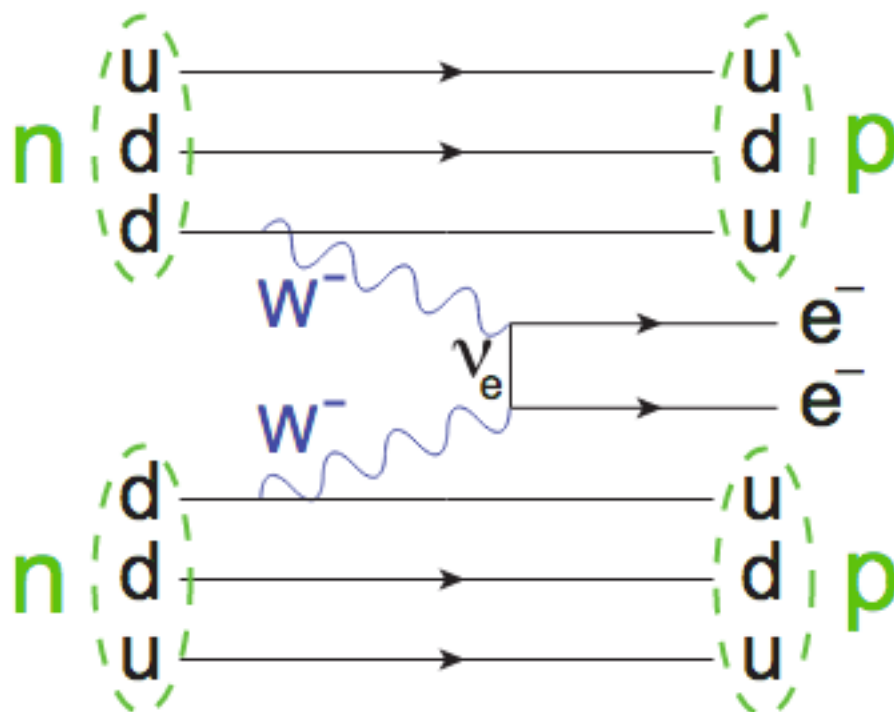


[arXiv:1603.05598](https://arxiv.org/abs/1603.05598)

Putting it all together



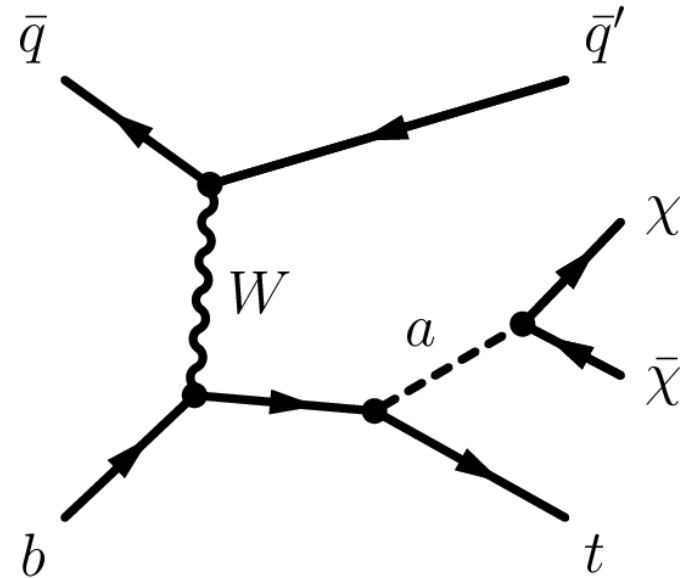
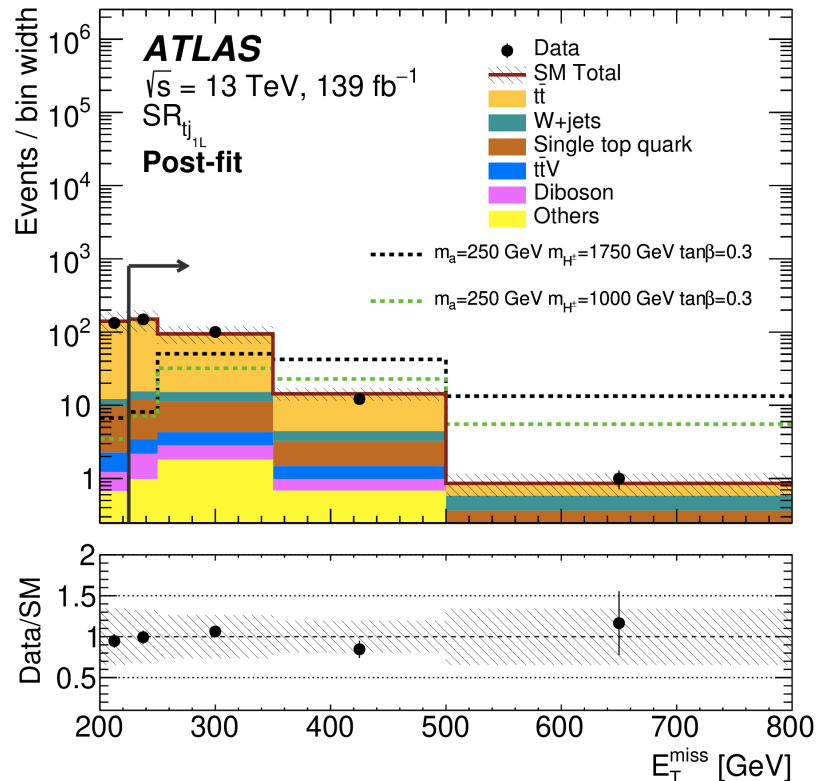
Neutrinos are not measured directly but inferred by applying the conservation of momentum to all measured objects



Any guesses?!

Are neutrinos Majorana particles (ie their own anti-particles)? Different than Dirac particles (not their own anti-particles). Would violate electron flavor number! How to observe this?

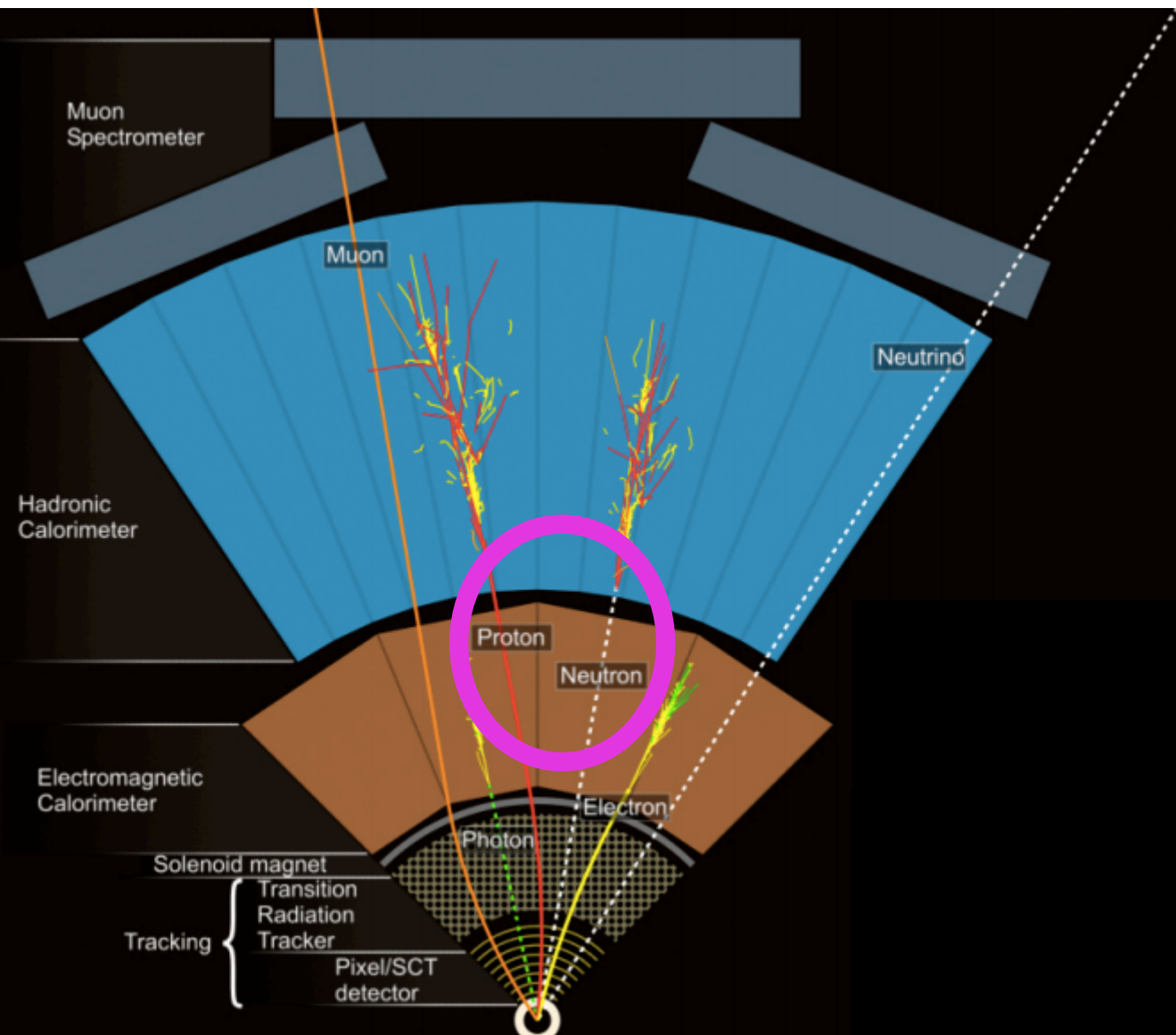
Using “MET” at ATLAS



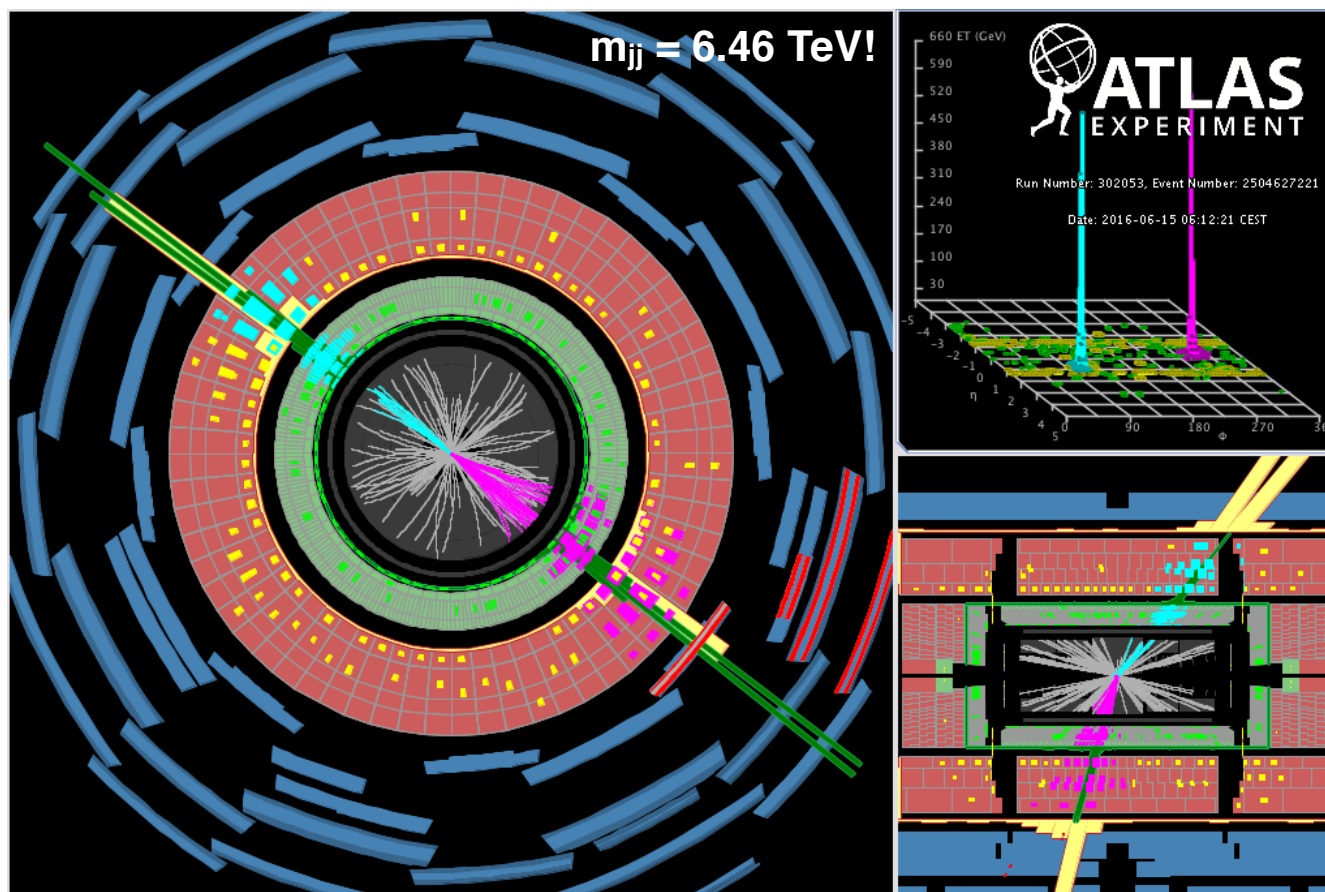
Using momentum imbalance to look for dark matter production

Note the nomenclature of “Missing energy” as part of “MET” even though energy is a scalar. Physicists are lazy!

Putting it all together



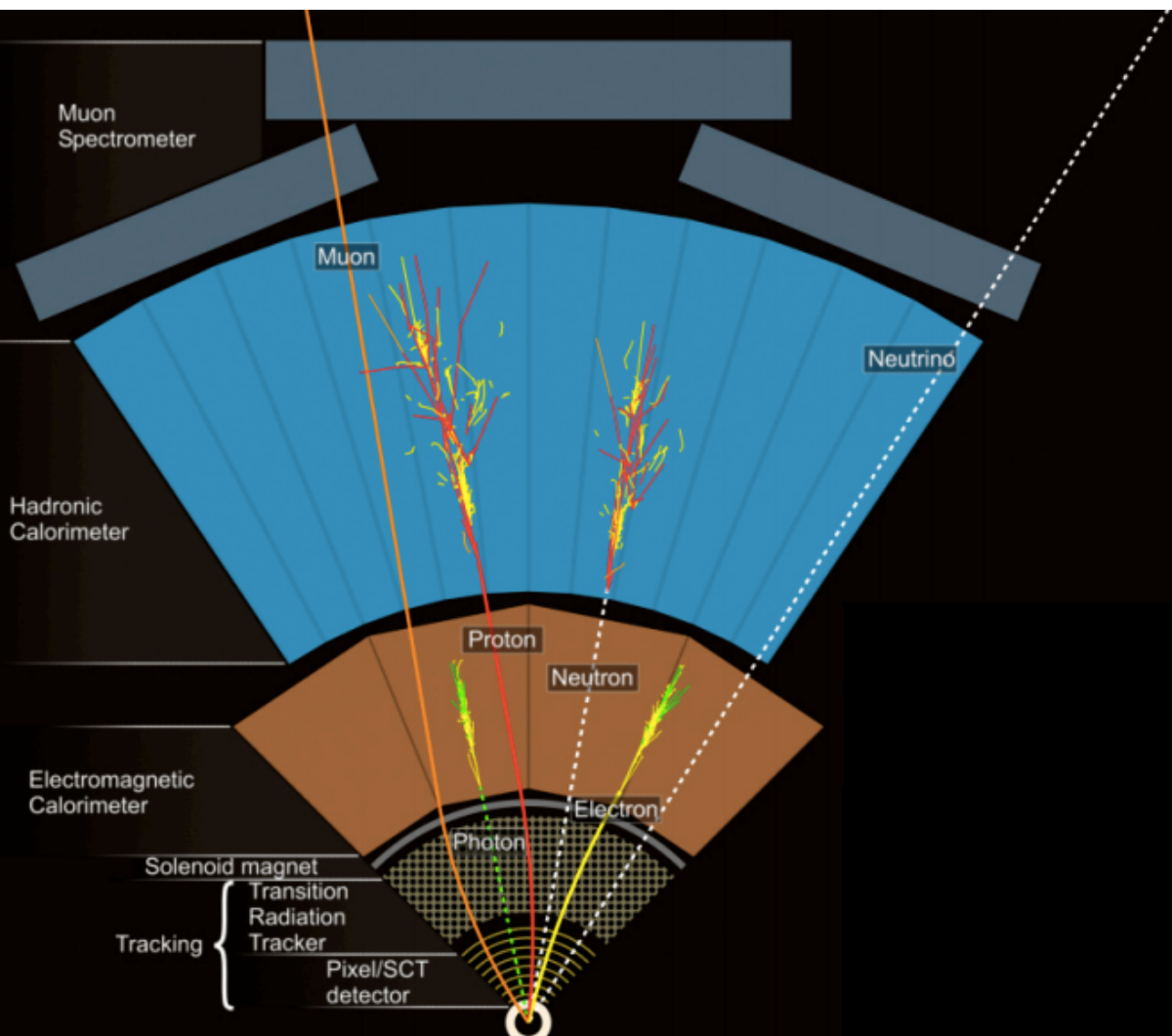
Protons leave charged tracks, neutrons do not. Each deposit energy in both the electromagnetic and hadronic calorimeters. Both typically not produced on their own but with lots of other particles nearby inside of a **jet**



Typical jet has
~60% of energy
in charged
particles (mostly
pions), ~30% in
photons from
neutral pion
decay, and 10%
neutrals. On
average, of
course

In a process like $pp \rightarrow qq\bar{q}$, quarks are flying apart in opposite directions. They do not form a bound state together, but the energy pulling them apart leads to radiation of gluons and lots of other quarks, which decay to other objects with QCD color charge, which decay, etc into a collection of particles called a **jet**

Putting it all together



Taus can decay to

an electron (18%);

a muon (17%);

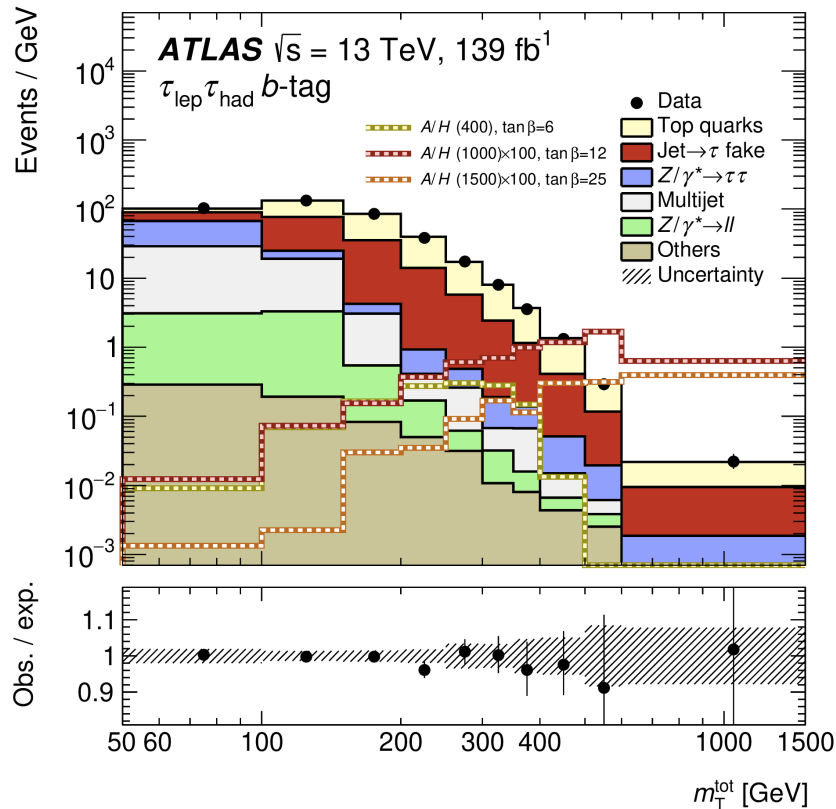
a single charged pion and extra neutral pions decaying to photons (48%);

three charged pions plus extra neutral pions decaying to photons (15%)

Taus are often reconstructed as a narrow collimated jet of 1 or 3 tracks

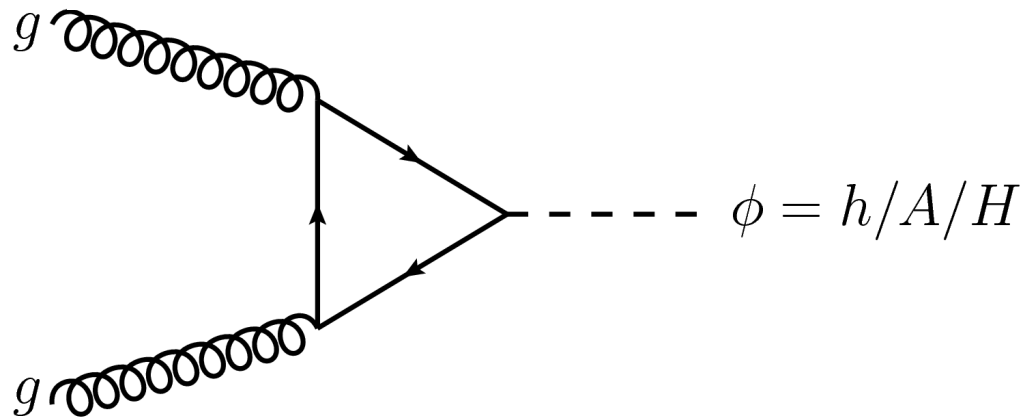
(Ignoring neutrinos)

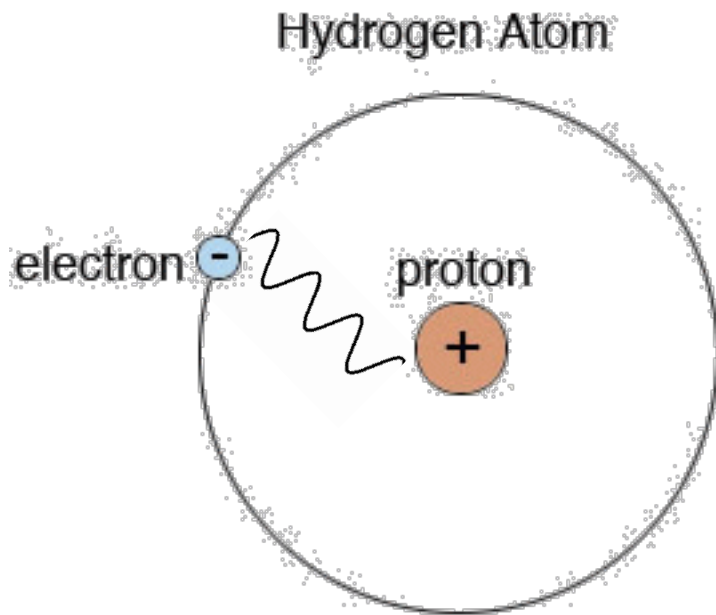
Using taus at ATLAS



[arXiv:2002.12223](https://arxiv.org/abs/2002.12223)

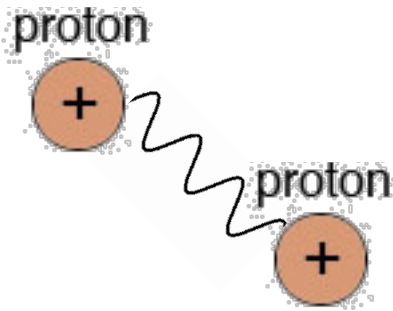
In many models of Beyond Standard Model physics, new Higgs-like particles prefer to decay to heavy objects. Can have such objects decay to a pair of taus



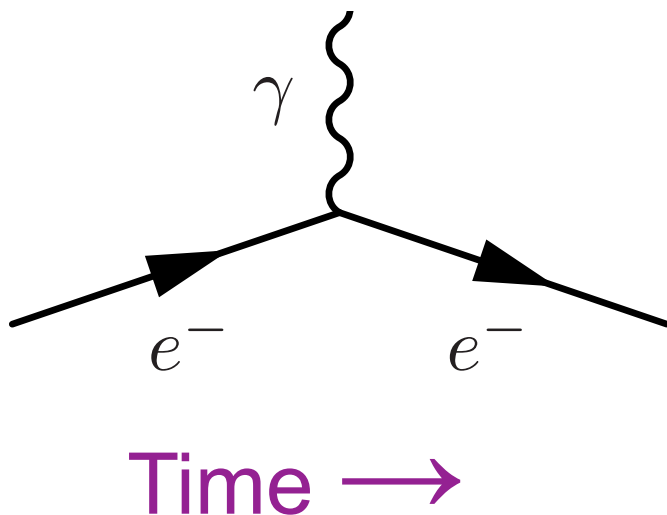


Photon as a particle (classical). But of course, what we really mean is that the field is quantized (here providing an attractive force), and the quantized unit of the field transmits some momentum from one object to another

But these forces can also be repulsive (more intuitive, actually)



Photon are still exchanged here, but now they transmit a repulsive force. It's a bit counterintuitive to think of forces being transmitted (or even better, '**mediated**') by particles, especially on a macroscopic scale, but we are anyway talking about single particles

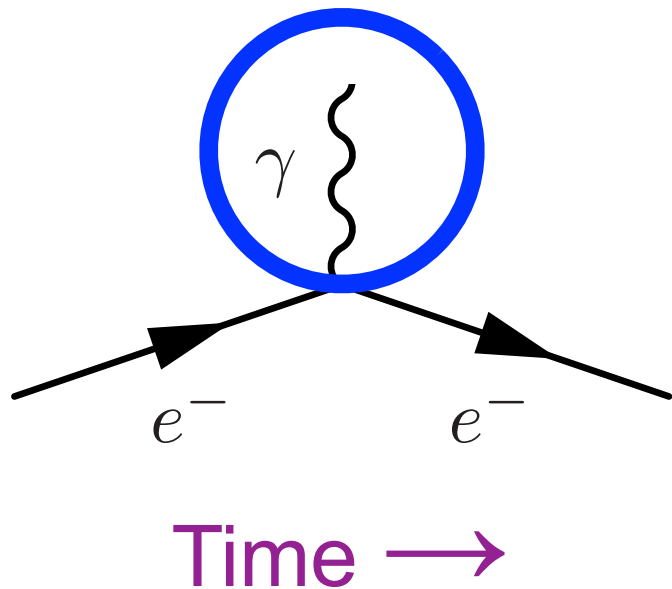


Think of time “passing” to the right, so initially (the “initial state”) we start with an electron. And at the end (in the “final state”), we also have an electron.

At some intermediate time, there is a photon interacting with this electron (whether it emits it or absorbs it). We can combine multiple such diagrams

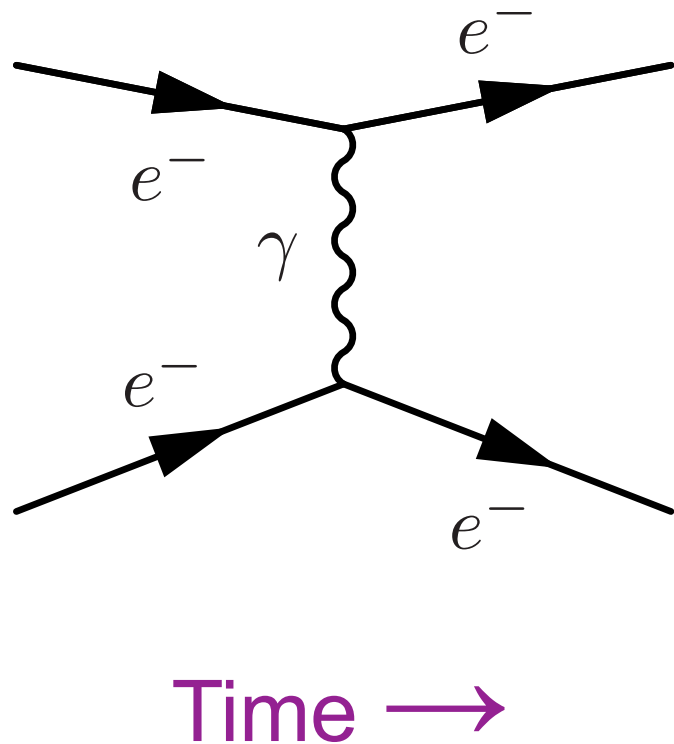
Feynman diagram

Note: Photon gets a squiggly line!



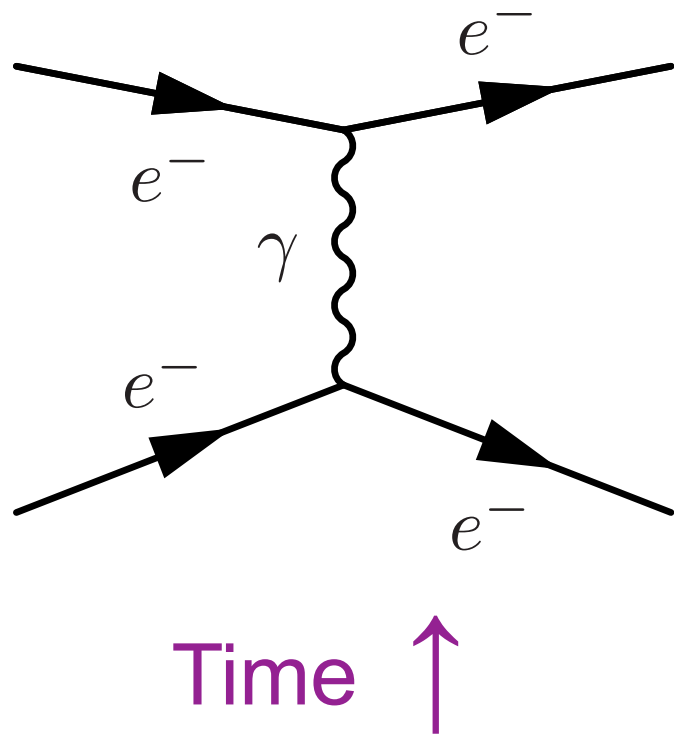
Think of time “passing” to the right, so initially (the “initial state”) we start with an electron. And at the end (in the “final state”), we also have an electron.

At some intermediate time, there is a photon interacting with this electron (whether it emits it or absorbs it). We can combine multiple such diagrams



At some initial time, there were two separate electrons. At a later time, there were also two electrons. At an intermediate time, they were exchanging a photon between them (repulsive force).

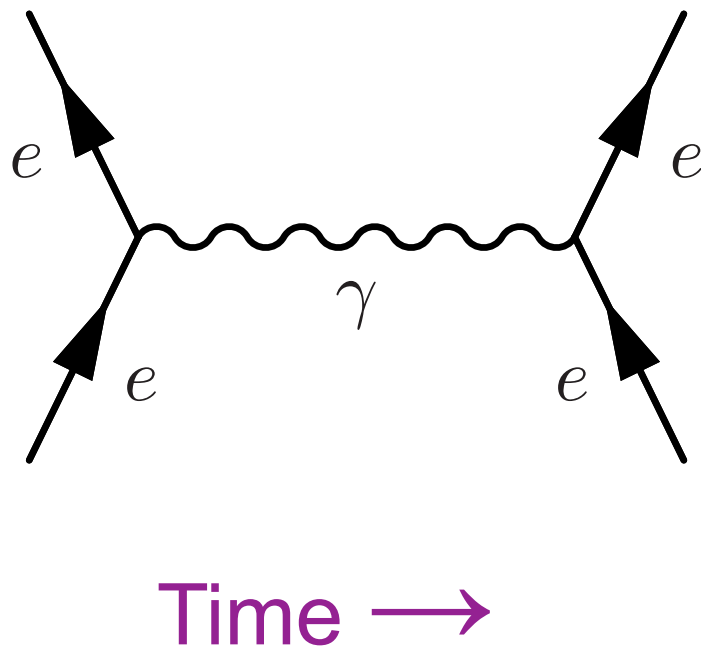
Møller scattering



What happens if we just change the direction of time? Everyone turn your heads now :)

Does this remind you of anything from earlier in the course?

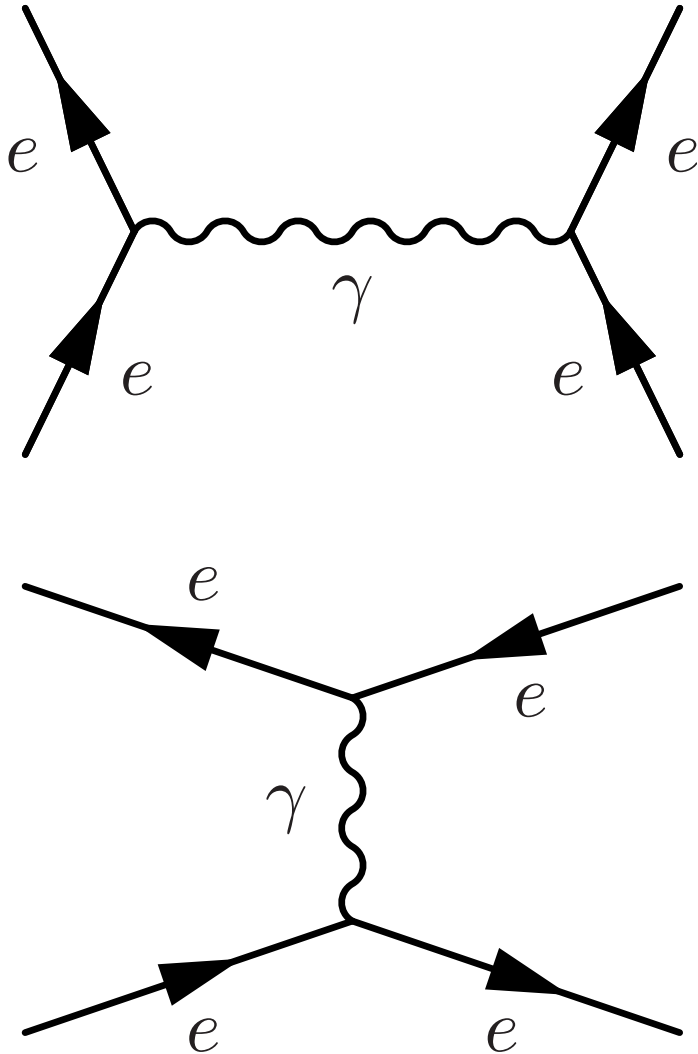
Feynman diagram (I turned things for you)



Electron vs positron
should now be more
obvious/automatic

Here I put things back such that time moves to the right. Note that in the initial time (on left) there is a fermion line moving backwards! This is an antiparticle moving forwards in time. And on the right there is a fermion line also going backwards, this is again an anti-particle

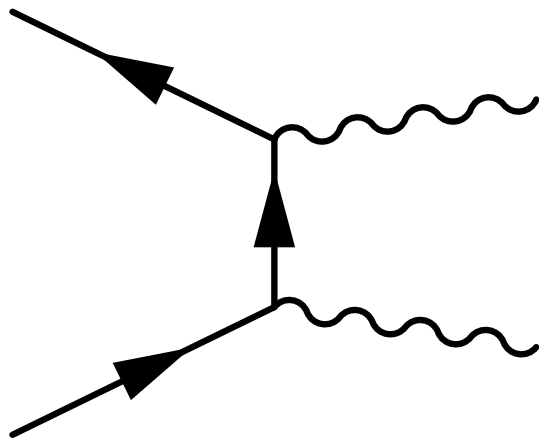
Bhabha scattering



Note the second diagram below... start with e^+e^- and end with e^+e^- ... these two diagrams are both needed (same initial and same final states, so they must interfere quantum mechanically!)

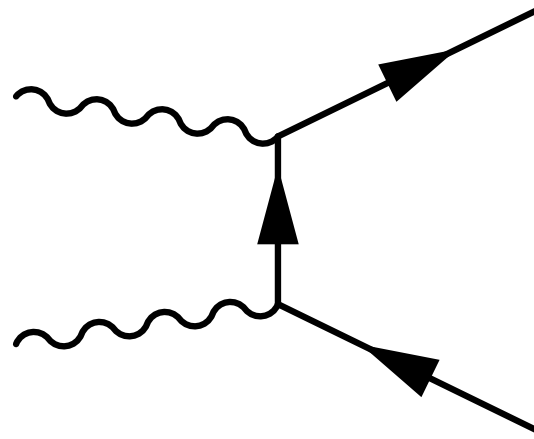
Feynman diagrams (note crossing symmetry again!)

Pair annihilation



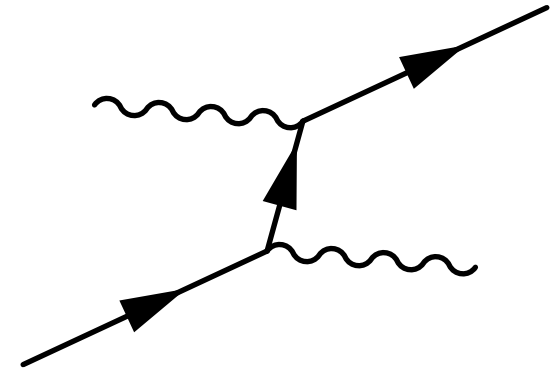
$$e^-e^+ \rightarrow \gamma\gamma$$

Pair production



$$\gamma\gamma \rightarrow e^-e^+$$

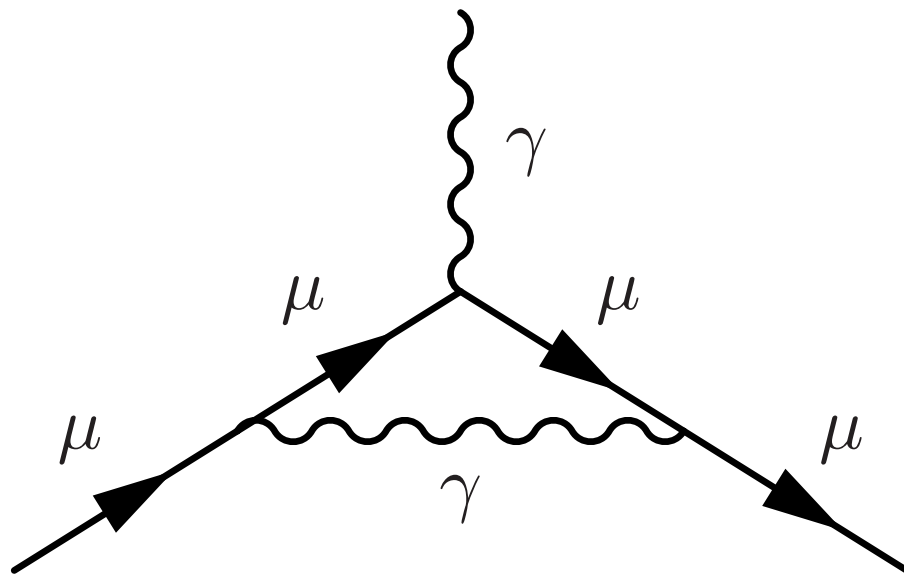
Compton scattering



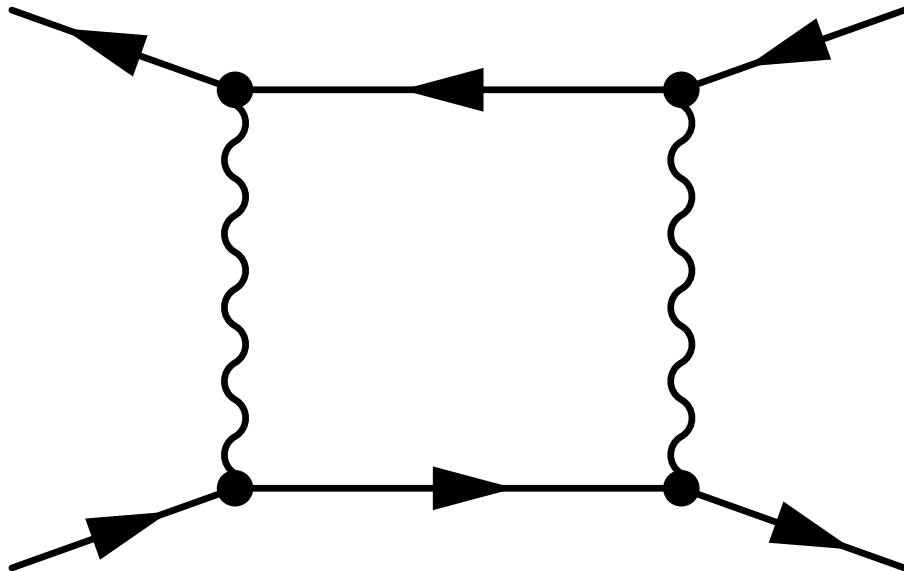
$$e^-\gamma \rightarrow \gamma e^-$$

Electrons here could be replaced by other objects with electric charge. Note that Feynman diagrams so far just look like pictorial ways to represent processes, but they can be used for much more, as we'll see

We can start to combine these...

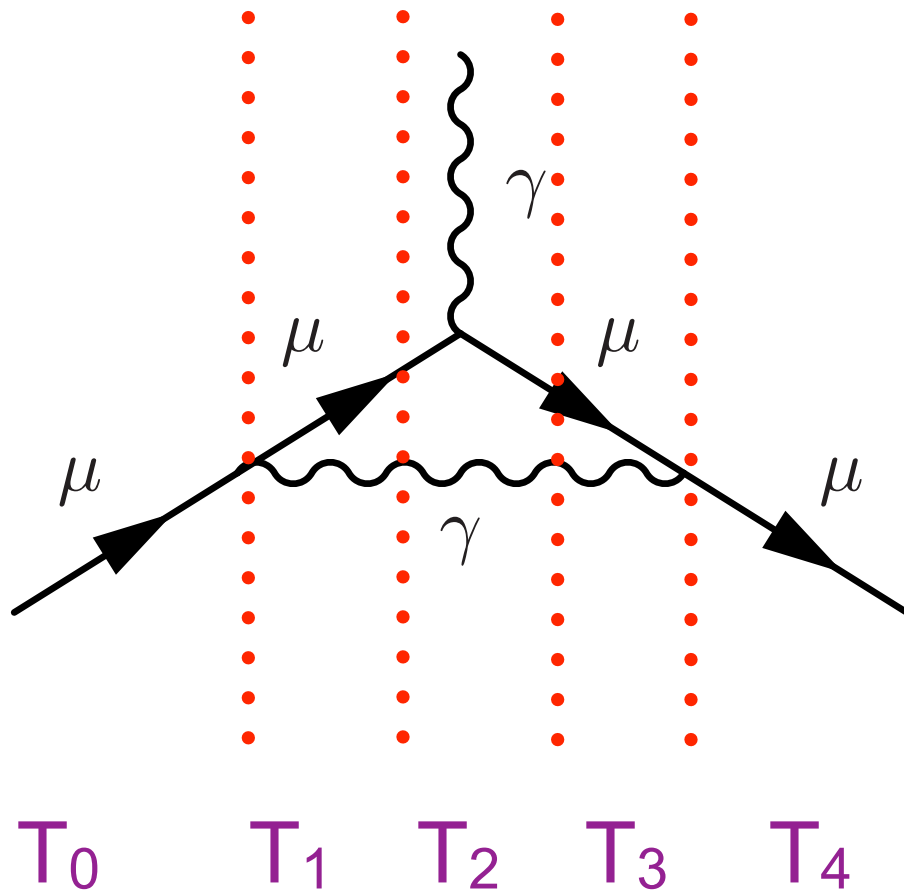


What is this? Does it remind you of any experiment that NIU works on? :)



Modification to Bhabha scattering (same initial and final states, different diagram)

Let's take a closer look at these diagrams



T_0 : Single initial muon

T_1 : Muon after interaction with photon, and that photon

T_2 : Some external photon, muon after interaction with one or two photons, the internal photon

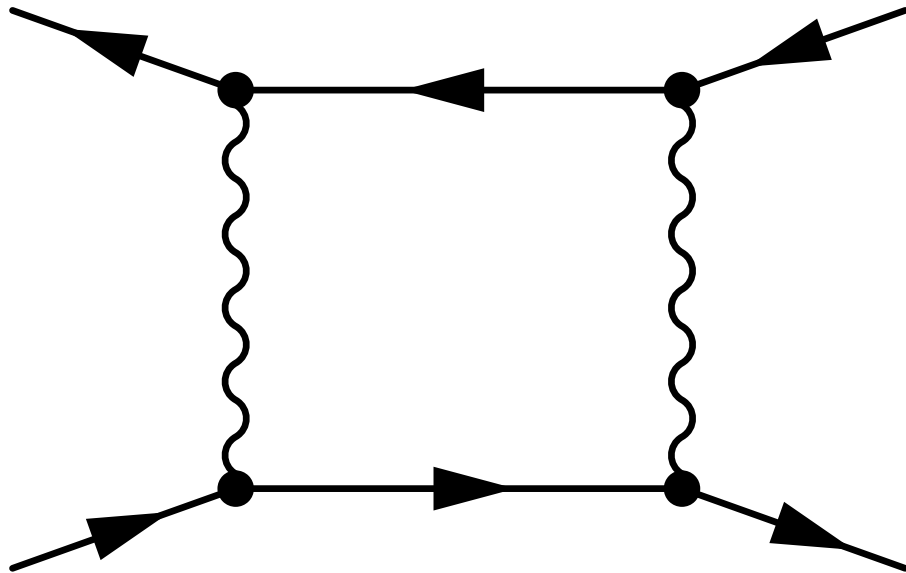
T_3 : Muon after interaction with external photon, before reabsorbing the internal photon

T_4 : Single final muon

Let's slice this up into different time bins

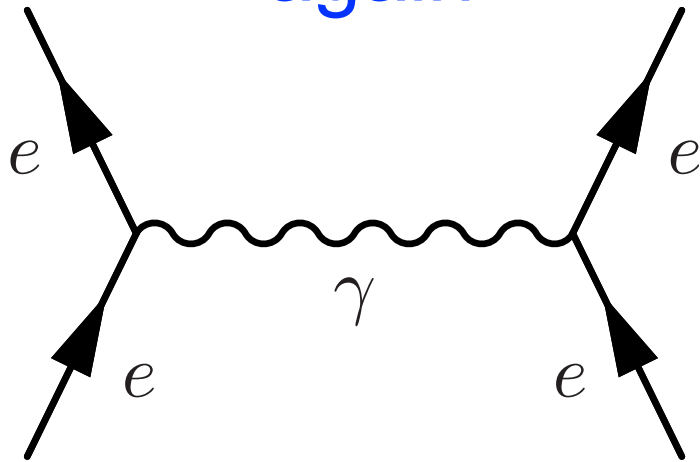
Can cleanly divide into **internal** and **external** particles

Let's take a closer look at these diagrams

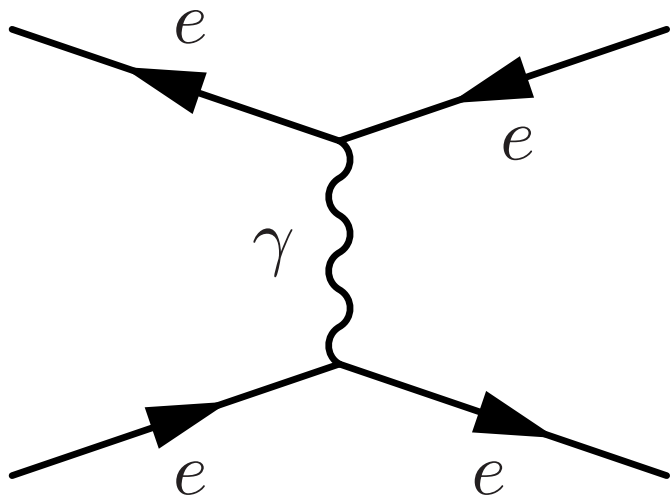


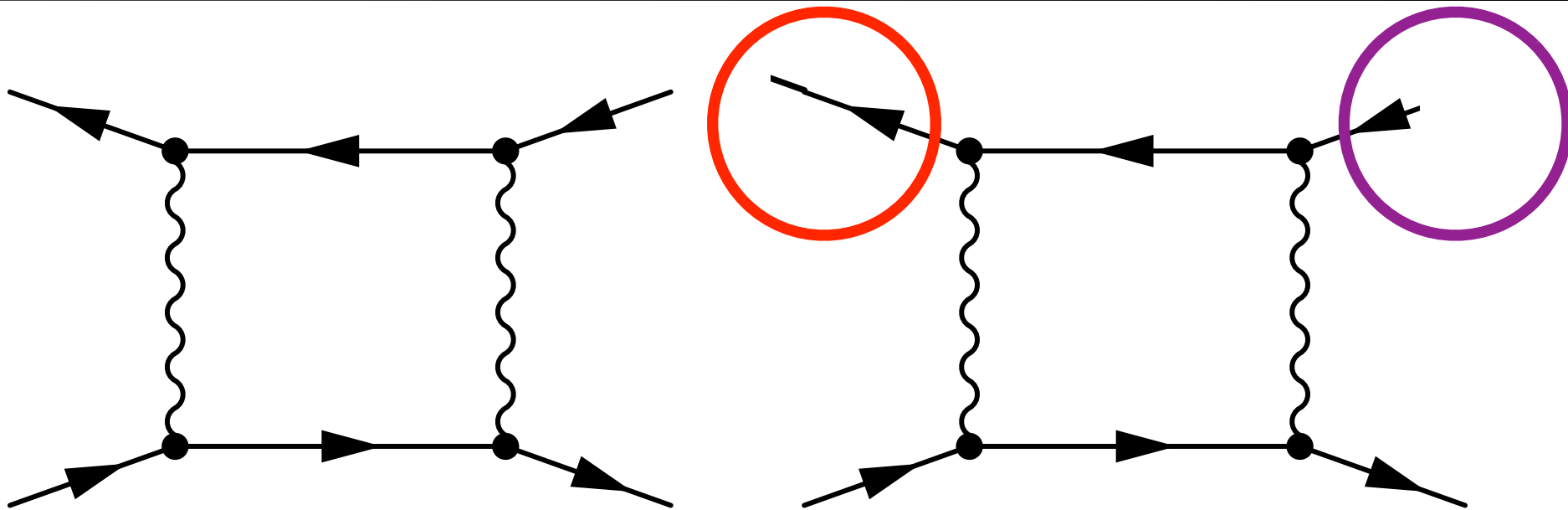
There are eight different particles in this diagram. Four of them are **external** to the diagram and **can be observed**.

The other four are **internal** to the diagram and are called **virtual particles** and do **not** have to have on-shell mass

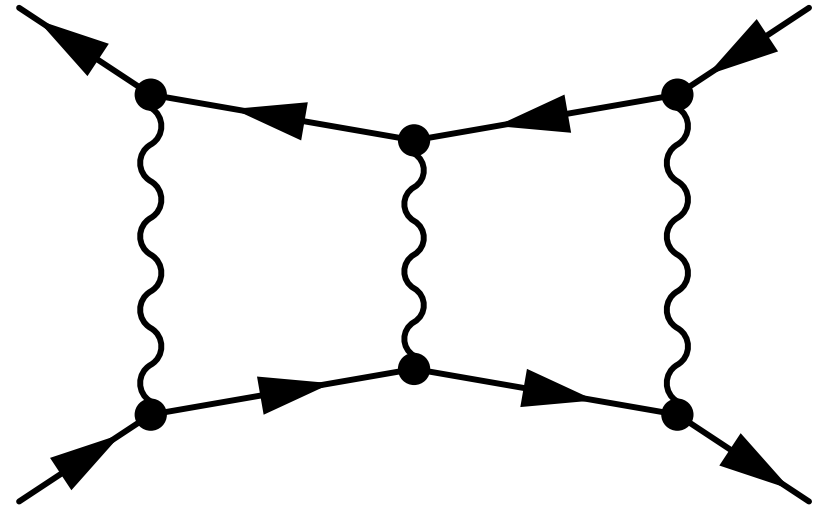
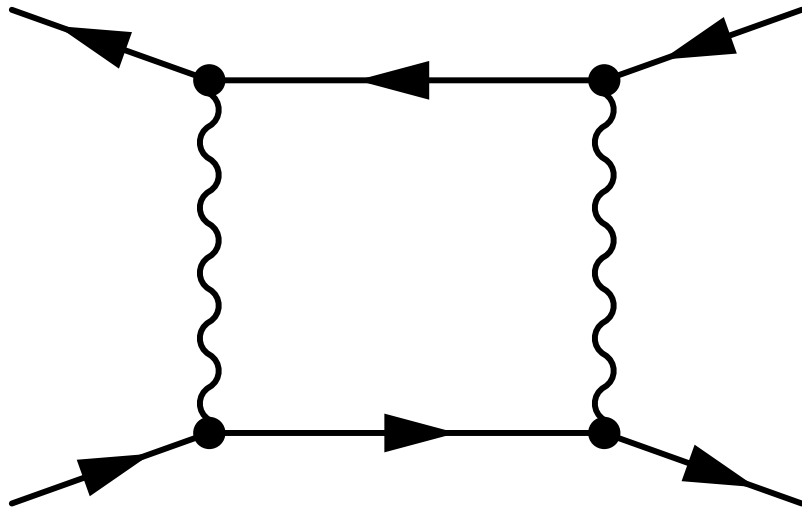
Bhabha scattering
again

Virtual particles here (the photon in each diagram) cannot be observed, since the initial and final states are the same, so these much have interfering matrix elements

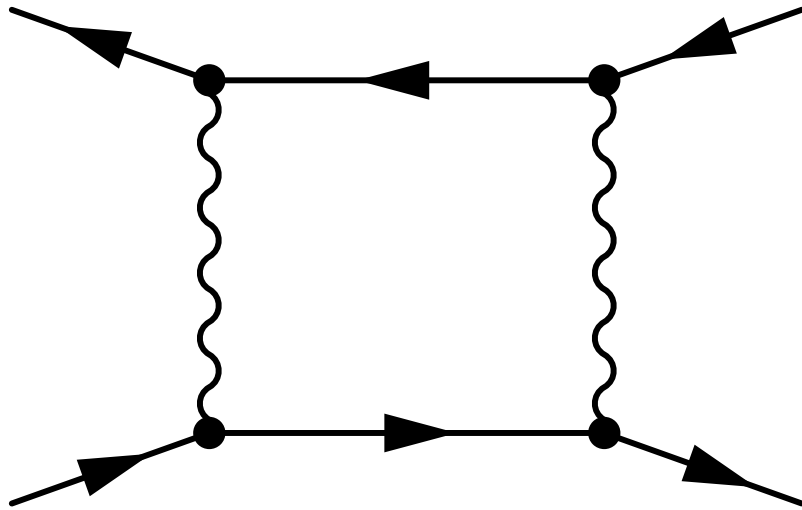




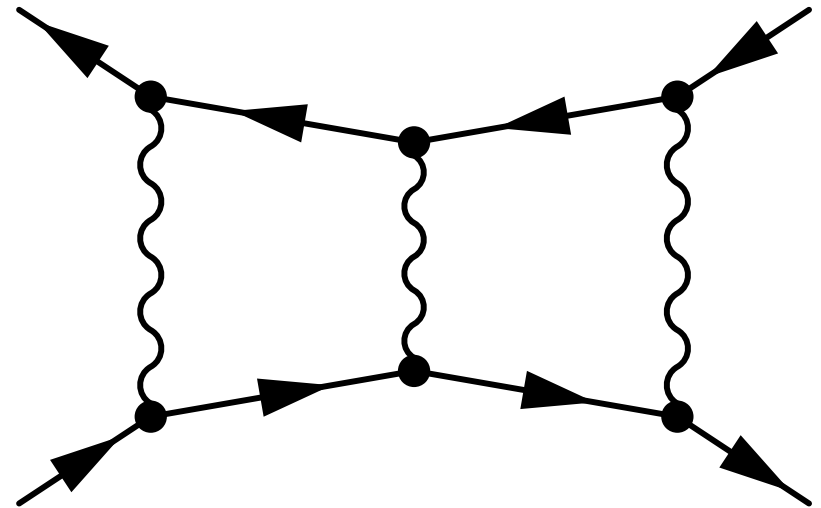
Have **extended one line** and **shrunk another**. Could have spaced things further apart or closer together - we do not differentiate between these sorts of things, nor the angle of the lines (**we are not artists, here, or at least, I am not**)



Again, can't distinguish these diagrams.
So the observable scattering amplitude
must be due to the sum of all such
diagrams ... but there are an infinite
number of them! Let's draw another few

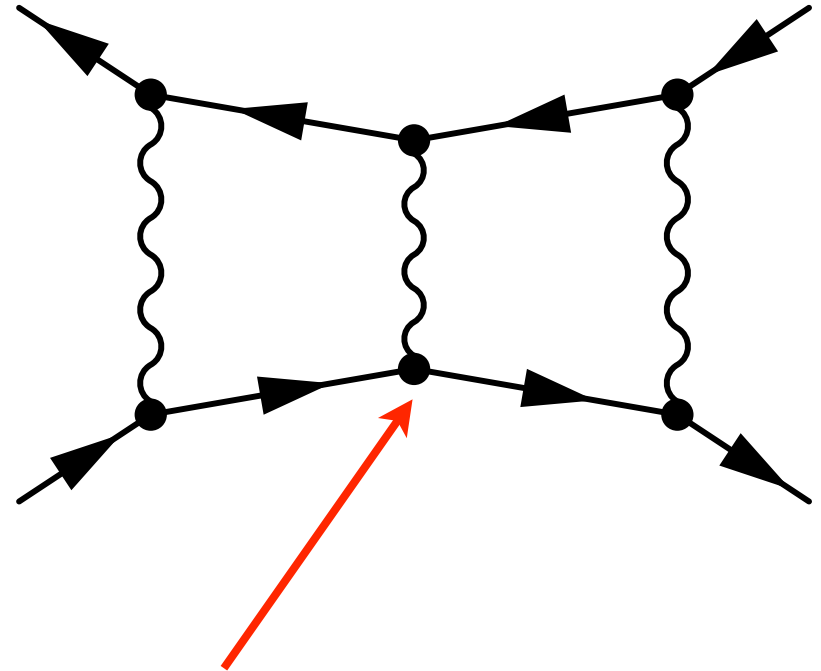
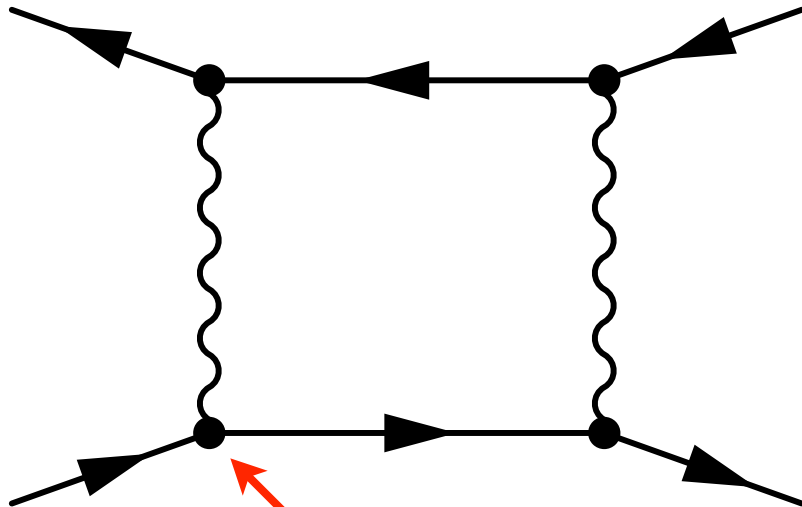


$$e^+e^- \rightarrow e^+e^- \rightarrow e^+e^-$$

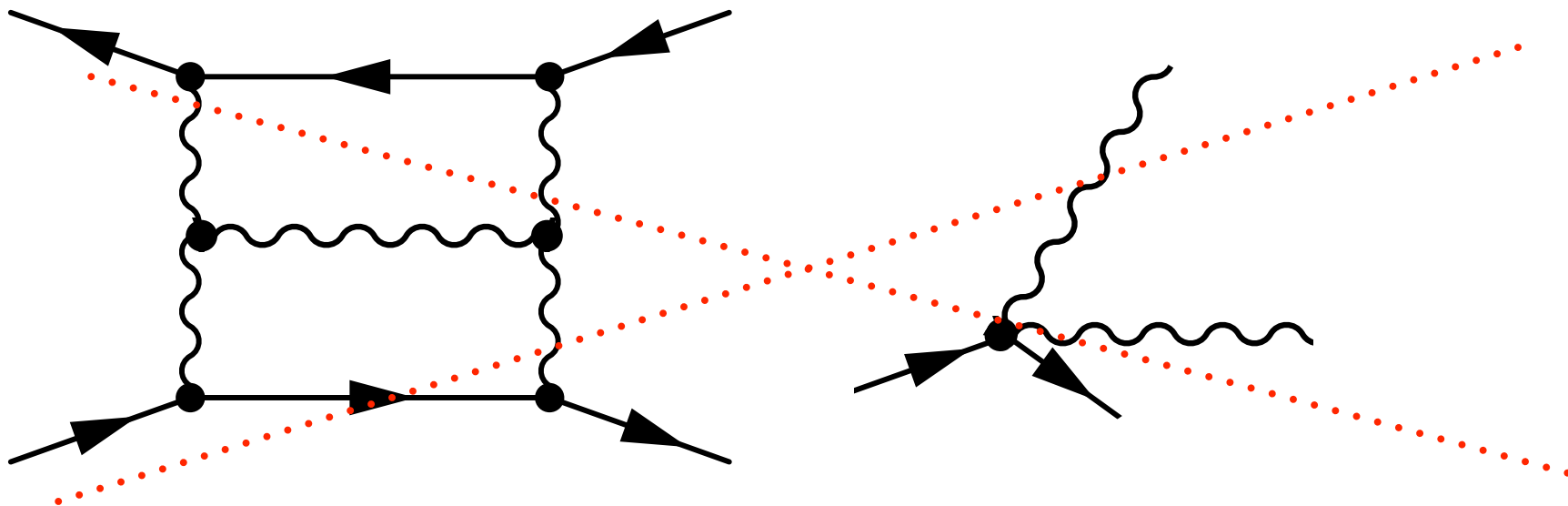


$$e^+e^- \rightarrow e^+e^- \rightarrow e^+e^- \rightarrow e^+e^-$$

$e^+e^- \rightarrow e^+e^-$ in both cases, since intermediate states are not observable. You might ask why we're bothering to draw such pictures, but they will shortly become an invaluable computation tool. Each of these represents a single number!



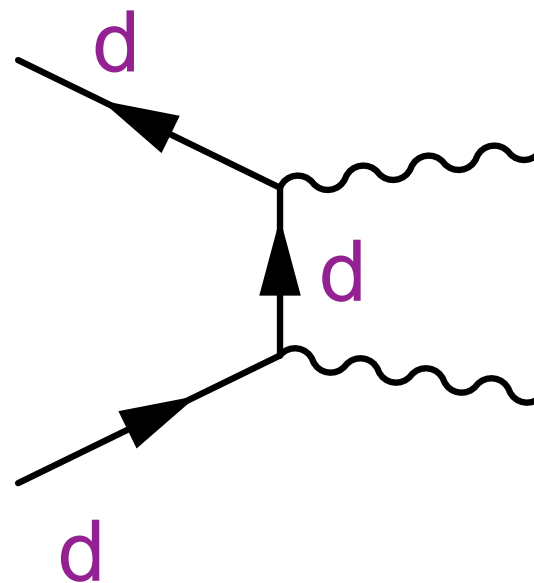
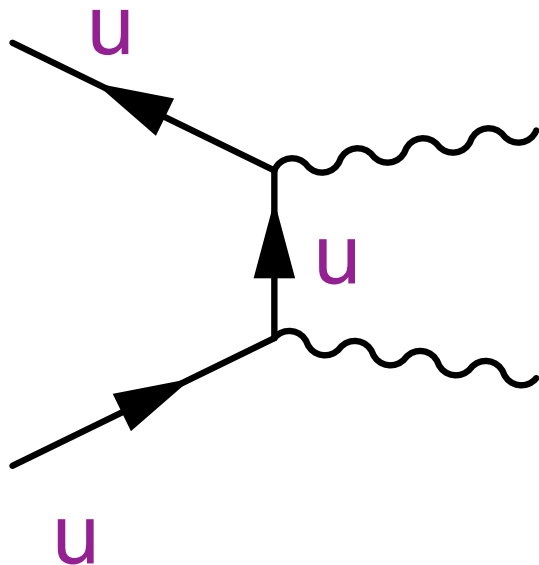
You may have noticed that I started putting circles at each interaction point - these are **vertices** and describe a point in space-time where an interaction occurs.



There is no such photon-photon-photon vertex in the SM (of course, you should know that already - the photon does not carry electric charge)

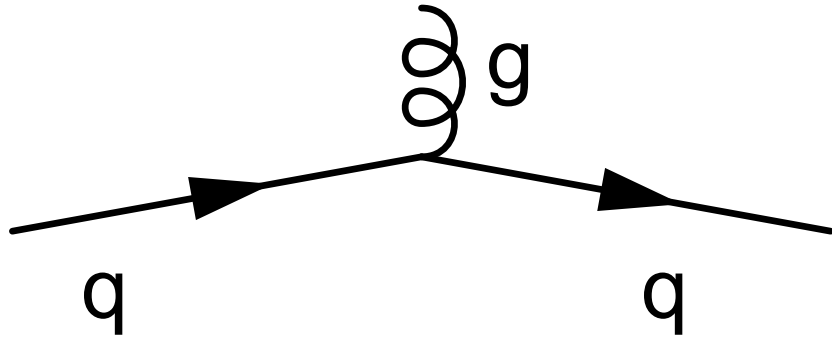
Muons can emit multiple photons, but not at the same vertex (note that the solid lines here represent any particle with electric charge)

Pair annihilation again, with quarks

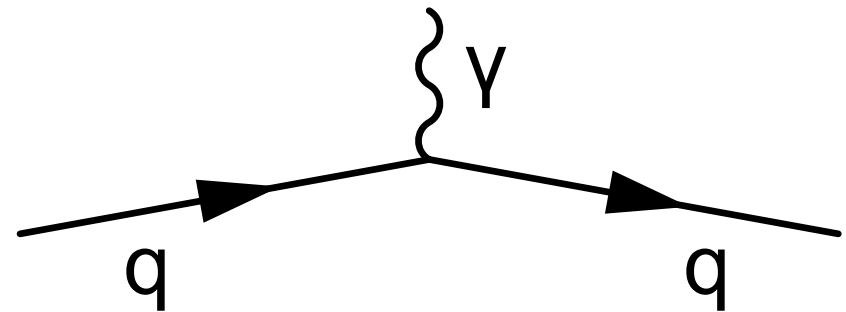


Now we can see why neutral pions decay 99% of the time to a pair of photons, and also why this happens so quickly (any good answers?)

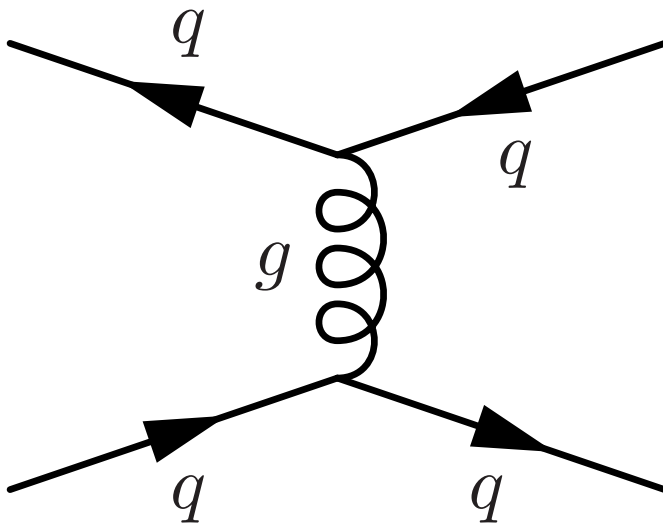
Start with common building block:



Note the similarity with the common building block of QED:

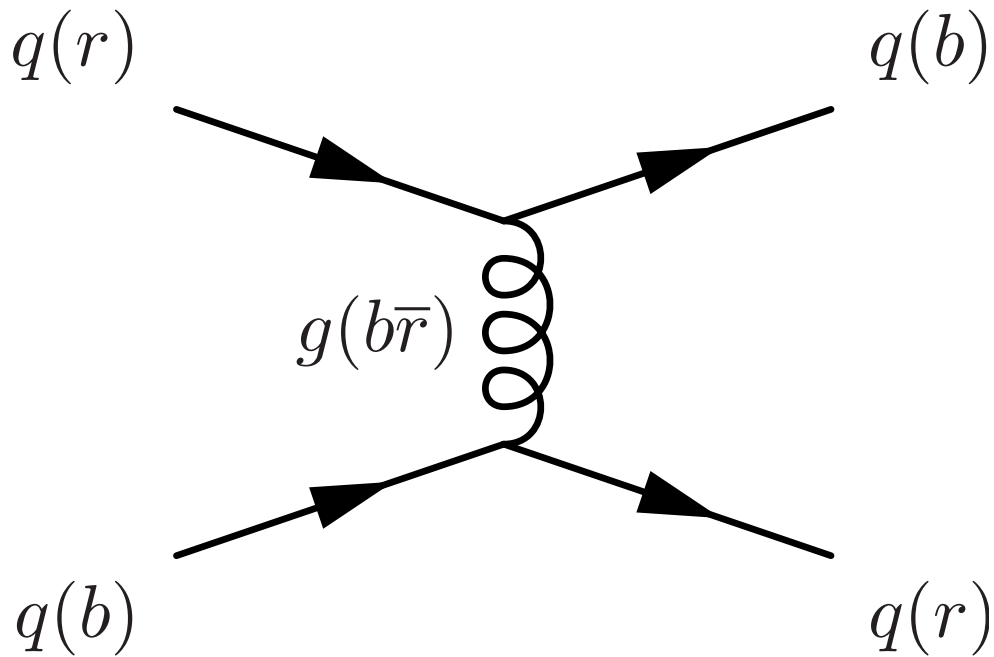


Gluon exchange between quark and anti-quark:



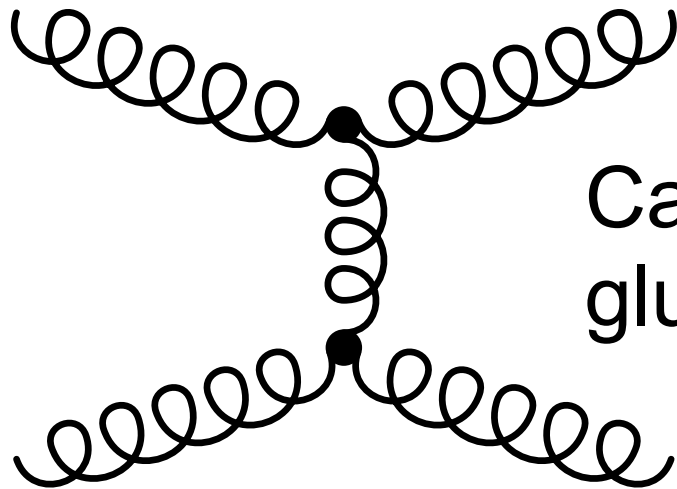
A few
fundamental
differences,
though, between
QED and QCD...

Gluon exchange between quarks:



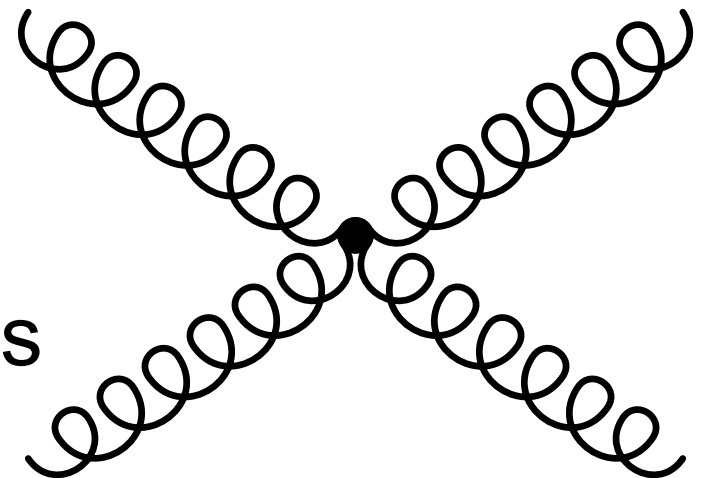
Remember that quarks have color (and so do gluons!) Try and follow the color lines (always a good thing to check)

Remember that gluons themselves have QCD color, so they self-couple!



Can have three-gluon vertices

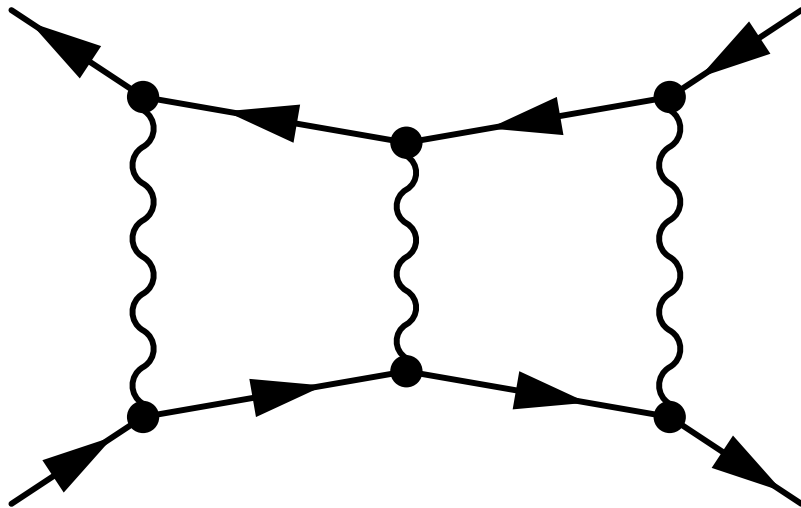
And four-gluon vertices



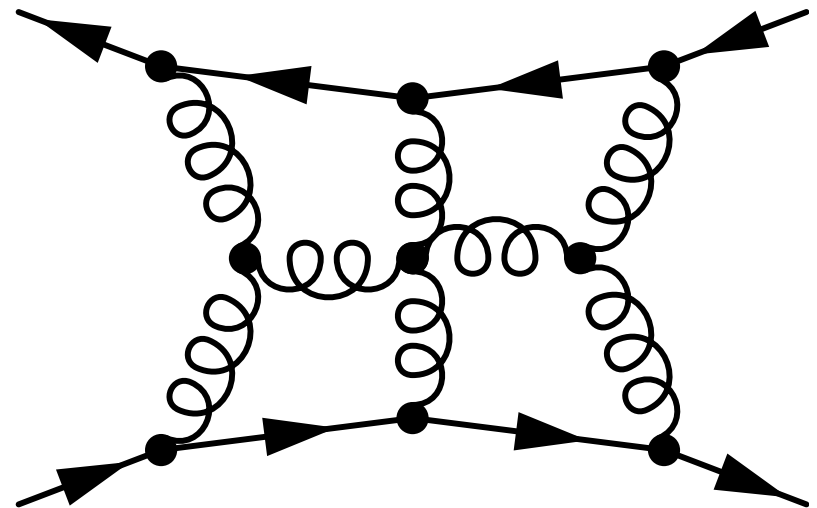
One other QED vs QCD differences

Each vertex describes an emission/absorption of a force carrier.

In QED, the probability of this is governed by the unit-less number $\alpha=1/137$, which is good, since it means the probability for many of these is small



In QCD, the probability of this is governed by the unit-less number $\alpha_s > 1$, which means the diagrams with more vertices contribute ... more!





Running of the coupling constant

The value of the coupling constant is indeed strong, but only at large distances. At small distances (such as inside of a proton), the strong coupling constant gets very small and we can calculate quantities

The property that the coupling gets weaker at smaller distances (aka at larger energies) is known as **asymptotic freedom**



Nobel prize for
Wilczek, Gross and
Politzer

As Griffiths points out...

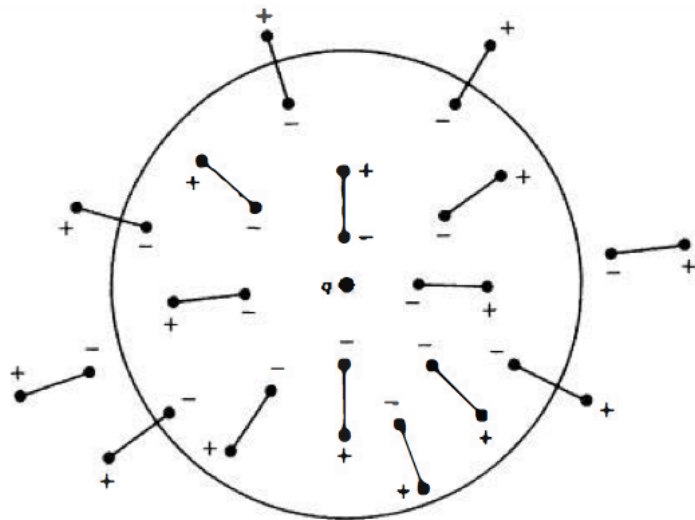


Fig. 2.1 Screening of a charge q by a dielectric medium.

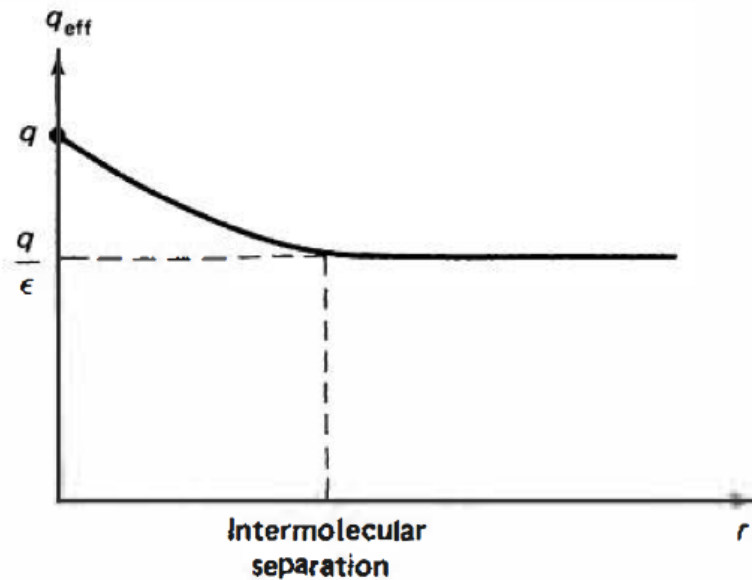
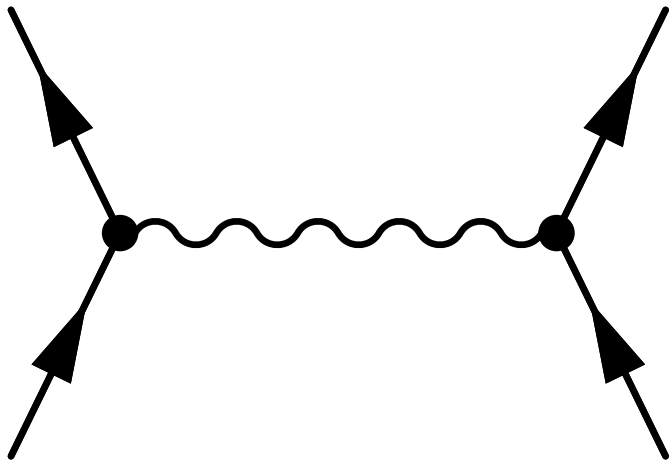


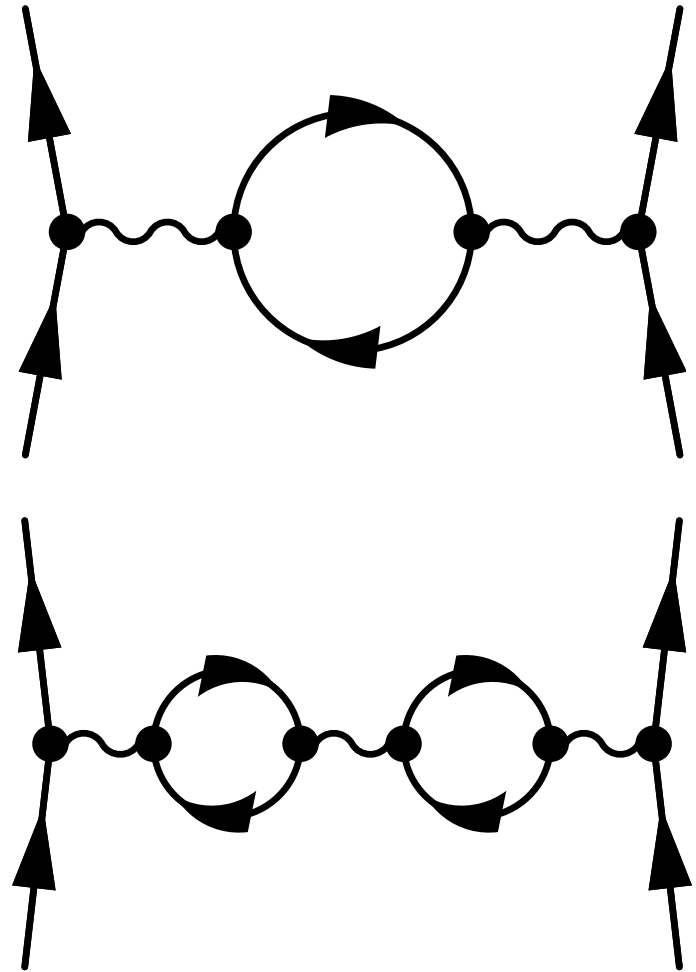
Fig. 2.2 Effective charge as a function of distance.

In classical E&M, the coupling is given by the charge q , and this is reduced at large distances by a dielectric

Bhabha
scattering again



Virtual diagrams
contributing



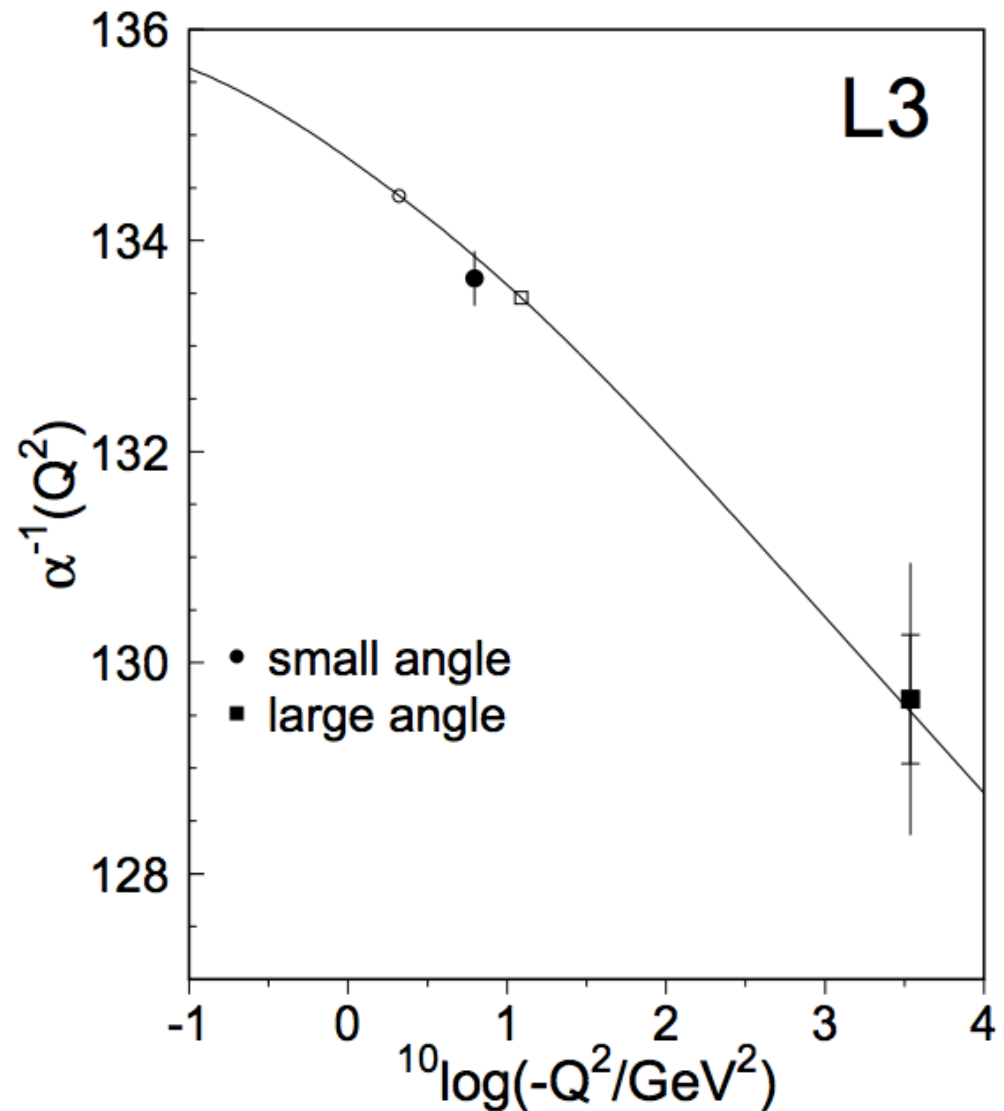
Running of the E&M fine structure constant

~1/137 at zero
momentum transfer

~1/127 at the Z
boson mass!

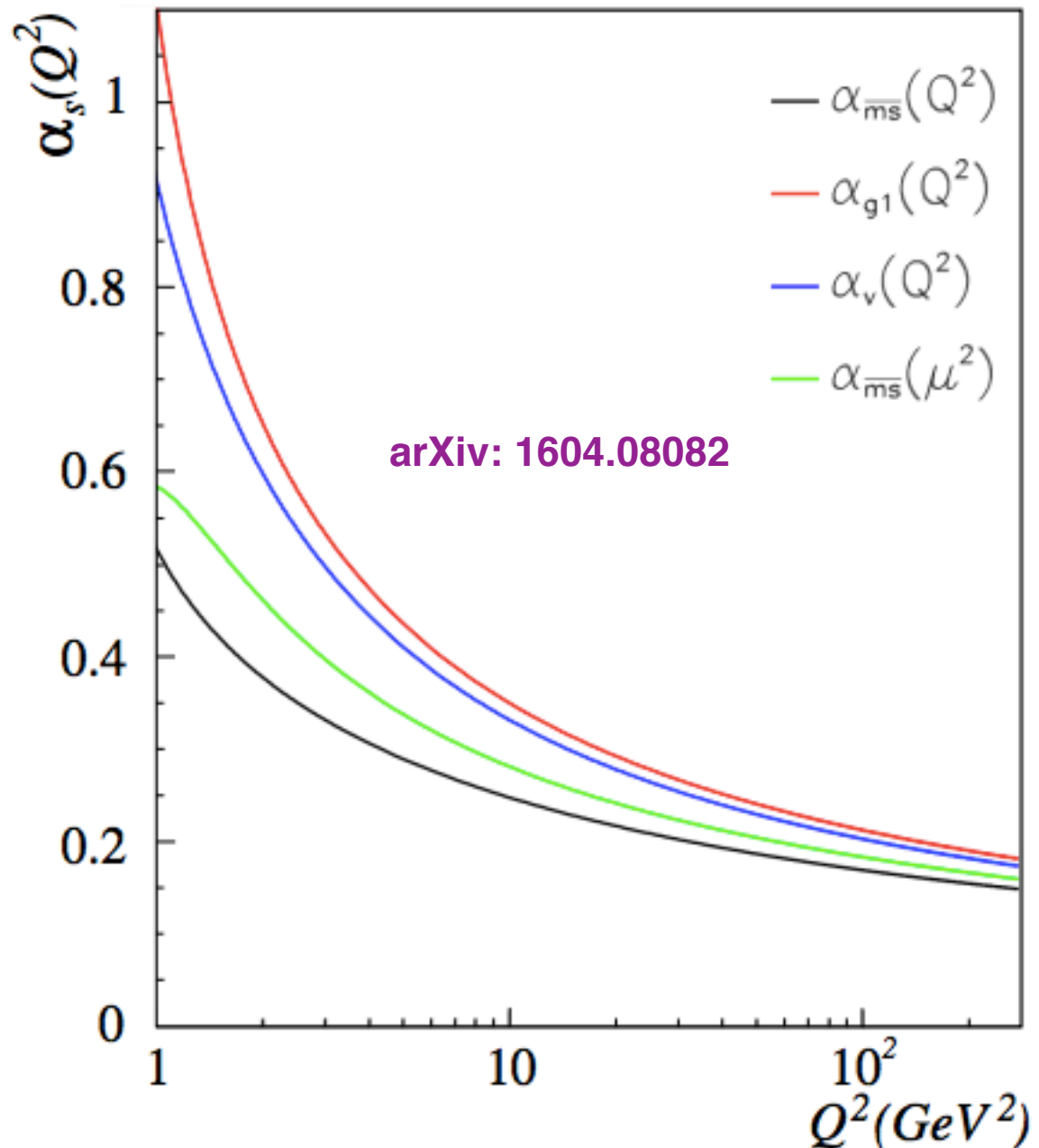
These are **vacuum
polarization** effects

hep-ex/0002035v1



Running of the QCD strong coupling constant

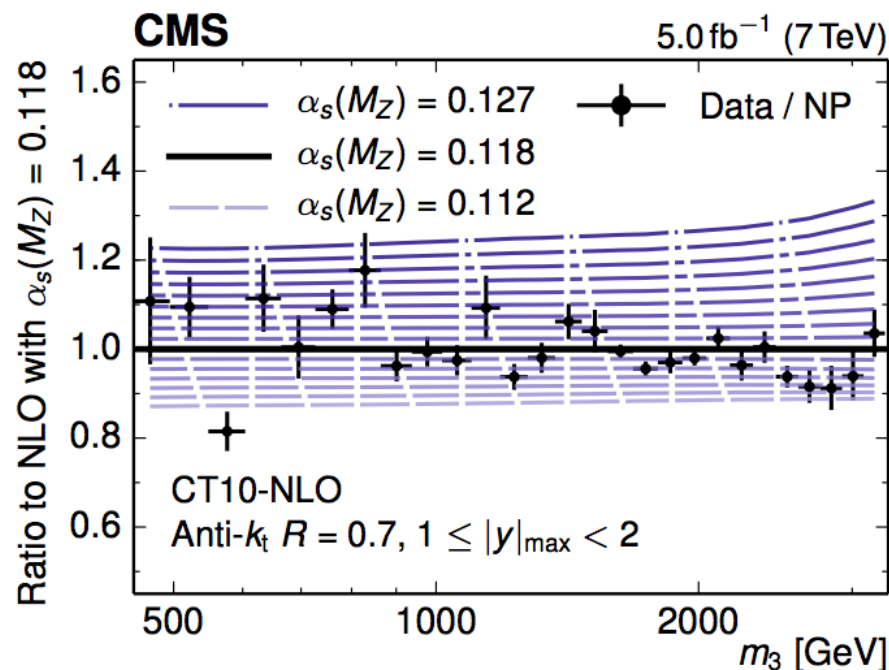
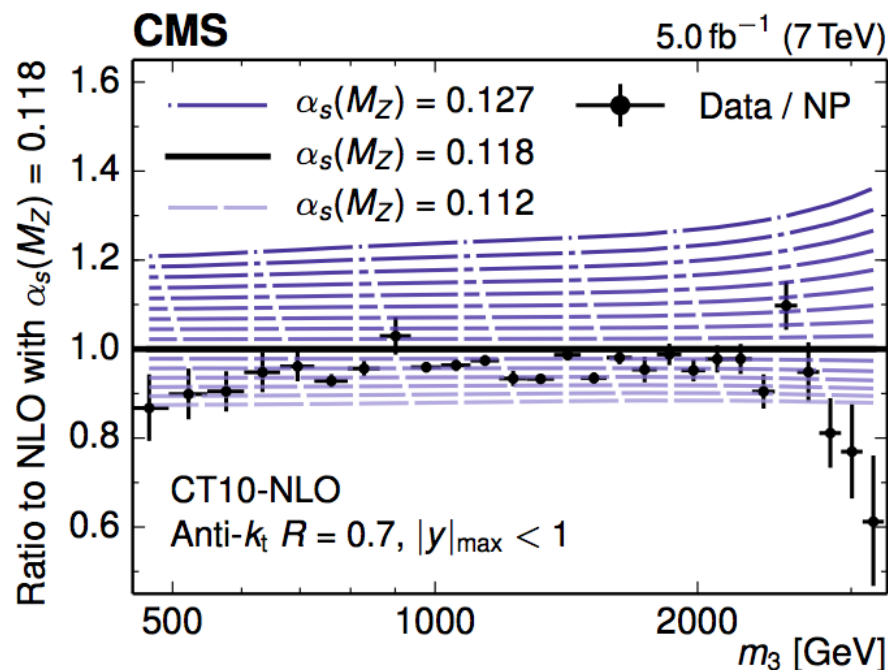
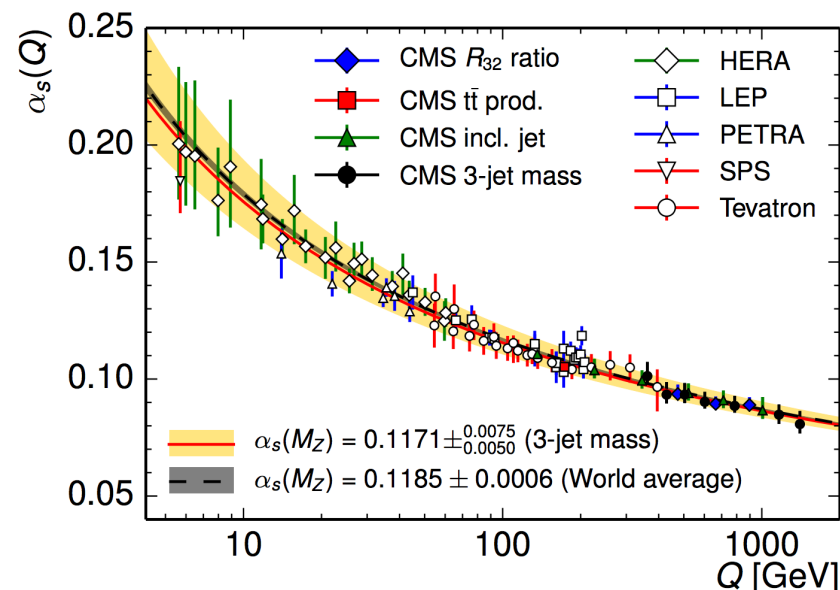
Large “running” of the coupling quite evident. Different colors are different “renormalization schemes” - we’ll get to that in a little bit, but consider it different coupling definitions



Can measure this in a variety of ways

Use trijet mass to determine the strong coupling constant!

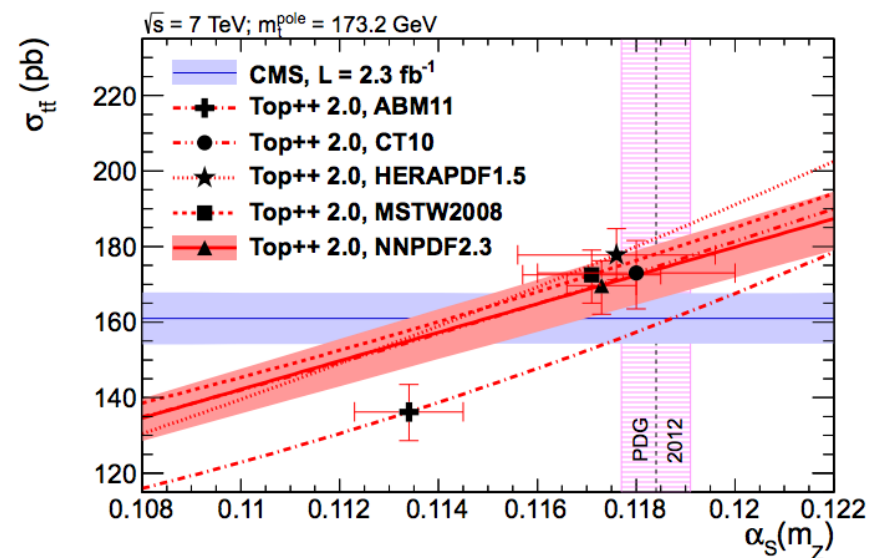
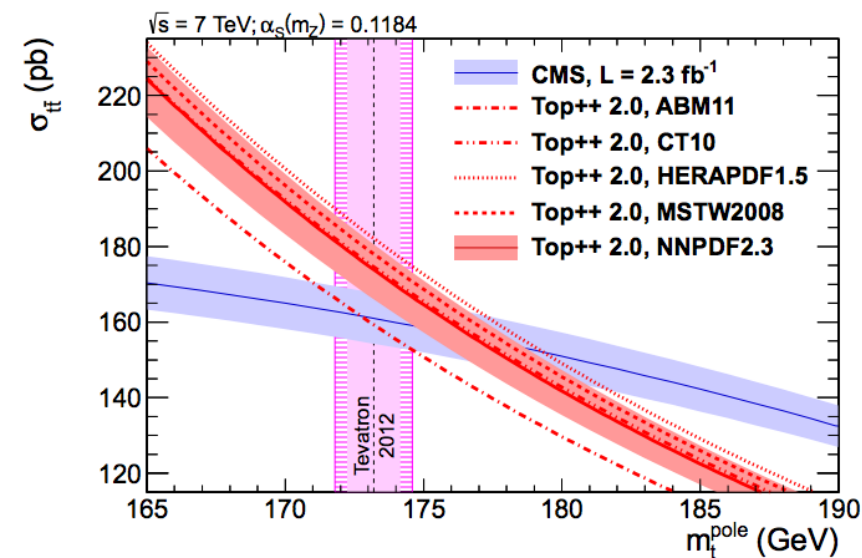
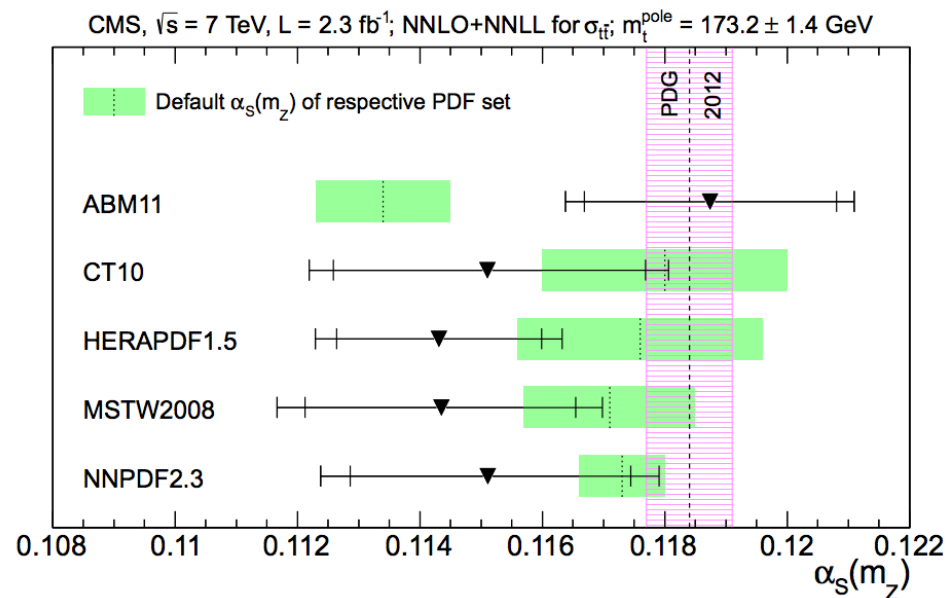
arXiv: 1412.1633



Can measure this in a variety of ways

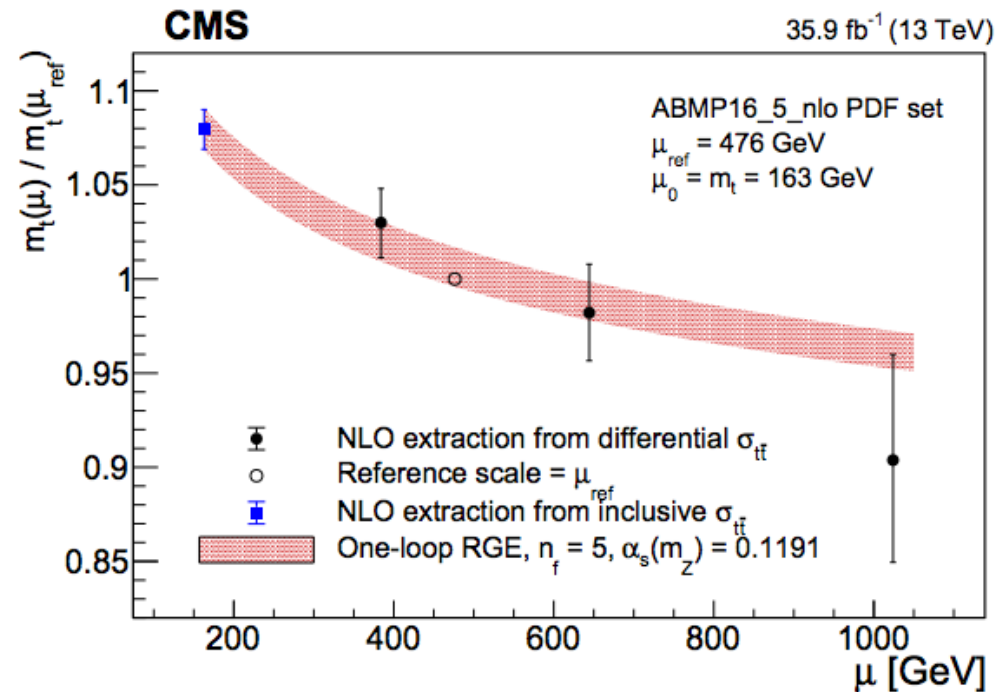
Use $t\bar{t}$
production cross
section instead!

arXiv: 1307.1907



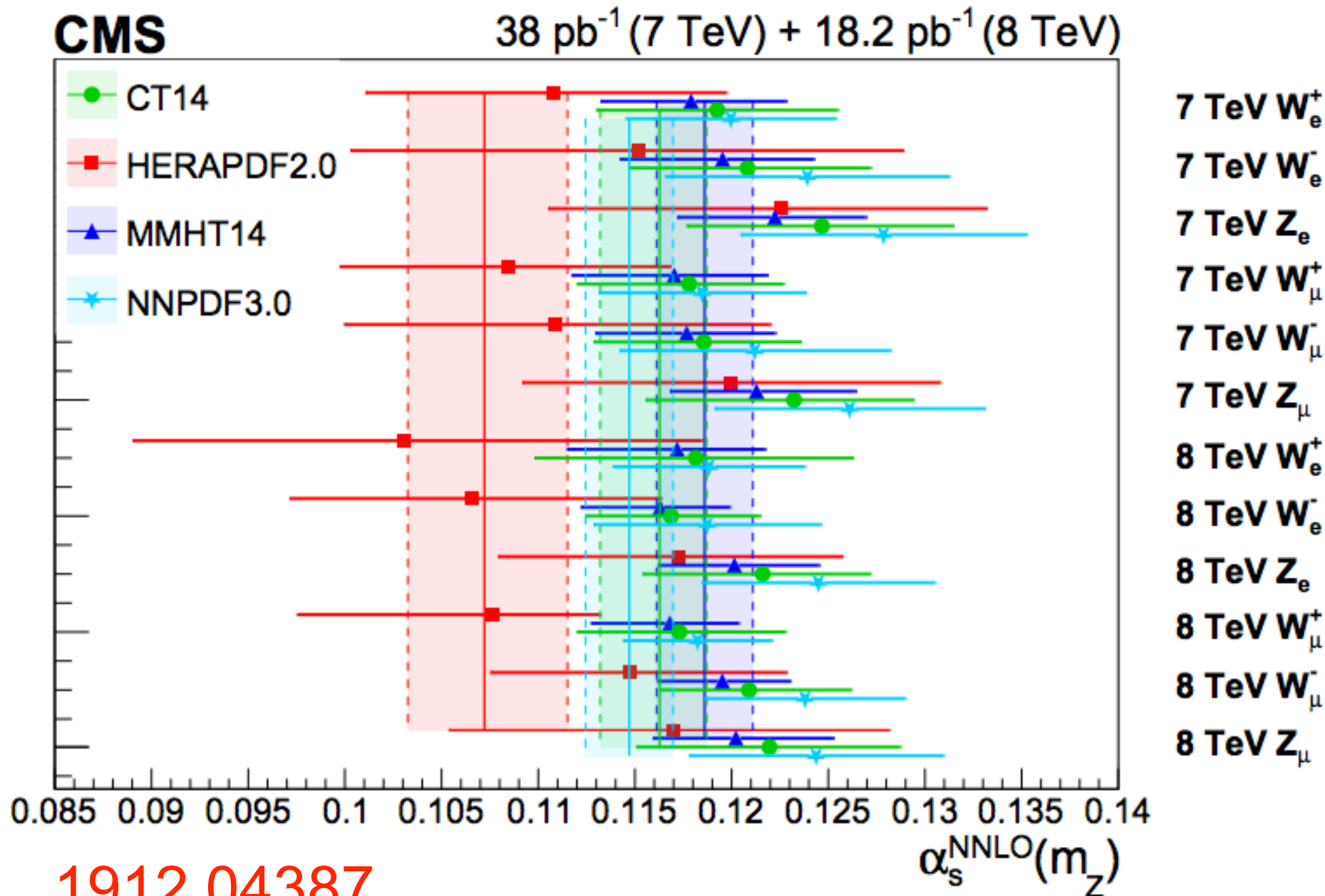
Masses of objects are also not single numbers!

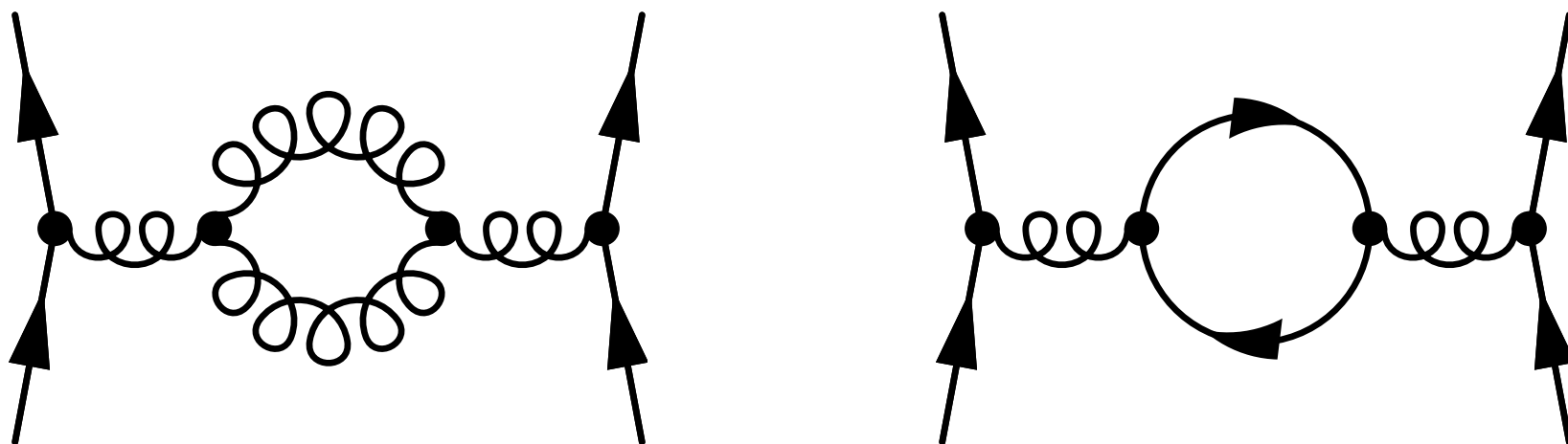
The “mass” of the top quark depends on the energy scale of the collision! Use the differential cross section vs $m_{t\bar{t}}$ as a proxy for this



arXiv: 1909.09193

Measurement of strong coupling from V cross sections





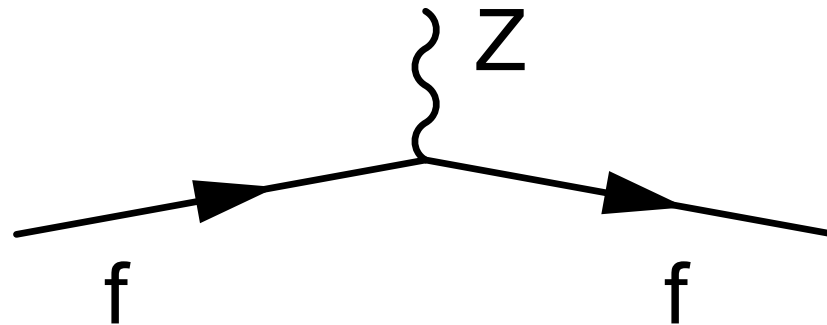
Effects from quark polarization and gluon polarization give opposite effects!

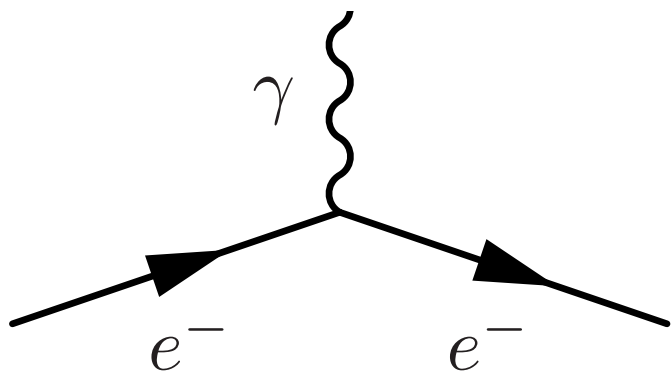
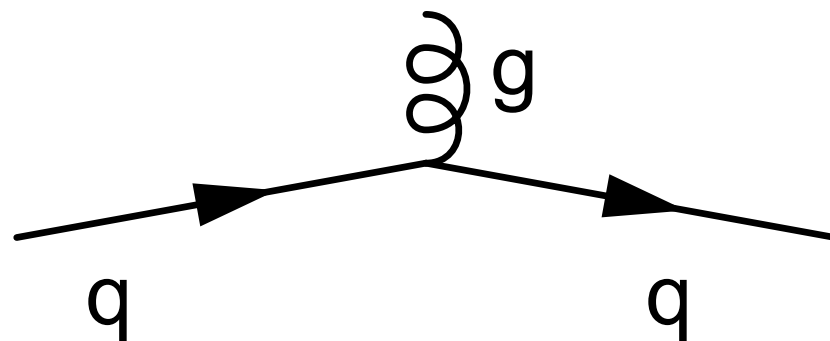
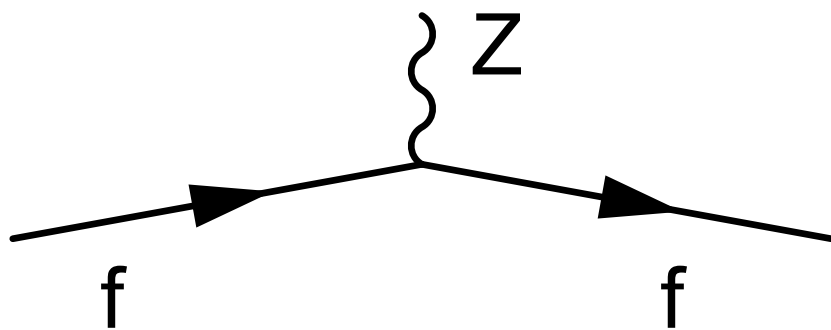
$a=2f-11n$ (f =number of flavors, n =number colors)

defines whether coupling increases or decreases at short distances

$f=6, n=3 \rightarrow a < 0 \rightarrow$ asymptotic freedom (upper limit on no more than 17 generations of quarks)

where f here
is any fermion (Z boson couples to all quarks,
charged leptons and neutral leptons)

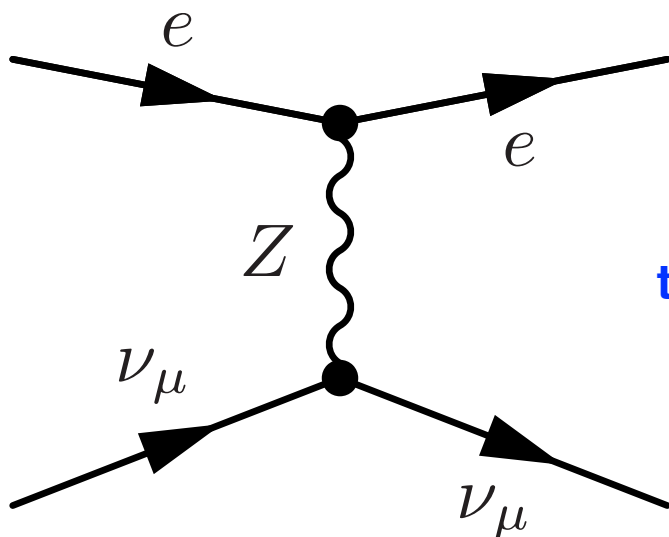




Griffiths uses a jagged straight line for EW bosons, but I will not. Just be careful, regardless of your choice!

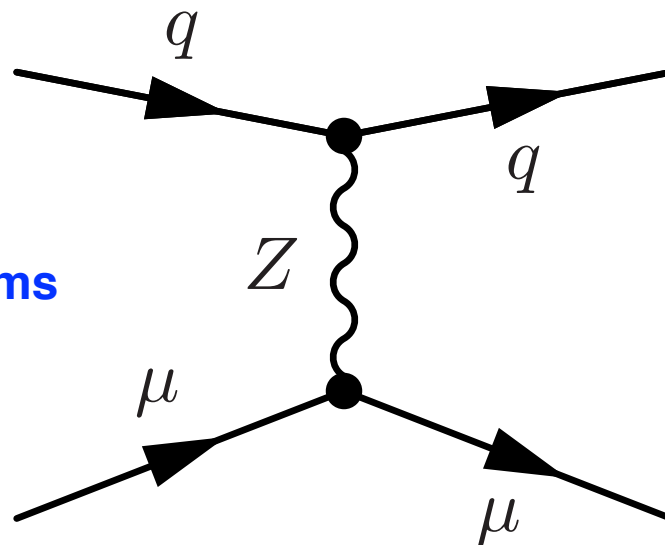
What processes can the Z boson mediate?

$$e^- \nu_e \rightarrow e^- \nu_e$$

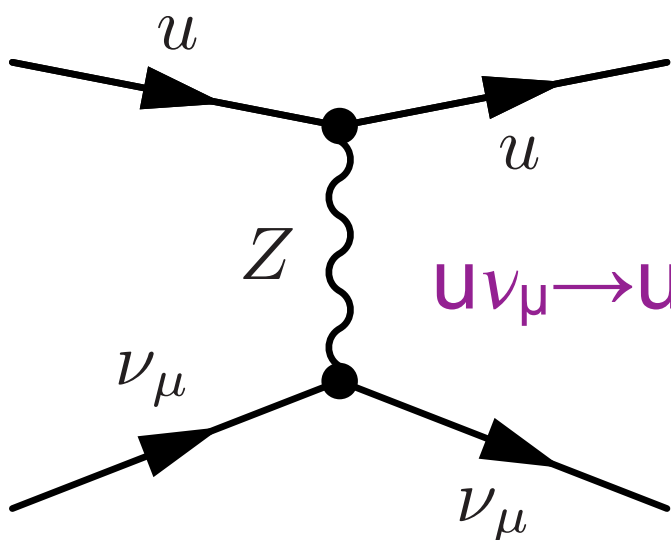


t channel diagrams

$$\mu^- q \rightarrow \mu^- q$$

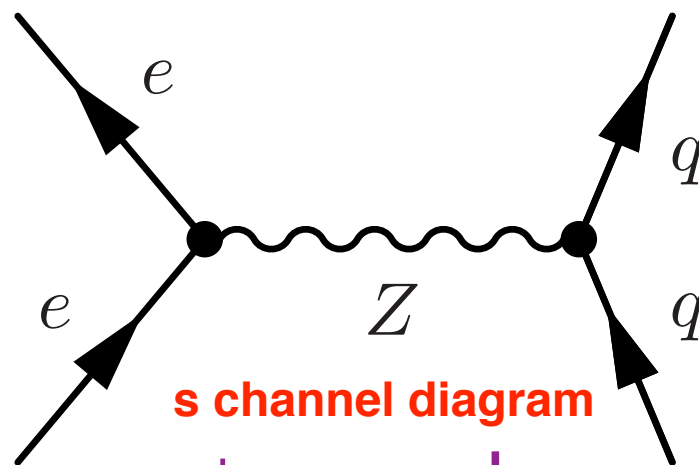


$$u \nu_\mu \rightarrow u \nu_\mu$$

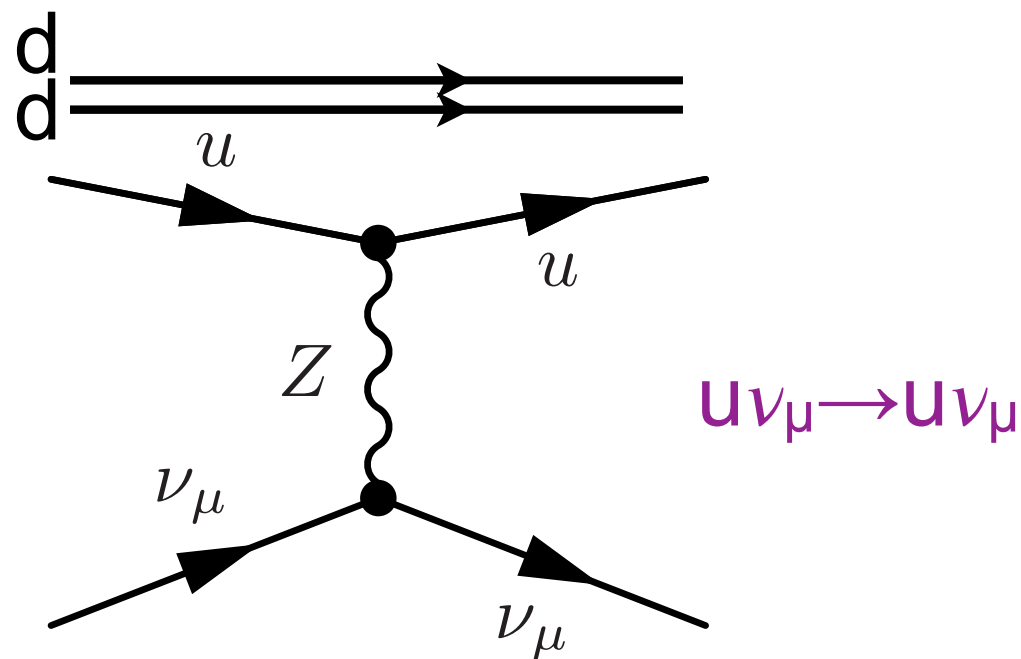


s channel diagram

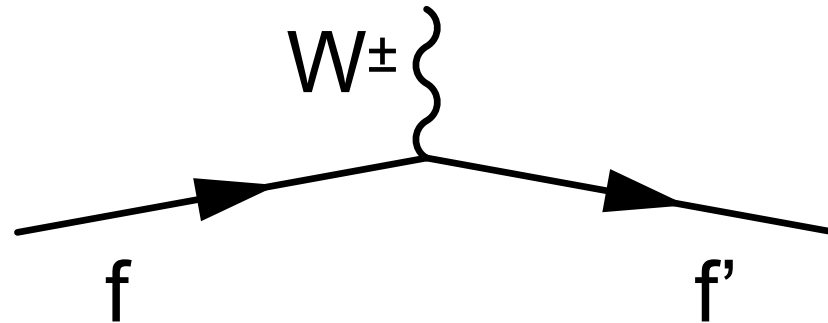
$$e^+ e^- \rightarrow q \bar{q}$$



We of course don't scatter the bare quarks, but quarks inside hadrons (here inside a neutron)

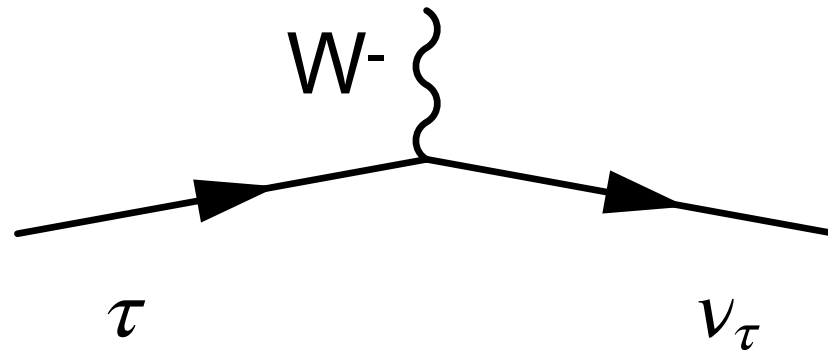


Remember that W bosons are the only ones involved in change of flavor or type of matter



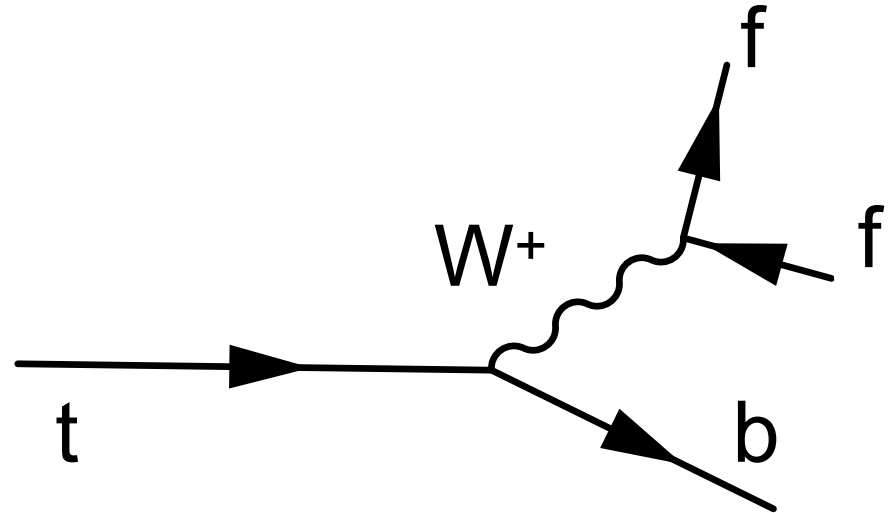
Remember that W bosons are the only ones involved in change of flavor or type of matter.

Example, a tau converts into a tau neutrino and a W boson:



Top quarks decay nearly $\sim 100\%$ of the time to a W boson and a bottom quark. The W boson can decay to a quark-antiquark pair, or to a charged lepton and a neutrino

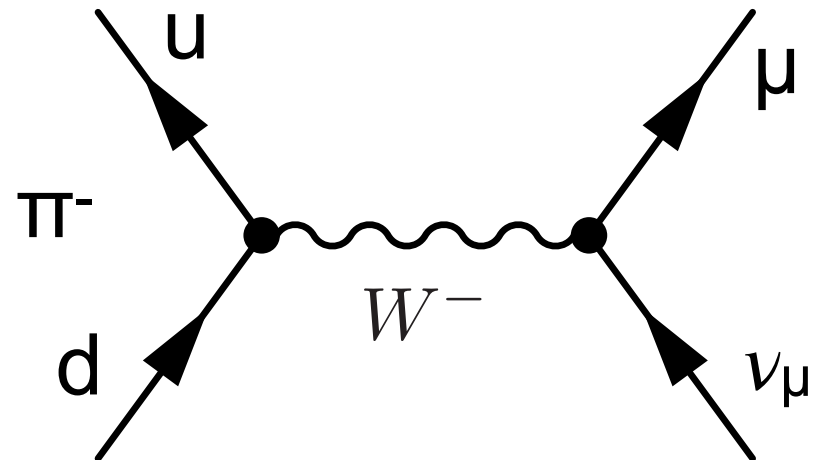
Check lepton
flavor numbers
and EM
charge!



Charged weak interactions

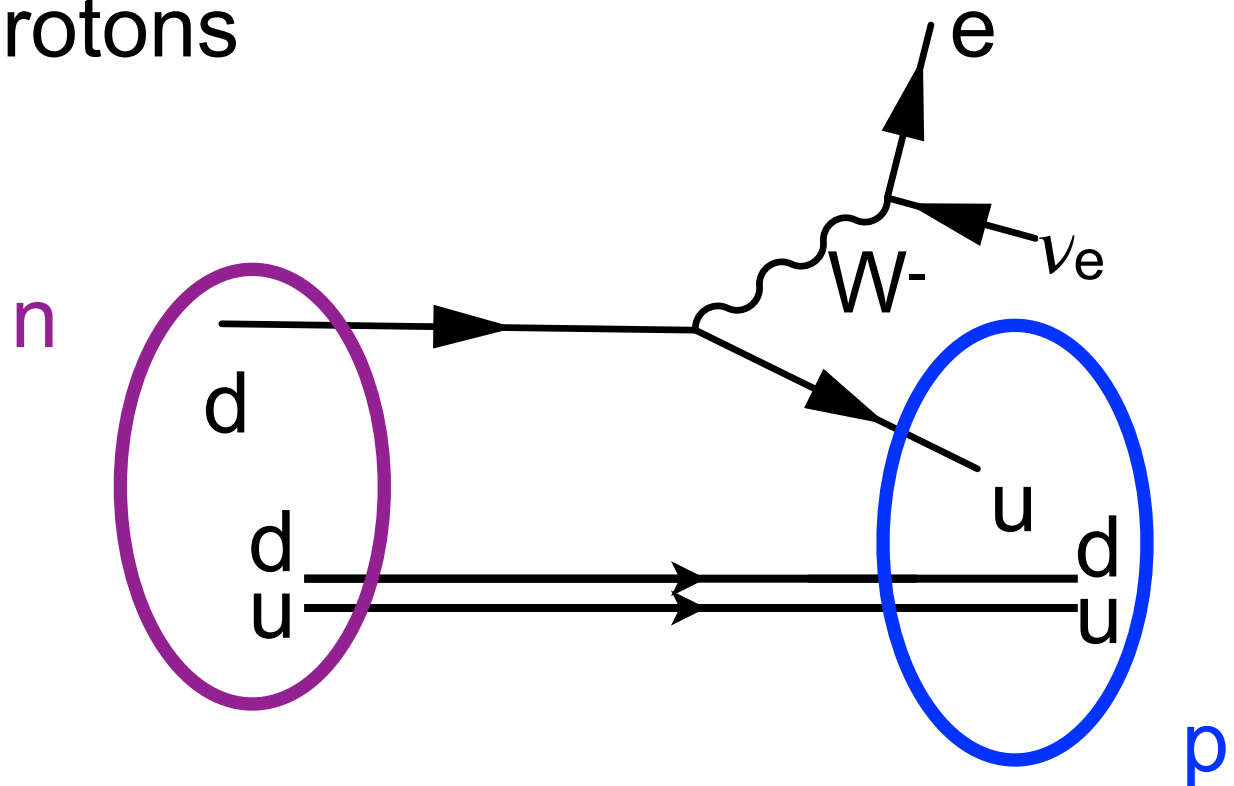
This is how a charged pion can decay to a muon (and an anti-muon neutrino). Could have guessed W boson involvement, because it involves a change of flavor (here charged pion decay is much slower than neutral pion decay)

Check lepton flavor numbers and EM charge!



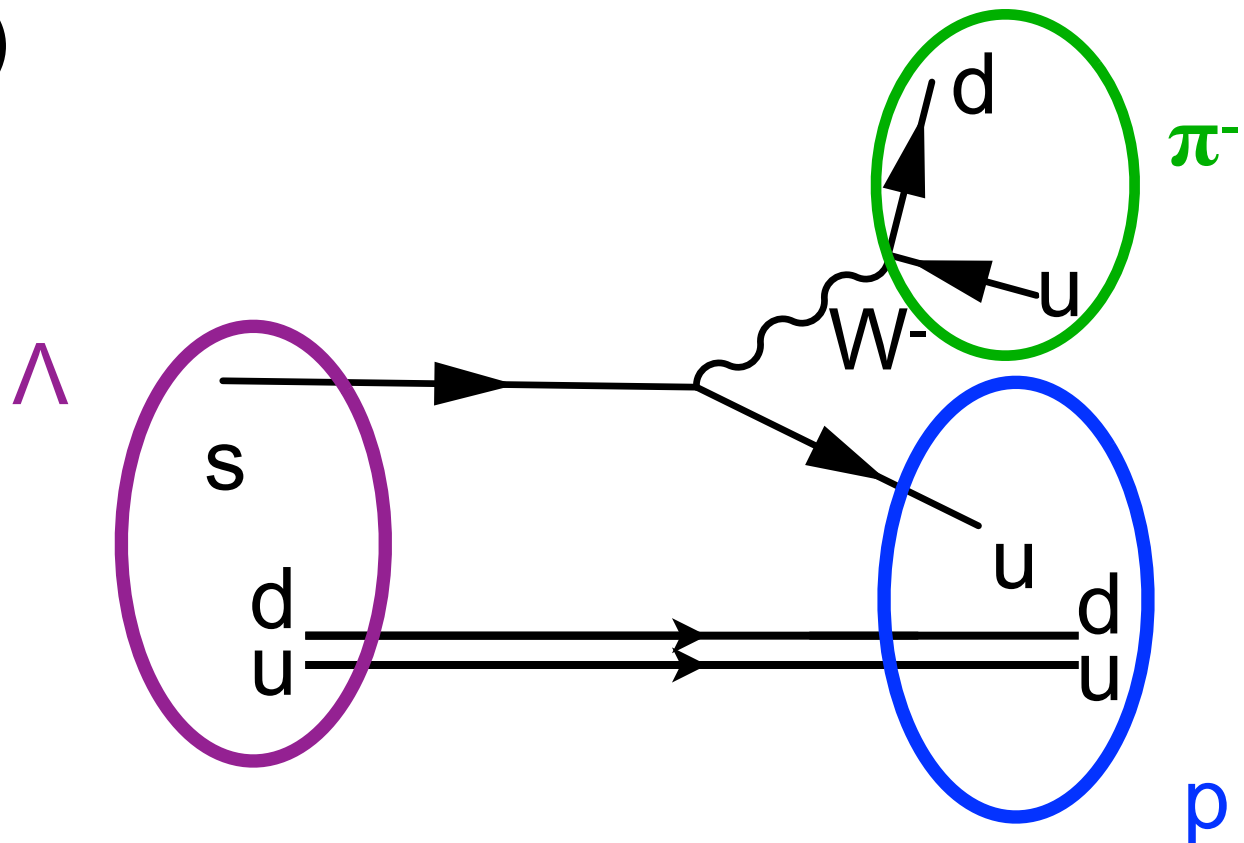
What processes can the W boson mediate?

We of course don't scatter the bare quarks, but quarks inside hadrons (here inside a neutron)
This is how neutrons beta-decay to protons



The important question...

How do we account for strangeness-changing weak interactions? (We know they have to come via the weak force, but so far we have only seen decays within a matter generation)



The weak force couples not to eigenstates of quarks that we observe, but to a slightly skewed set instead:

What we observe

$$\begin{pmatrix} u \\ d \end{pmatrix} \begin{pmatrix} c \\ s \end{pmatrix} \begin{pmatrix} t \\ b \end{pmatrix}$$

What weak force couples to

$$\begin{pmatrix} u \\ d' \end{pmatrix} \begin{pmatrix} c \\ s' \end{pmatrix} \begin{pmatrix} t \\ b' \end{pmatrix}$$

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

The Kobayashi-Maskawa matrix

What we observe

$$\begin{pmatrix} u \\ d \end{pmatrix} \begin{pmatrix} c \\ s \end{pmatrix} \begin{pmatrix} t \\ b \end{pmatrix}$$

What weak force
couples to

$$\begin{pmatrix} u \\ d' \end{pmatrix} \begin{pmatrix} c \\ s' \end{pmatrix} \begin{pmatrix} t \\ b' \end{pmatrix}$$

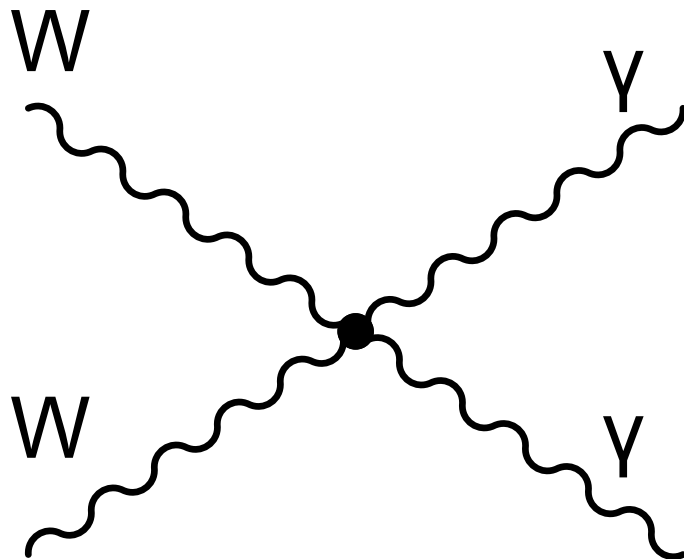
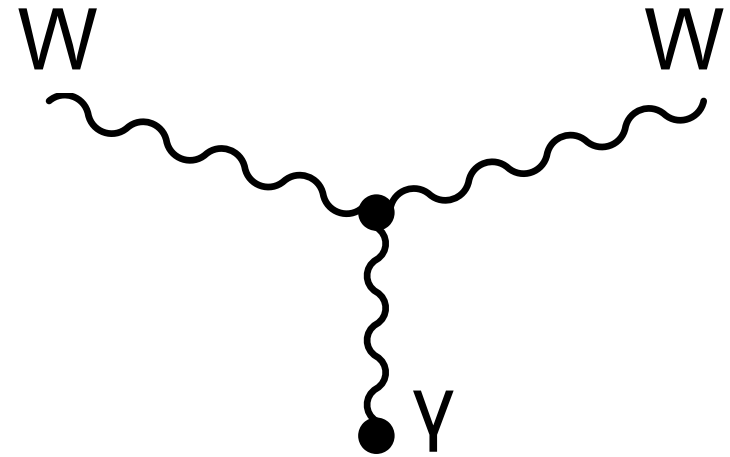
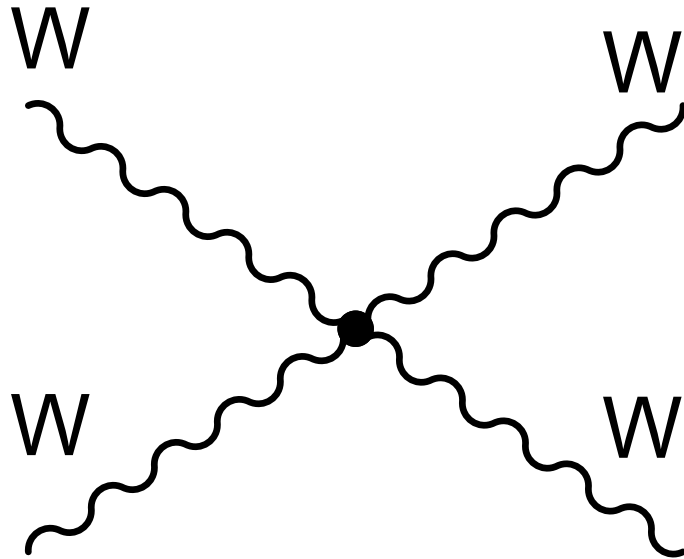
$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} 0.97434 & 0.22506 & 0.00357 \\ 0.22492 & 0.97351 & 0.0411 \\ 0.00875 & 0.0403 & 0.99915 \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix} \quad \text{2017 PDG}$$

Off-diagonal numbers are small, which has implications for which decays happen more/less frequently. **The matrix has to be unitary.** Note that I've cheated a bit, because there are phases in the matrix that I have ignored so far

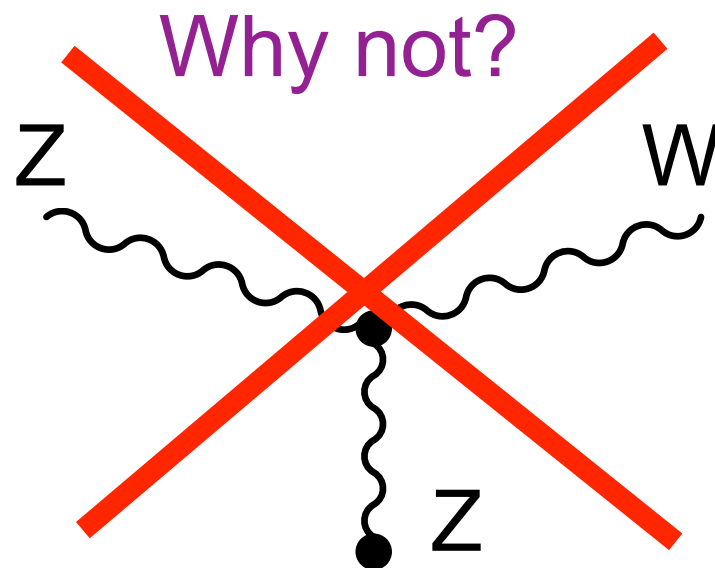
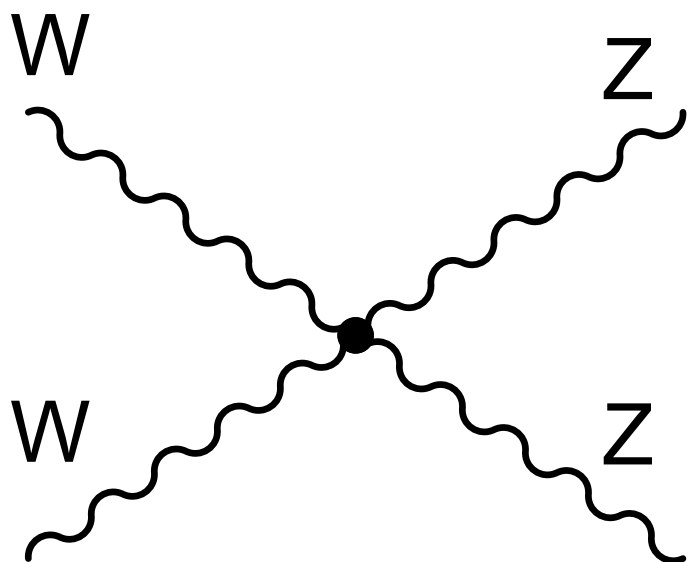
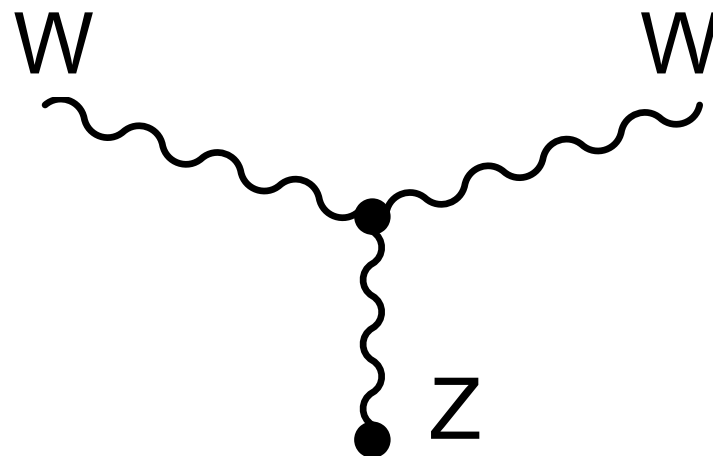
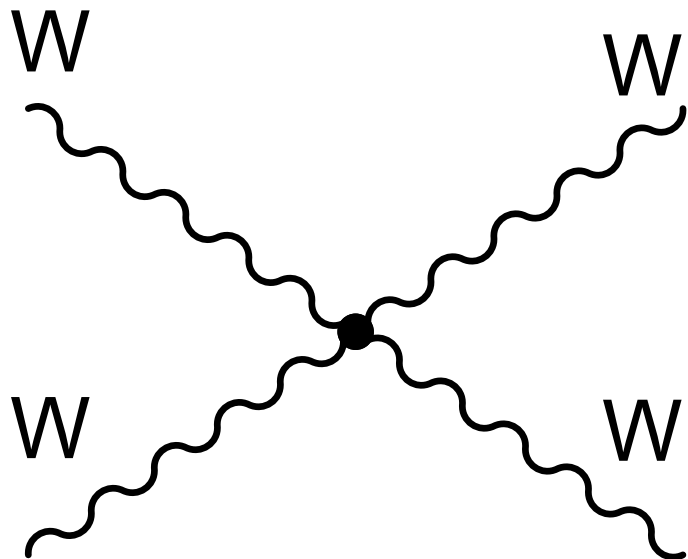
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Boson couplings in weak theory



In general, can always
replace a photon by a Z
boson in a diagram.
What about the reverse?

Boson couplings in weak theory



What are the s-channel and t-channel diagrams for $e^+e^- \rightarrow W^+W^-$? Which way do arrows go? Why? What about $e^+e^- \rightarrow \mu^+\mu^-$? What diagrams are there?

Particles... like to decay to lighter objects, unless there is a reason that they can't decay (such as a conservation law)

What is the most obvious reason for non-decay?

$$p^+ \rightarrow n e^+ \nu_e$$

Hint, look at the energy in the
rest frame

Momentum conservation

Angular momentum conservation

Conservation of charge

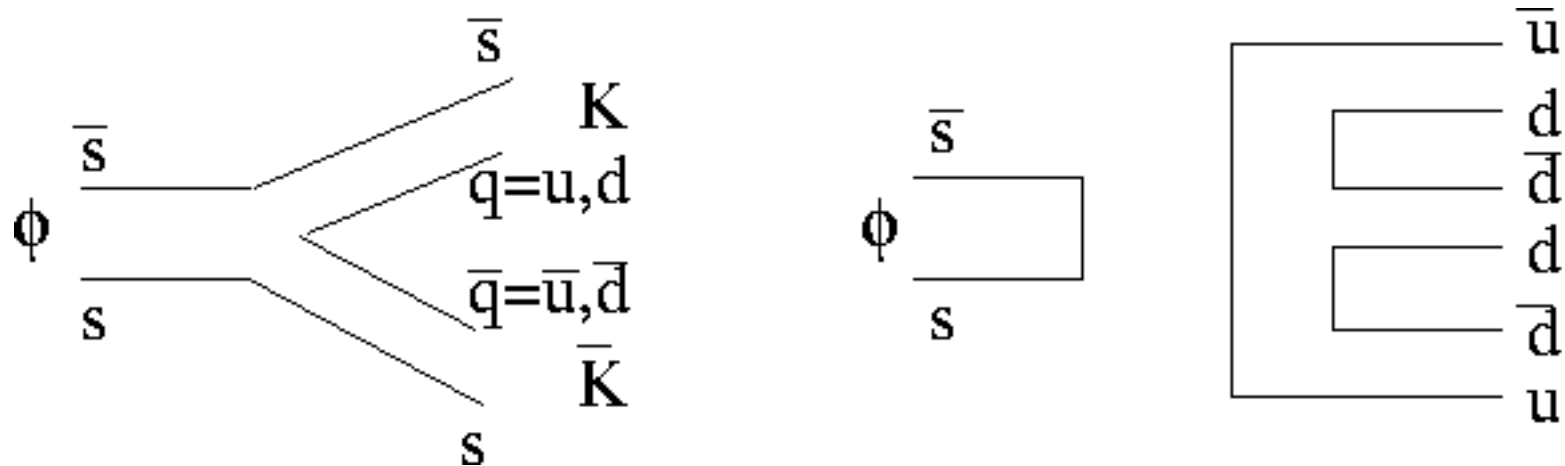
Conservation of color

Conservation of baryon number

Conservation of lepton (electron/muon/tau)
number

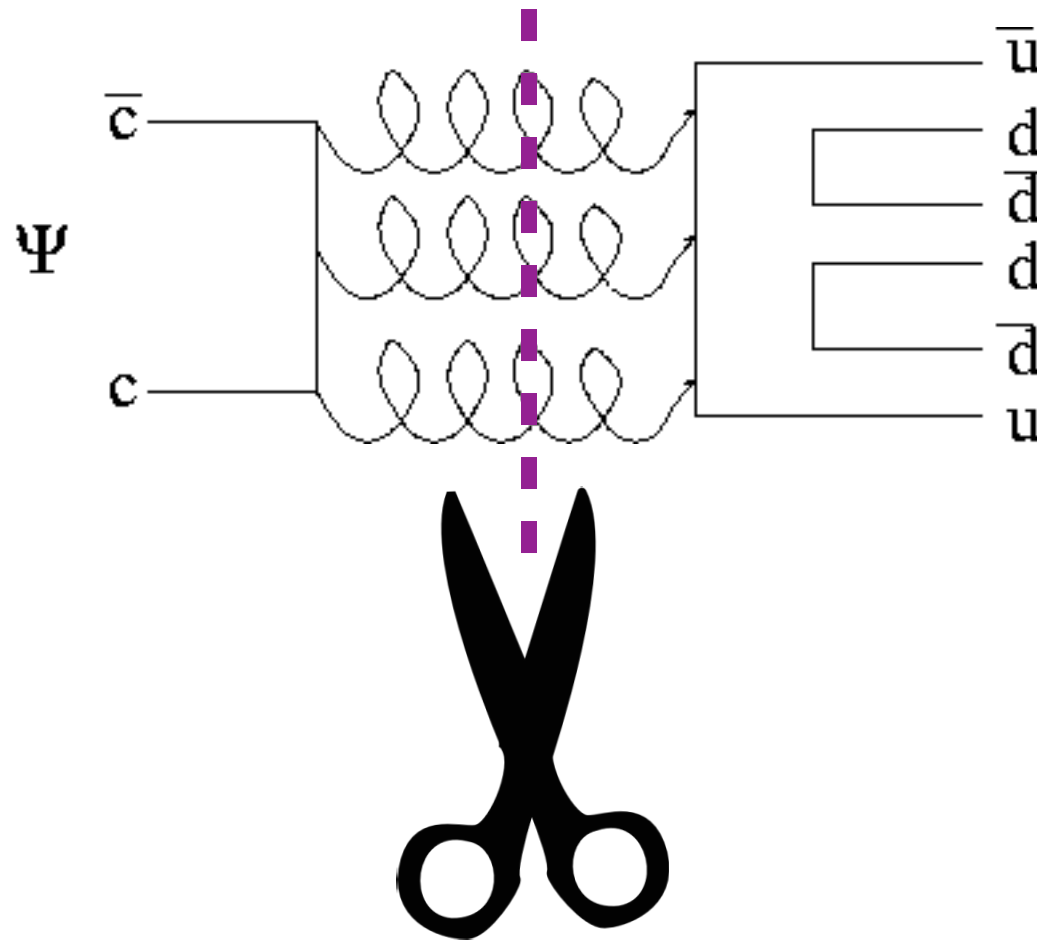
Quark flavor (not quite conserved)

https://www.ippp.dur.ac.uk/~krauss/Lectures/QuarksLeptons/QCD/Quarkonium_0.html



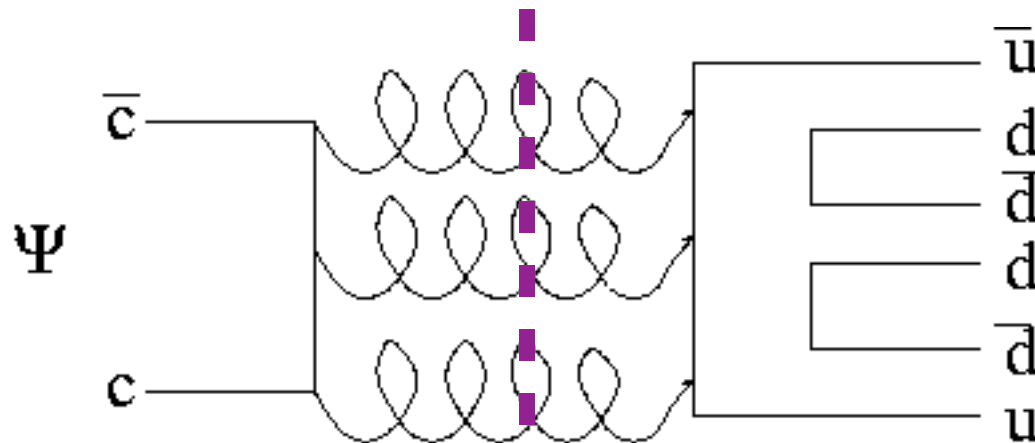
The ϕ decays much more commonly to $K \bar{K}$, despite a phase space preference for decays to three pions.
Why? The OZI rule...

<http://www.ippp.dur.ac.uk/~krauss/Lectures/QuarksLeptons/QCD/Equations/jpsidecay.gif>



OZI rule explains why the J/ψ takes so long to decay.
 What does this have to do with asymptotic freedom?

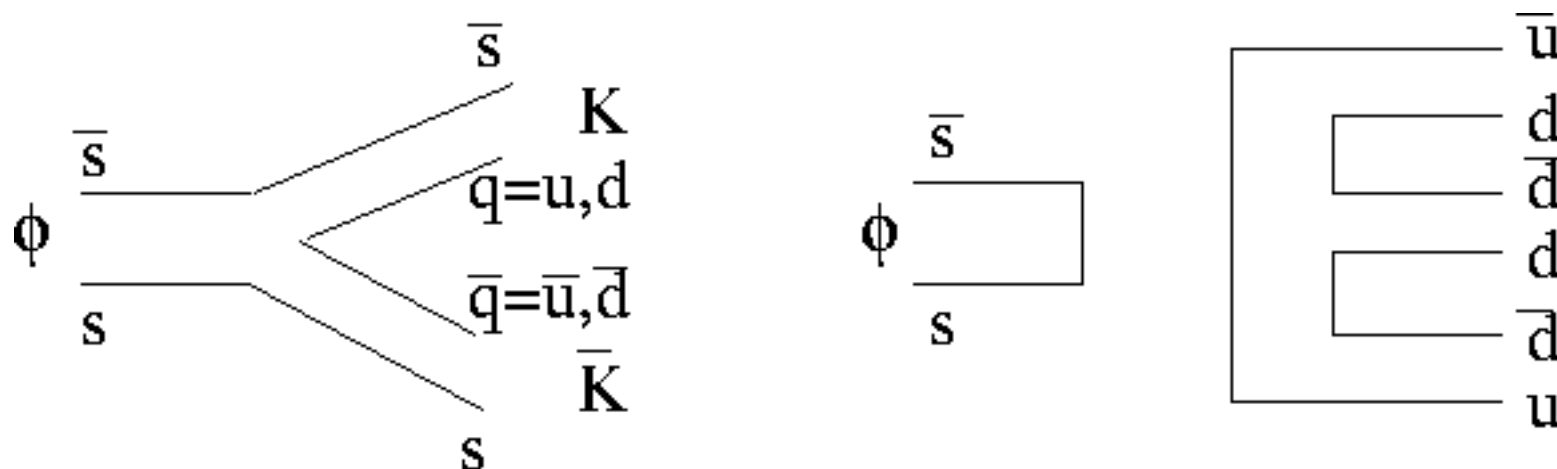
<http://www.ippp.dur.ac.uk/~krauss/Lectures/QuarksLeptons/QCD/Equations/jpsidecay.gif>



If there was a leftover quark, it could carry some of the initial energy in its rest mass. There isn't one here!



If we can make that cut, it means all the energy of the quarks is temporarily in the form of gluons. But QCD couplings decrease at high energy, so there is less probability of this happening



Explained by the OZI rule, let's go over this

$\phi(1020)$ DECAY MODES

	Mode	Fraction (Γ_i/Γ)	Scale factor/ Confidence level
Γ_1	$K^+ K^-$	(48.9 \pm 0.5) %	S=1.1
Γ_2	$K_L^0 K_S^0$	(34.2 \pm 0.4) %	S=1.1
Γ_3	$\rho\pi + \pi^+ \pi^- \pi^0$	(15.32 \pm 0.32) %	S=1.1
Γ_4	$\rho\pi$		
Γ_5	$\pi^+ \pi^- \pi^0$		

Photons can't decay (they already have zero mass - nothing lighter to decay into)

Protons are the lightest baryon, so baryon conservation tells us that they are stable

This is why the world is made up of protons, neutrons (which are stable inside nuclei), electrons and neutrinos

Decays are probabilistic - you never know when an object will decay, but you can say on average how long a type of object will take to decay

μ : 2.2×10^{-6} s

π^+ : 2.6×10^{-8} s

π^0 : 8.3×10^{-17} s

τ : 2.9×10^{-13} s

n (free): 880 s

top quark: 4×10^{-25} s

Many of these objects will decay to multiple final states with different, predicted **branching ratios**

Why so different?

Strong decays: 10^{-23} s (top quark)

EM decays: 10^{-16} s (π^0)

Weak decays: longer (neutron and muon)

The more (less) phase space for a decay, the faster (slower) it will occur.

See the free neutron





Photos: Internet screengrabs

OK, not a real physics explanation, but a good way to remember things

Griffiths
problems
1.19, 2.1, 2.2,
2.5, 2.6, 2.7,
2.8